

# Course Syllabus(modified)

Date	Topic	Instructor
2/25	Introduction and review	Chung-Ting Ke
3/4	Charge transport review and nanoelectronics I	Chung-Ting Ke
3/11	Charge transport review and nanoelectronics II	Chung-Ting Ke
3/18	Nano-optics	Yu-Chieh Wen
3/25	Quantum transport	Chen-Hsuan Hsu
4/1	Superconductivity	Tien-Ming Chuang
4/8	Superconducting theory and devices	Chung-Ting Ke
4/15	Midterm exam I	Chung-Ting Ke
4/22	Carbon-based nano-materials and 2D materials	Chung-Ting Ke
4/29	Thermoelectricity in nanoscale systems	Ou Min-Nan
5/6	Magnetism and magnetoelectronics (1)	Shang Fan Lee
5/13	Magnetism and magnetoelectronics (2)	Shang Fan Lee
5/20	Topological materials 1	Tien-Ming Chuang
5/27	Midterm II	Chung-Ting Ke
6/3	Study group oral presentation (I)	Chung-Ting Ke
6/10	Study group oral presentation (II)	Chung-Ting Ke

# Text book and Evaluation

## Textbook:

Nanostructures and nanotechnology by Douglas Natelson, Cambridge University Press (2015)

eBook available (<https://doi.org/10.1017/CBO9781139025485>) if accessed from AS domain.

## Evaluation:

Quiz and attendance 30%

Midterm I 20%

Midterm II 20%

Final presentation 40%

# Let's get to know each other

Chung-Ting Ke (Ting) 柯忠廷

Assistant Research Fellow in the Institute of Physics and RCCI

Research Field :

Quantum transport, Quantum materials

Topological system, Superconducting qubit

Expertise :

Low-temperature physics, low noise electrical measurement

Nanofabrication, 2D materials.



# Charge transport and nanoelectronics I&II

TIGP Advanced Nanotechnology

Chung-Ting Ke

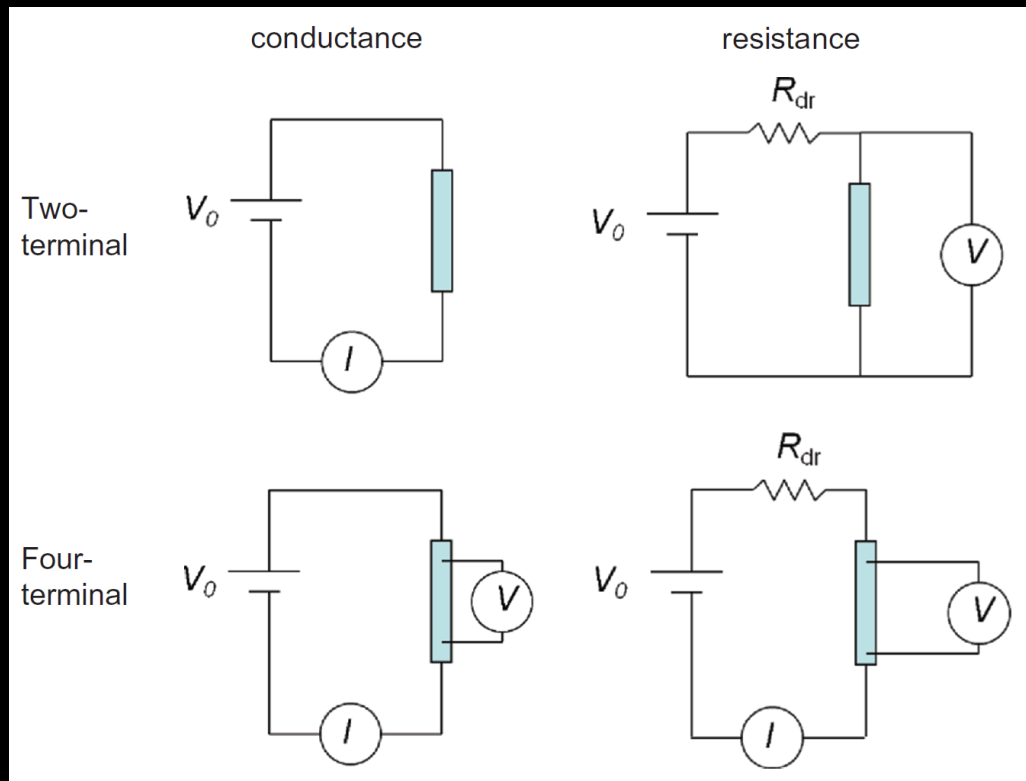
02/25/2026

**TIGP@AS**

# Charge transport and nanoelectronics

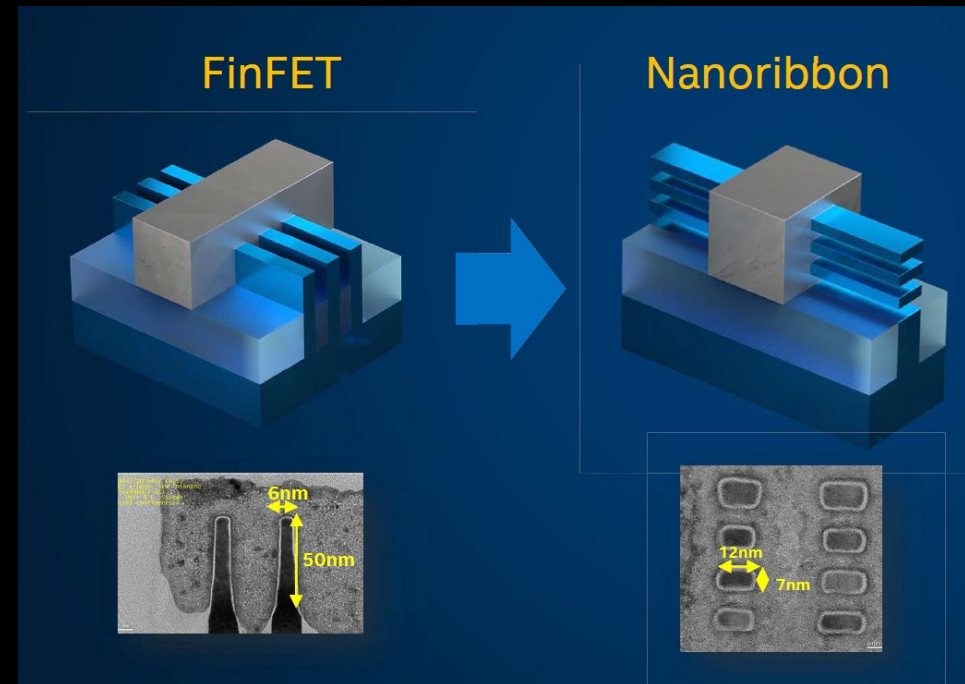
## What is the charge transport

Charge moving—electrical response



## Nanoelectronics

“Nano” means a scale — however, reference length scale is important!



# Outline – chapter 2-4

2.1 Free electrons

2.2 Nearly free electrons

2.3 Chemical approaches to electronic structure

2.4 More modern electronic structure methods

2.5 Lattice dynamics: phonons

3.1 Electronic types of solids

3.2 Metals

3.3 Inorganic semiconductors

3.4 Band insulators

3.5 Correlated oxides

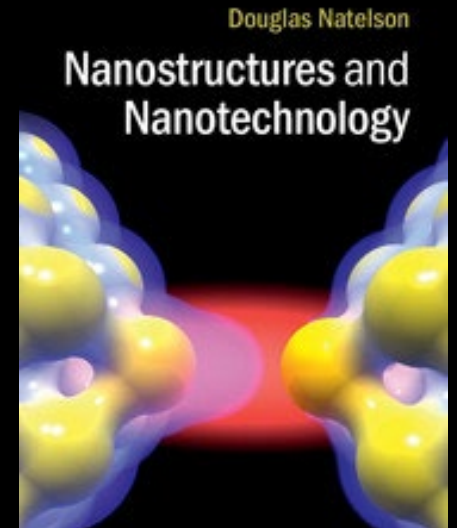
3.6 Molecular structures

4.1 Characterization

4.2 Materials growth

4.3 Material removal

4.4 Patterning



# Outline – chapter 5-6

**5.1 Defects**

**5.2 Interfaces and surfaces**

**5.3 Screening**

**5.4 Excitons**

**5.5 Junctions between materials**

**5.6 Quantum wires**

**5.7 Quantum dots**

**6.1 Transport terminology**

**6.2 Kinetic concepts**

**6.3 Hall effect**

**6.4 Quantum transport**

**6.5 The classical MOSFET**

**6.6 State-of-the-art**

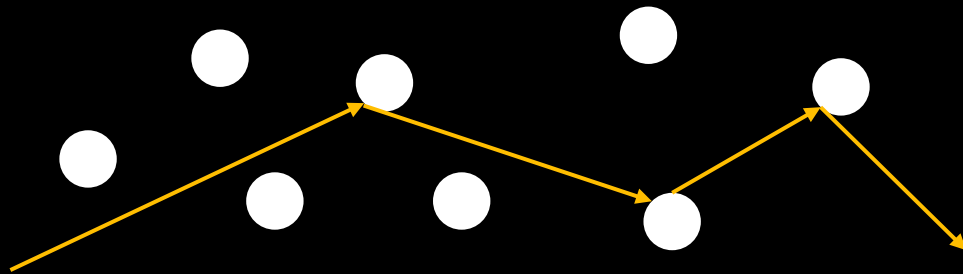
**6.7 Beyond CMOS**

# Transport 101

Earlier studies on metals are trying to understand electrons' behavior in metal materials

- Drude model

scattering mechanism happening between ions and electrons



DC conductivity can be described as

$$\mathbf{j} = \sigma \mathbf{E}, \sigma = \frac{ne^2\tau}{m}$$

Where  $\mathbf{j}$  is the current density,  $\sigma$  is the conductance,  $\mathbf{E}$  is the electric field  $n$  is the charge density  $m$  is the electron mass and  $\tau$  is the average time constant

# Transport 101

We would like to know the behavior of the electron(s)

$$-\frac{\hbar^2}{2m} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \psi(r) = \epsilon \psi(r)$$

- Free electron (Drude-Sommerfeld theory)

Simple, it can explain a lot of physics to a certain degree.

Several assumptions:

1. the interaction of ions and electrons away from the Fermi level is neglected.
2. electron-electron interaction is neglected.
3. The outcome of collision is treated with an average collision without considering the detail of the collision.
4. the electron distribution follows the Fermi-Dirac distribution.

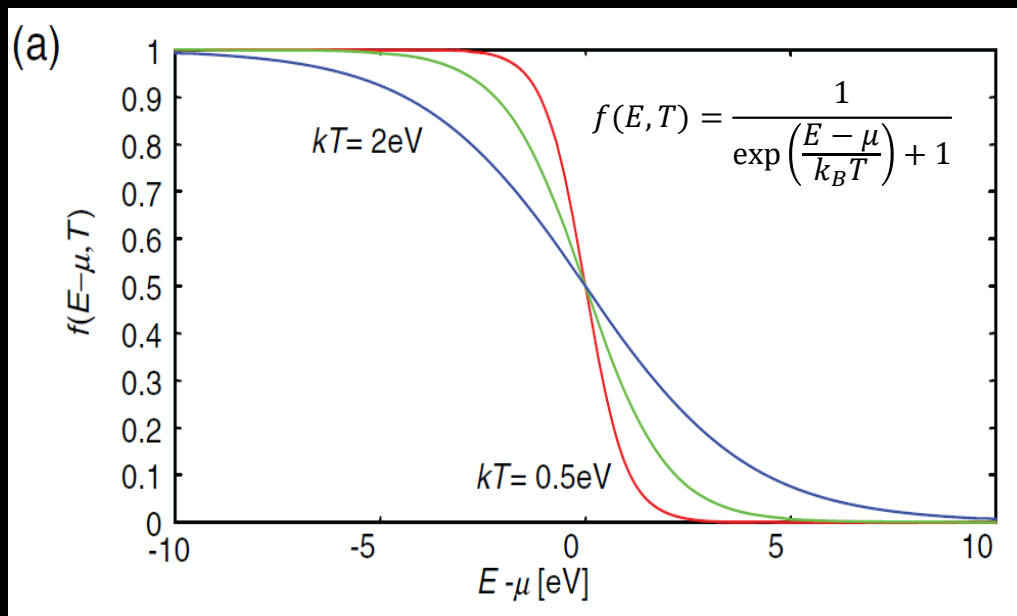
Despite the oversimplification, the free electron model has a great success in understanding a lot of phenomena

For example density of state, heat transport, Wiedemann-Franz law, etc.

# Transport 101

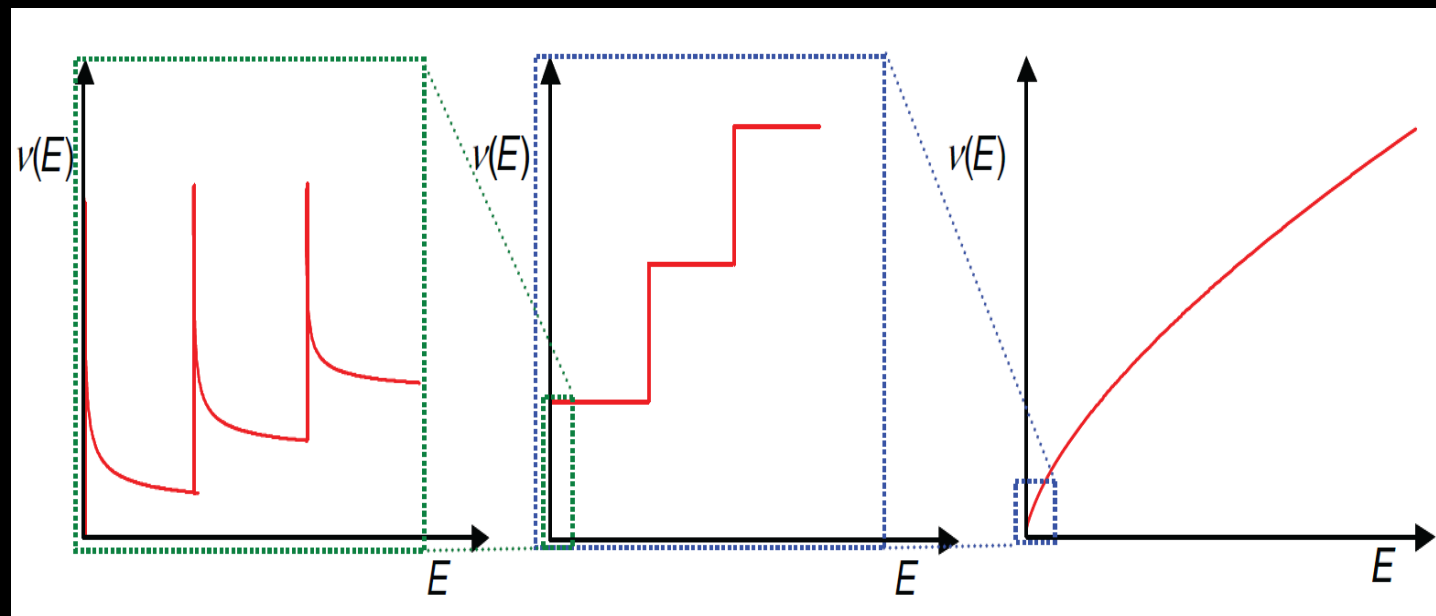
## Fermi Dirac distribution

For electron gas— Maxwell distribution doesn't work, Pauli exclusion leads to a Fermi Dirac distribution



## Density of state

For a small system, the allowed state to fill in a single particle is greatly depending on the confinement.



# Transport 101

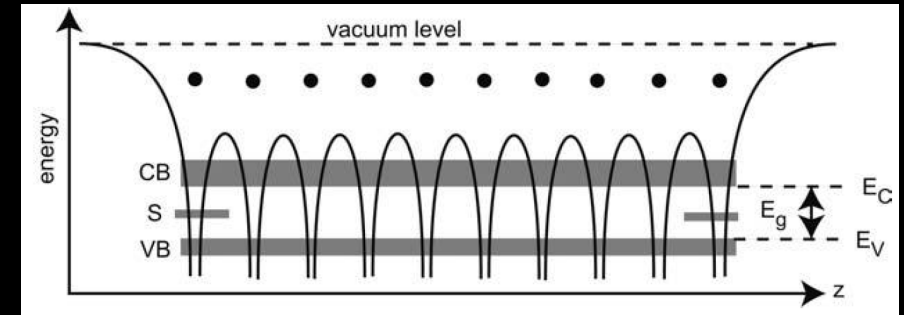
Degrees of freedom	Dispersion (kinetic energy)	Density of states	Effective density of states
3 (bulk)	$E = \frac{\hbar^2}{2m^*}(k_x^2 + k_y^2 + k_z^2)$	$\rho_{\text{DOS}}^{3\text{D}} = \frac{1}{2\pi^2} \left( \frac{2m^*}{\hbar^2} \right)^{\frac{3}{2}} \sqrt{E - E_C}$	$N_c^{3\text{D}} = \frac{1}{\sqrt{2}} \left( \frac{m^* kT}{\pi \hbar^2} \right)^{\frac{3}{2}}$
2 (slab)	$E = \frac{\hbar^2}{2m^*}(k_x^2 + k_y^2)$	$\rho_{\text{DOS}}^{2\text{D}} = \frac{m^*}{\pi \hbar^2} \sigma(E - E_C)$	$N_c^{2\text{D}} = \frac{m^*}{\pi \hbar^2} kT$
1 (wire)	$E = \frac{\hbar^2}{2m^*}(k_x^2)$	$\rho_{\text{DOS}}^{1\text{D}} = \frac{m^*}{\pi \hbar} \sqrt{\frac{m^*}{2(E - E_C)}}$	$N_c^{1\text{D}} = \sqrt{\frac{m^* kT}{2\pi \hbar^2}}$
0 (box)	–	$\rho_{\text{DOS}}^{0\text{D}} = 2\delta(E - E_C)$	$N_c^{0\text{D}} = 2$

# Transport 101

Bloch's Theorem  $\left(-\frac{\hbar^2}{2m}\nabla^2 + U(r)\right)\psi(r) = \varepsilon\psi(r)$

$$\varphi(\mathbf{r}) = e^{i\mathbf{k}\cdot\mathbf{r}} u_{\mathbf{k}}(\mathbf{r})$$

$$U(r) = U(r + R)$$



In a periodic potential created by ions or valence electrons.

We define a translation function  $T_R$ .

$$T_R f(\mathbf{r}) = f(\mathbf{r} + \mathbf{R}) \quad T_R \varphi(\mathbf{r}) = c(\mathbf{R}) \varphi(\mathbf{r}) \quad \text{and} \quad c(\mathbf{R}) = \exp(i\mathbf{k} \cdot \mathbf{R})$$

Now, we realize that  $T_R \varphi(\mathbf{r}) = \varphi(\mathbf{r} + \mathbf{R}) = \exp(i\mathbf{k} \cdot \mathbf{R}) \varphi(\mathbf{r})$

And we can define  $u_{\mathbf{k}}(\mathbf{r}) = \exp(-i\mathbf{k}\cdot\mathbf{r}) \varphi(\mathbf{r})$

Working out the math, we can get  $u_{\mathbf{k}}(\mathbf{r} + \mathbf{R}) = \exp(-i\mathbf{k}(\mathbf{r} + \mathbf{R})) \varphi(\mathbf{r} + \mathbf{R})$   
 $= \exp(-i\mathbf{k}\cdot\mathbf{r}) \varphi(\mathbf{r}) = u_{\mathbf{k}}(\mathbf{r})$

# Transport 101

## Band Structure

with the simple single-particle wavefunction, we can further impose the boundary condition, a Born-von Karman B.Cs. assume periodicity happened in  $a_i$  direction after  $N_i$  site.

$$\varphi(r + R), \text{ let } R = a_i N_i,$$

$R$  is also the Bravais lattice vector( recall of reciprocal lattice!)

If we use a cube lattice, we can have  $i=1-3$ , for three directions.

Bloch's theorem:  $\varphi(r + R) = \exp(ik a_i N_i) = \exp(2\pi i x_i N_i) = 1$ , note  $kR = 2\pi j$

From this equality, we know that the allowed  $k$  values,

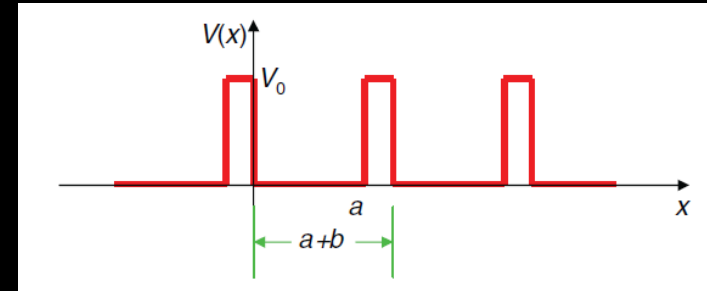
$$\mathbf{k} = \sum_{i=1}^3 \frac{j_i}{N_i} \mathbf{b}_i$$

Recap:

The primitive lattice vector  $\mathbf{R} = \sum_{i=1}^3 n_i \mathbf{a}_i$   
The reciprocal lattice vector  $\mathbf{G} = \sum_{i=1}^3 n_i \mathbf{b}_i$

Meaning, different to free electron case, multiple solutions!

# Transport 101



## 1D Band Structure (König Penney model)

Now we can calculate the simple 1D band structure under a periodic potential,

$$\psi(x) = Ae^{i\alpha x} + Be^{-i\alpha x},$$

$$\alpha \equiv \left[ \frac{2mE}{\hbar^2} \right]^{1/2},$$

$$a > x > 0,$$

$$\psi(x) = Ce^{\beta x} + De^{-\beta x},$$

$$\beta \equiv \left[ \frac{2m}{\hbar^2} (V_0 - E) \right]^{1/2},$$

$$-b < x < 0.$$

Bloch's theorem  $\psi(x) = e^{ikr} u_k(x)$

$$u_k(x) = Ae^{i(\alpha-k)x} + Be^{-i(\alpha+k)x}, \quad a > x > 0,$$

$$u_k(x) = Ce^{i(\beta-ik)x} + De^{-i(\beta+ik)x}, \quad -b < x < 0.$$

Working out the continuity conditions  $u_k(x)$ ,  $du_k(x)/dx$  and periodic in  $a+b$

One arrives at the energy-k relationship

$$\cos(\alpha a) \cosh(\beta b) + \frac{\beta^2 - \alpha^2}{2\alpha\beta} \sin(\alpha a) \sinh(\beta b) = \cos(k(a+b)).$$

For  $E > V_0$  and  $V_0$  goes to  $\infty$  and  $b$  goes to 0,

$$\cos(ka) = \cos(\alpha a) + (p \sin(\alpha a)) / (\alpha a) \quad \frac{1}{2} \beta a b = p$$

# Transport 101

## 1D Band Structure (König Penney model)

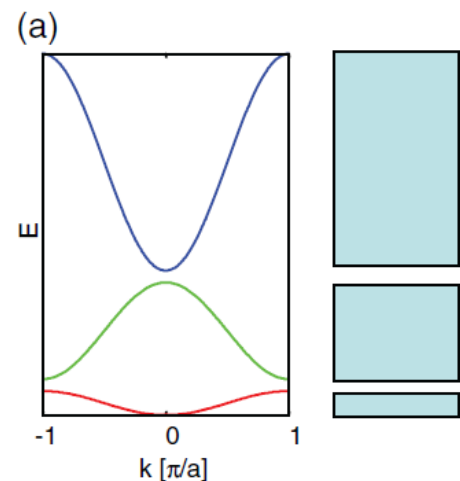
From the previous calculation, energy as the function of  $k$ :  $F(E) = \cos(k(a + b))$

For  $|F(E)| > 1$ ,  $k$  will have to be imaginary, therefore, it is forbidden.

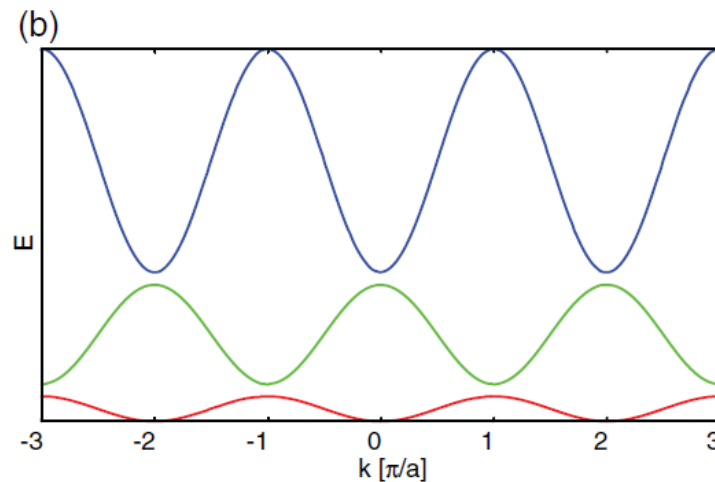
Under a weak potential case and more electrons, one can arrive the 1D band structure.

(See Ashcroft/Mermin ch8 to ch9)

First Brillouin zone



Repeating zone



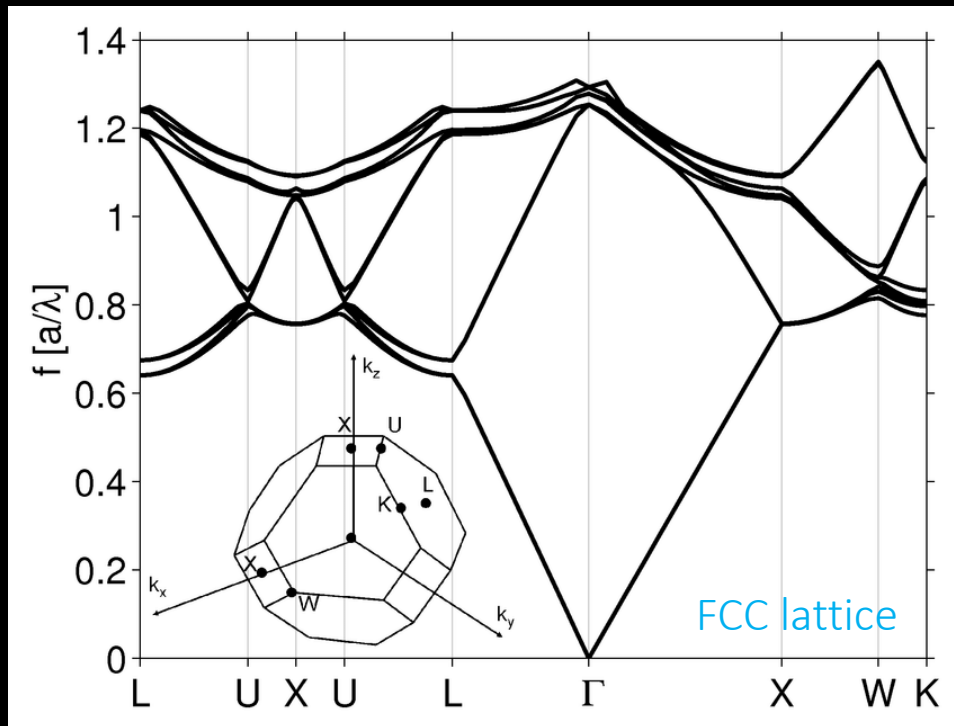
Again, one can prove that outside the FBZ is only repeating :

$$\begin{aligned}\psi_{n,\mathbf{k}+\mathbf{G}}(\mathbf{r}) &= \exp(i(\mathbf{k} + \mathbf{G}) \cdot \mathbf{r})u_{n,\mathbf{k}+\mathbf{G}}(\mathbf{r}) \\ &= \exp(i\mathbf{k} \cdot \mathbf{r})[u_{n,\mathbf{k}+\mathbf{G}}(\mathbf{r}) \exp(i\mathbf{G} \cdot \mathbf{r})] \\ &= \exp(i\mathbf{k} \cdot \mathbf{r})\tilde{u}(\mathbf{r}) \\ &= \psi_{n',\mathbf{k}}(\mathbf{r}).\end{aligned}$$

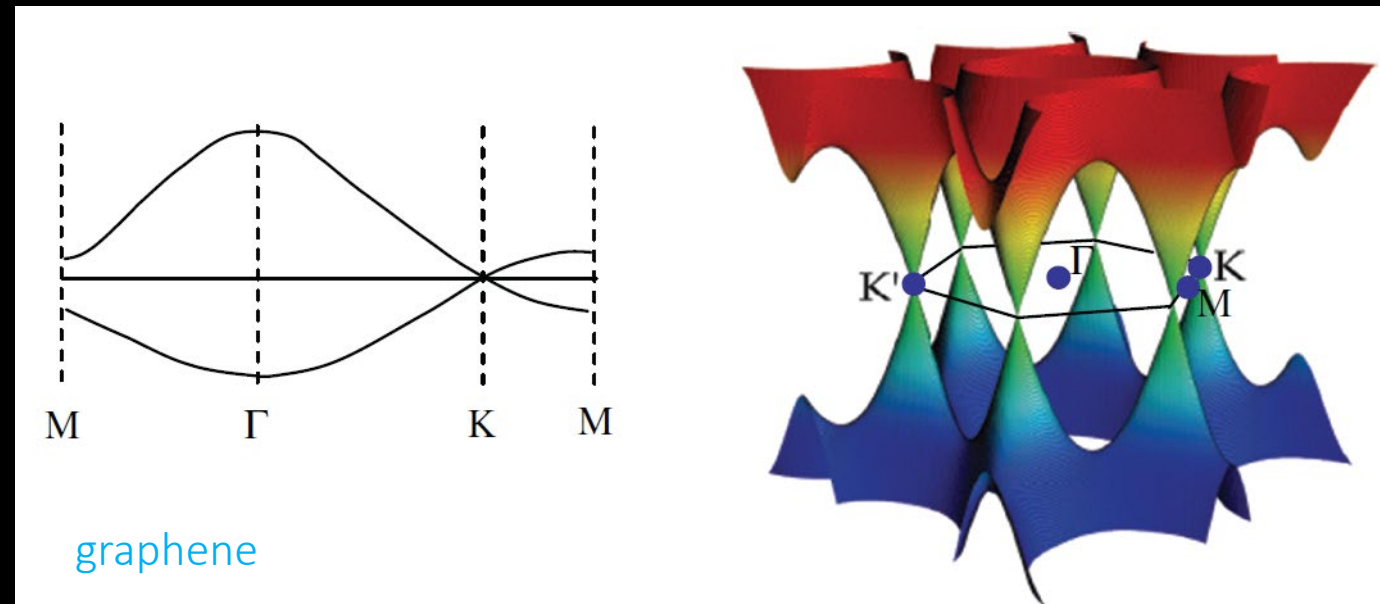
# Transport 101

Other methods to calculate the band structure:

Tight-Binding model, k p theory(effective mass/spin-orbit), green function, etc.  
Exact band structure is much more complicated!



Celine Vion et al. JAP (2009)



Ref: <http://lampx.tugraz.at/~hadley/ss1/empty/empty.php>

# Transport 101

Density of levels and van hove singularity:

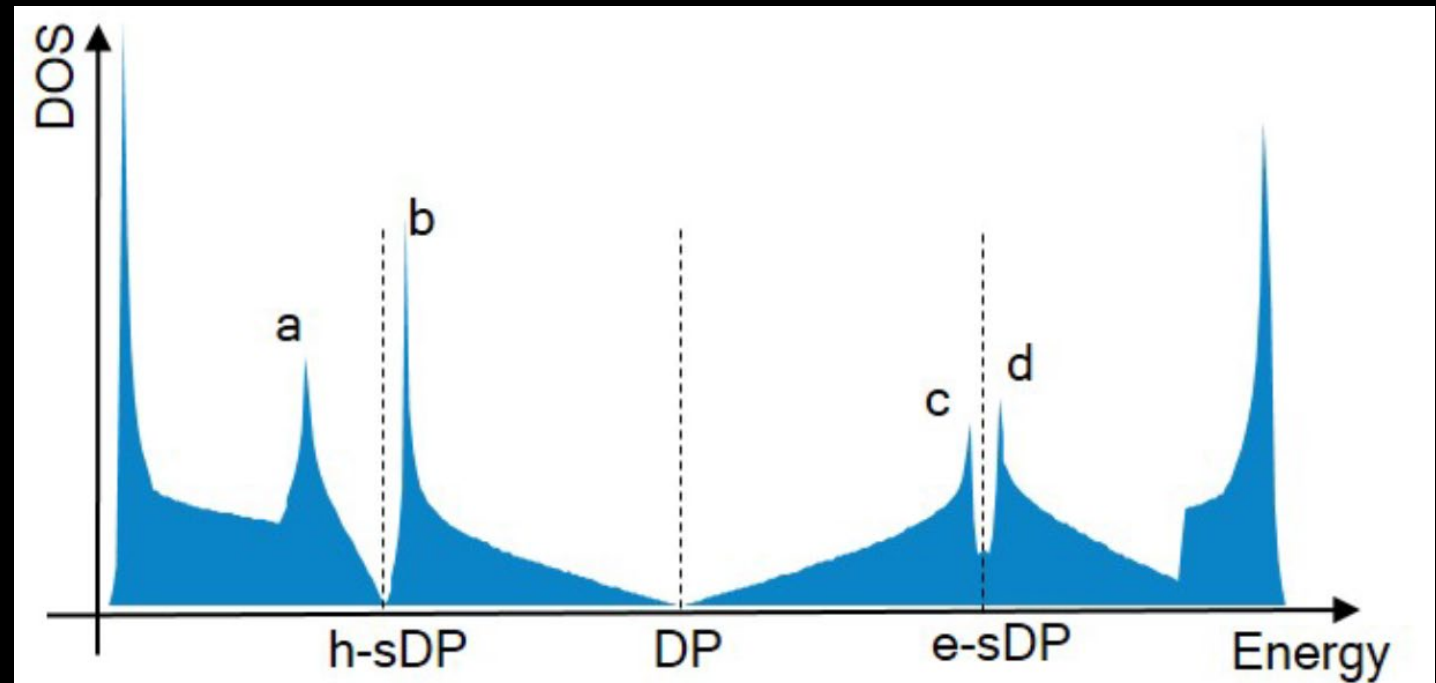
We can calculate the weighted sum over the electronic levels, like DOS in the free electron case. ( A&M Ch8)

$$g_n(\varepsilon)d\varepsilon = \int_{S_n(\varepsilon)} \frac{dS}{4\pi^3} \delta k(\mathbf{k})$$

$$\delta k(\mathbf{k}) = \frac{d\varepsilon}{|\nabla\varepsilon|}$$

$$g_n(\varepsilon) = \int_{S_n(\varepsilon)} \frac{dS}{4\pi^3} \frac{1}{|\nabla\varepsilon|}$$

When  $|\nabla\varepsilon|=0$  we have a divergence of  $dg_n/d\varepsilon$  is called van Hove singularities



# Transport 101

Density of levels and van hove singularity:

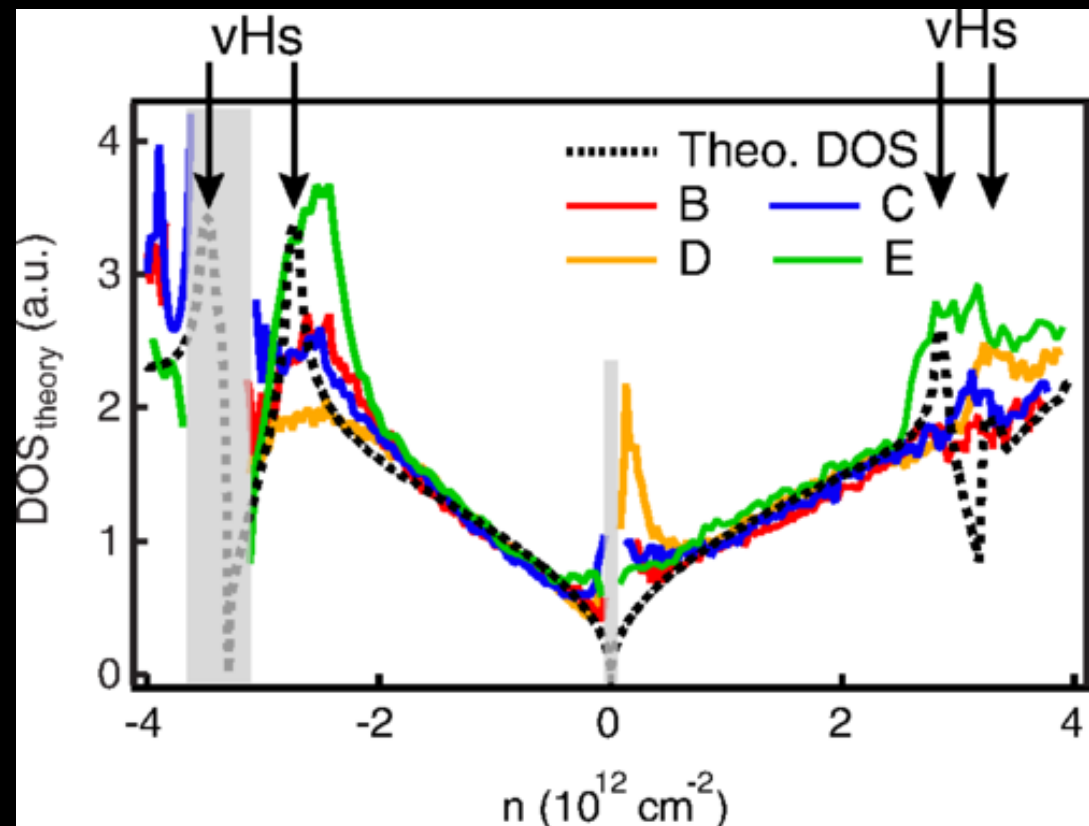
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# Type of materials

Metal

Insulator

Semiconductor

Superconductor

Topological material

# Type of materials

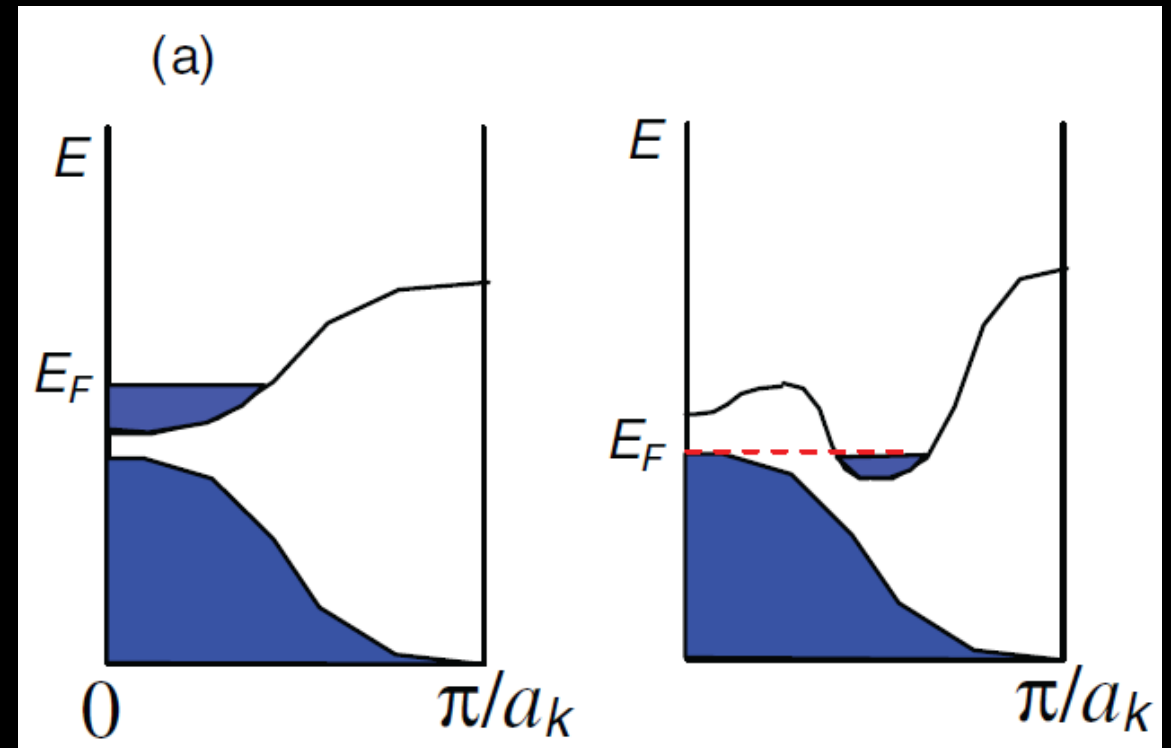
Metal

Insulator

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Superconductor

Topological material



Consider  $e/h$  as quasiparticle states

with a lifetime  $\tau$ , so energy uncertainty,  $\Gamma \sim \hbar/\tau$ , to have a well-defined quasiparticles  $\Gamma \ll k_B T$ . Under certain conditions, we can treat them as non-interacting Fermi liquid.

# Type of materials

Metal

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Topological material

Typical metal:

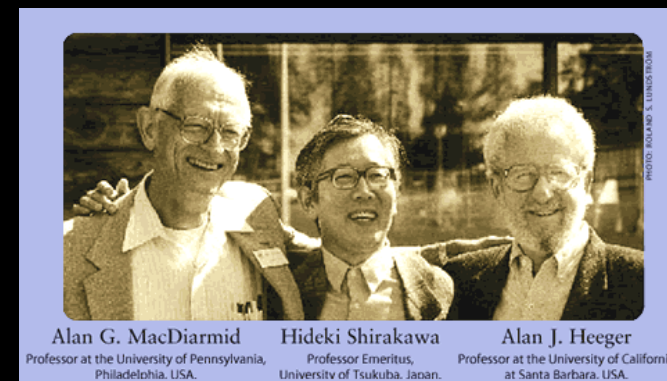
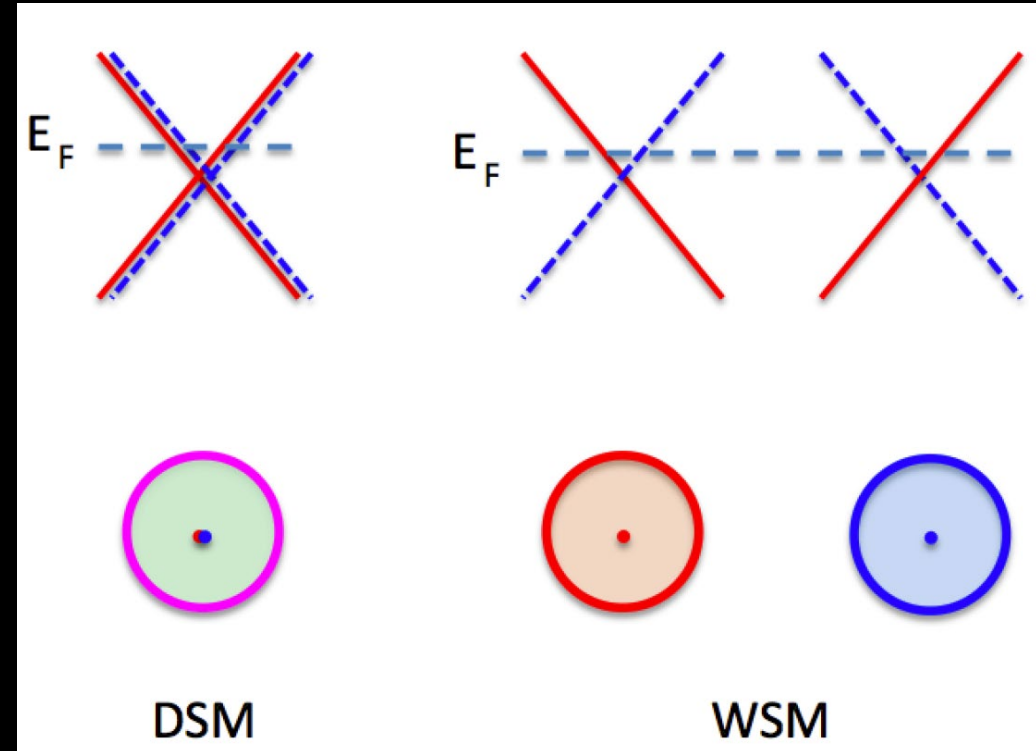
Akali, Nobel, transition and

Rare earth metals.

Yet, there are also organic metals!!

2000 Nobel prize in chemistry

Semimetal



# Type of materials

Metal

Insulator

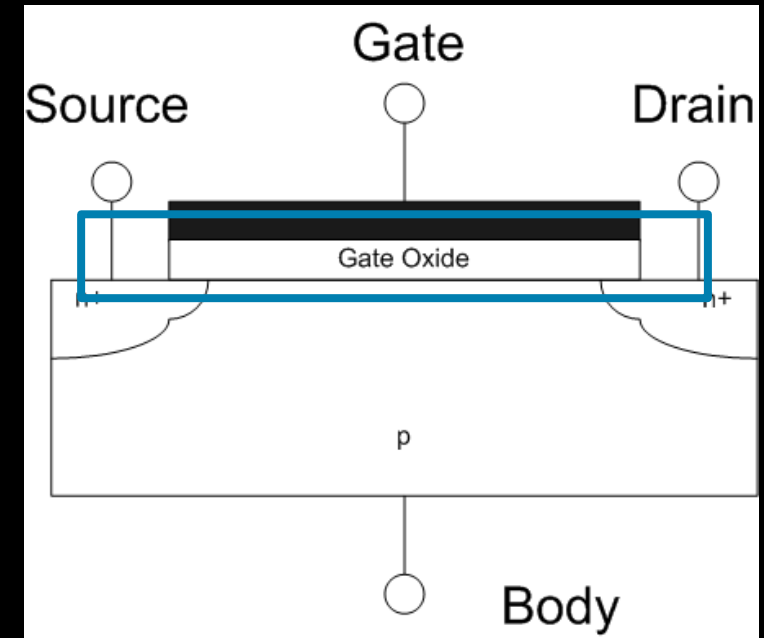
Semiconductor

Superconductor

Topological material

One of the key elements in many mesoscopic devices. For example, MOSFET can use high  $k$  materials for the gate dielectric, allowing a much better gate response and lower leakage.

Potential materials:  $\text{HfO}_4\text{Si}$ ,  $\text{HfO}_2$  etc.



# Type of materials

Metal

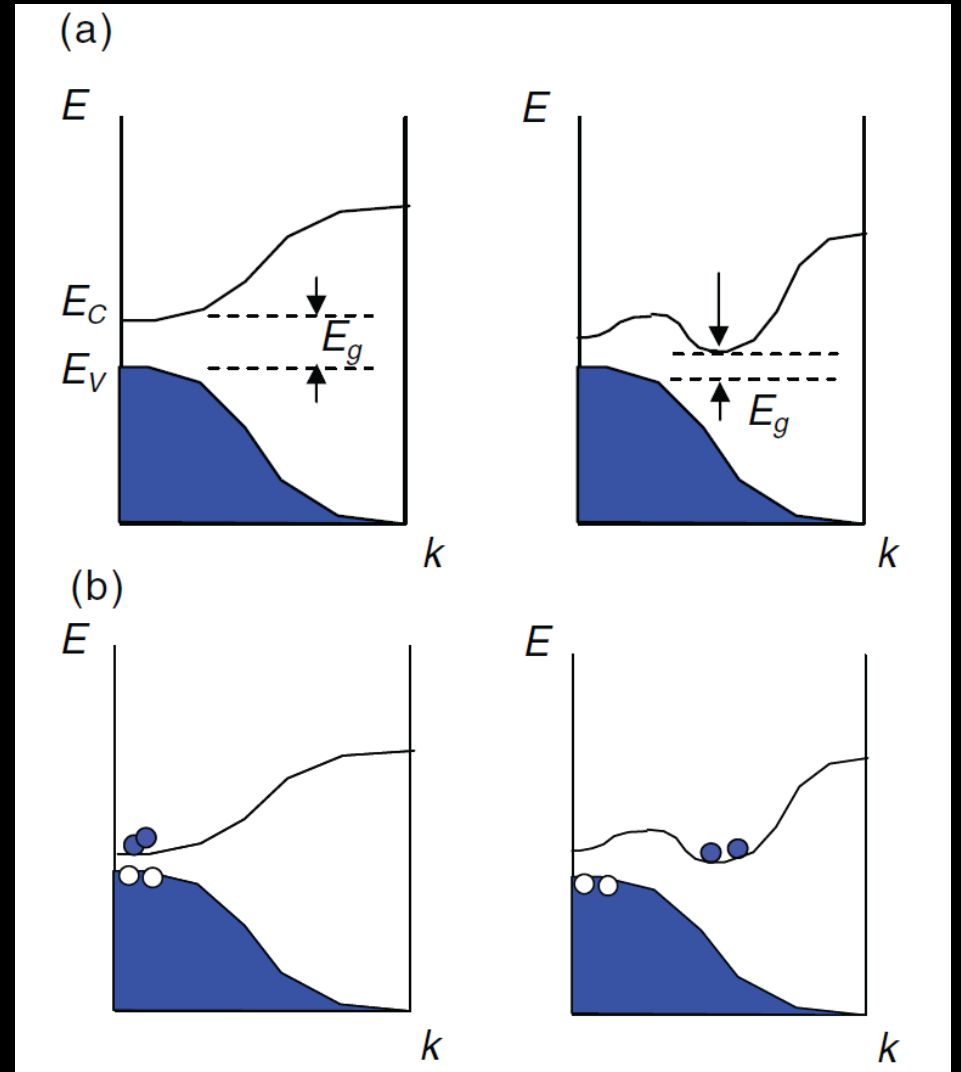
Insulator

Semiconductor

Superconductor

Topological material

A small bandgap of materials, there are direct (Ge) and indirect band gaps(Si). The gap value is in a range of 0.1 to 2 eV (300 K ~ 26 meV). Therefore, they are not very conductive at room temperature!



# Type of materials

Metal

Insulator

Semiconductor

Superconductor

Topological material

$$n = \int_{E_C}^{E_{\text{top}}} \nu_e(E) f(E, E_F, T) dE,$$

$$n = \left[ 2 \left( \frac{2\pi m_e^* k_B T}{\hbar^2} \right)^{3/2} M_C \right] \cdot \exp \left( -\frac{E_C - E_F}{k_B T} \right)$$
$$= N_C(T) \cdot \exp \left( -\frac{E_C - E_F}{k_B T} \right).$$

$$p = \left[ 2 \left( \frac{2\pi m_h^* k_B T}{\hbar^2} \right)^{3/2} \right] \cdot \exp \left( -\frac{E_F - E_V}{k_B T} \right)$$
$$= N_V(T) \cdot \exp \left( -\frac{E_F - E_V}{k_B T} \right),$$

# Type of materials

Metal

Insulator

Semiconductor

Superconductor

Topological material

$$n_i \equiv \sqrt{np} = \sqrt{N_C N_V} \cdot \exp\left(-\frac{E_g}{2k_B T}\right)$$

$$n_i = 4.9 \times 10^{15} \left(\frac{m_e^* m_h^*}{m_0^2}\right) M_C^{1/2} T^{3/2} \exp\left(-\frac{E_g}{2k_B T}\right)$$

Typical values of carrier density at 300 K:

Si ( $10^{10} \text{ cm}^{-3}$ ), Ge ( $10^{13} \text{ cm}^{-3}$ ) and GaAs ( $10^6 \text{ cm}^{-3}$ )

While for Cu  $10^{22} \text{ cm}^{-3}$  (depending on the number of the outer shell electrons)

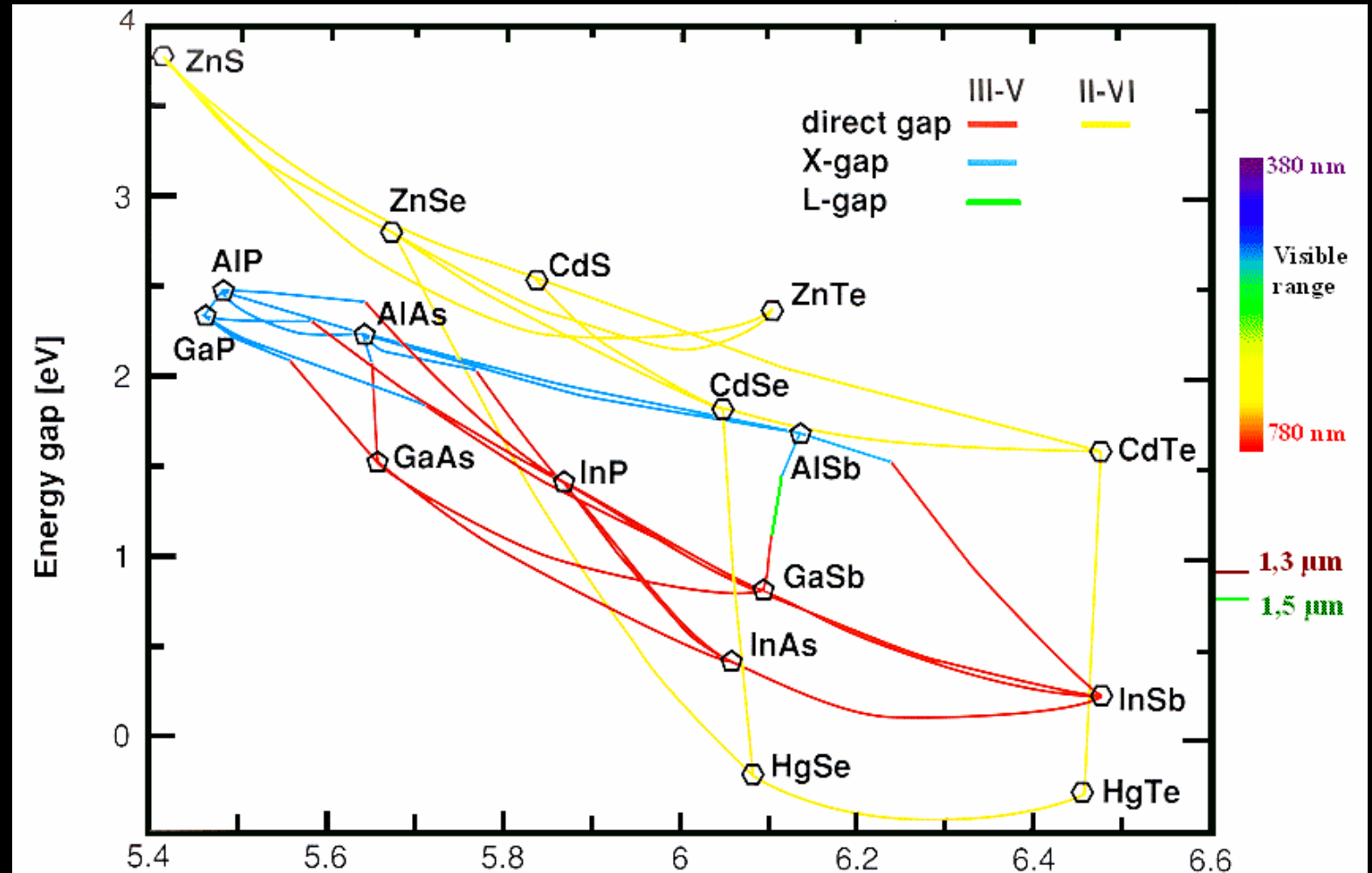
To increase conductivity of semiconductor, one can add dopants.

# Type of materials

<https://www.tf.uni-kiel.de/>

- Metal
- Insulator
- Semiconductor
- Superconductor
- Topological material

Besides elements, there are a lot of compound semiconductors.



# Type of materials

Metal

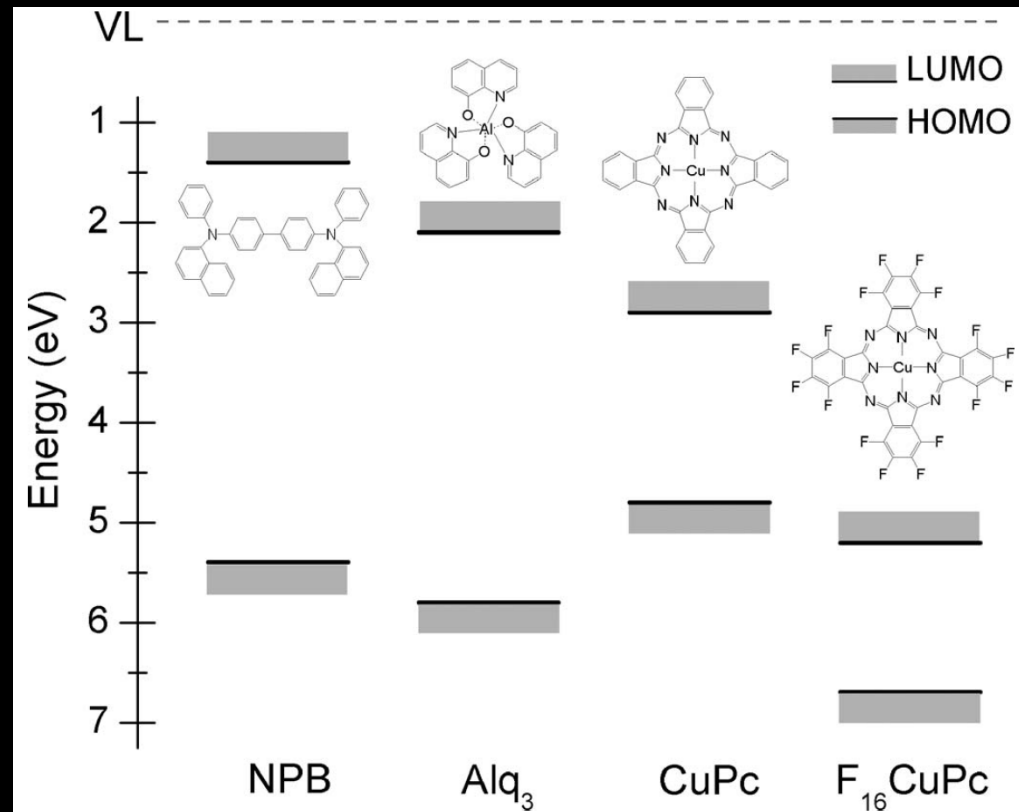
Insulator

Semiconductor

Superconductor

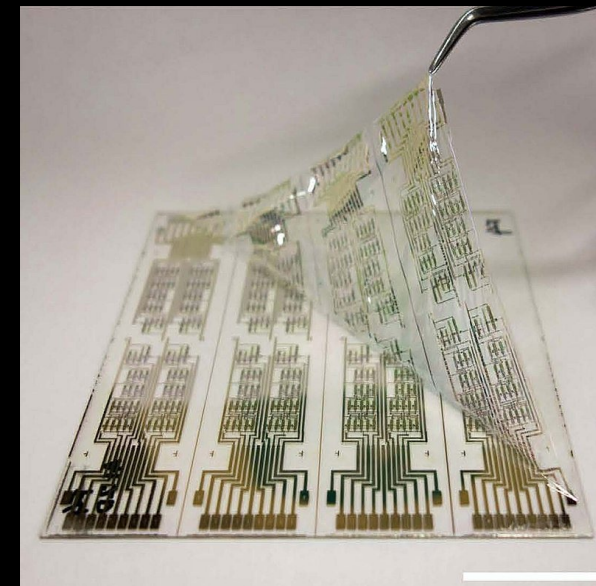
Topological material

The other is the organic semiconductors which are used in OLED/solar cell applications.



J. X. Tang et al, J. Appl. Phys. 101, (2007)

Wikipedia



# Type of materials

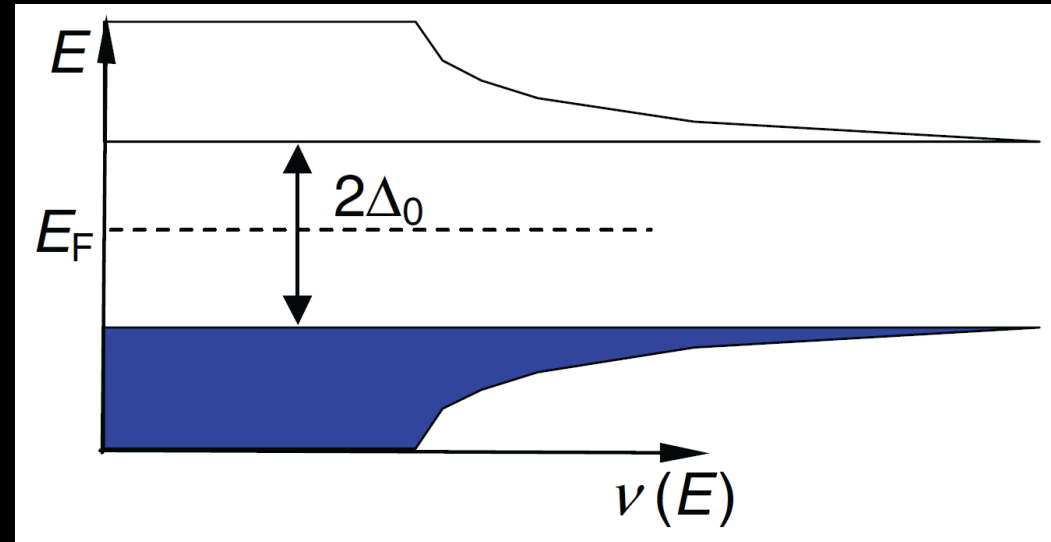
Metal

Insulator

Semiconductor

**Superconductor**

Topological material



Some properties:

1. below  $T_c$ , forming a zero DC resistance state
2. cooper pair is two electrons with coupling strength in the order of superconducting gap.
3. Meissner effect, the magnetic field lines exclusion effect

# Type of materials

Metal

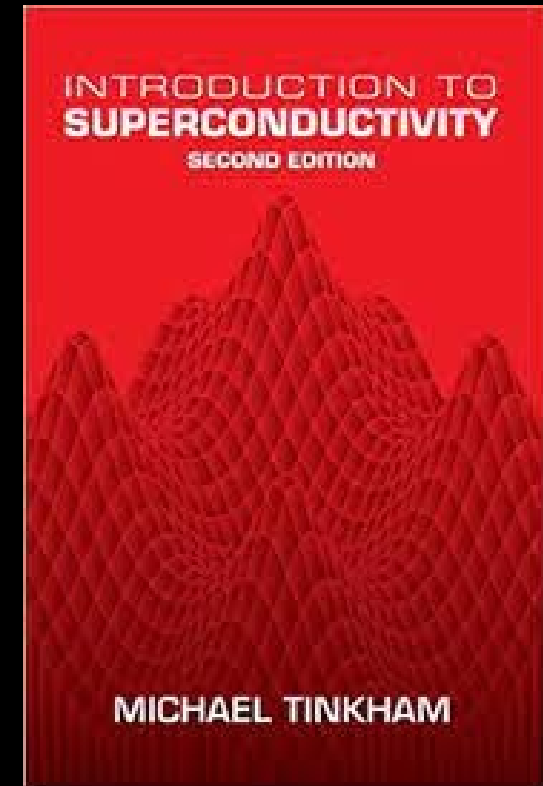
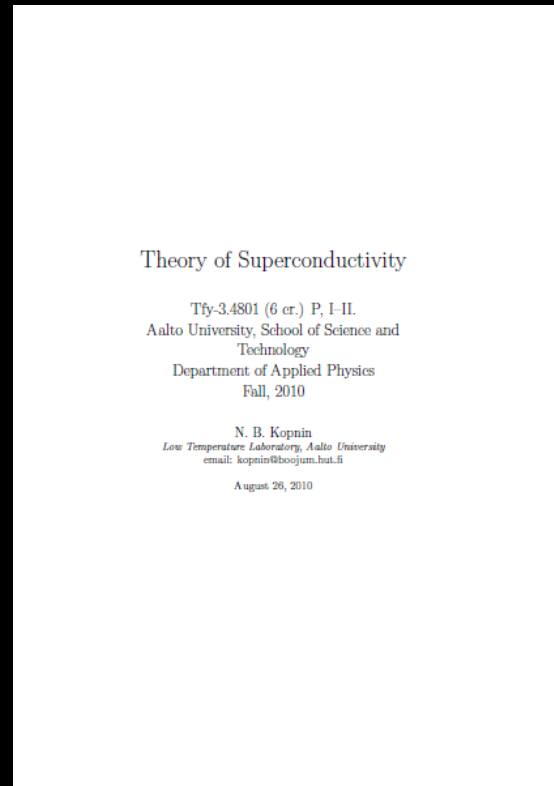
Insulator

Semiconductor

**Superconductor**

Topological material

Important theory for SC:  
highly recommended books  
for superconductivity



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Semiconductor

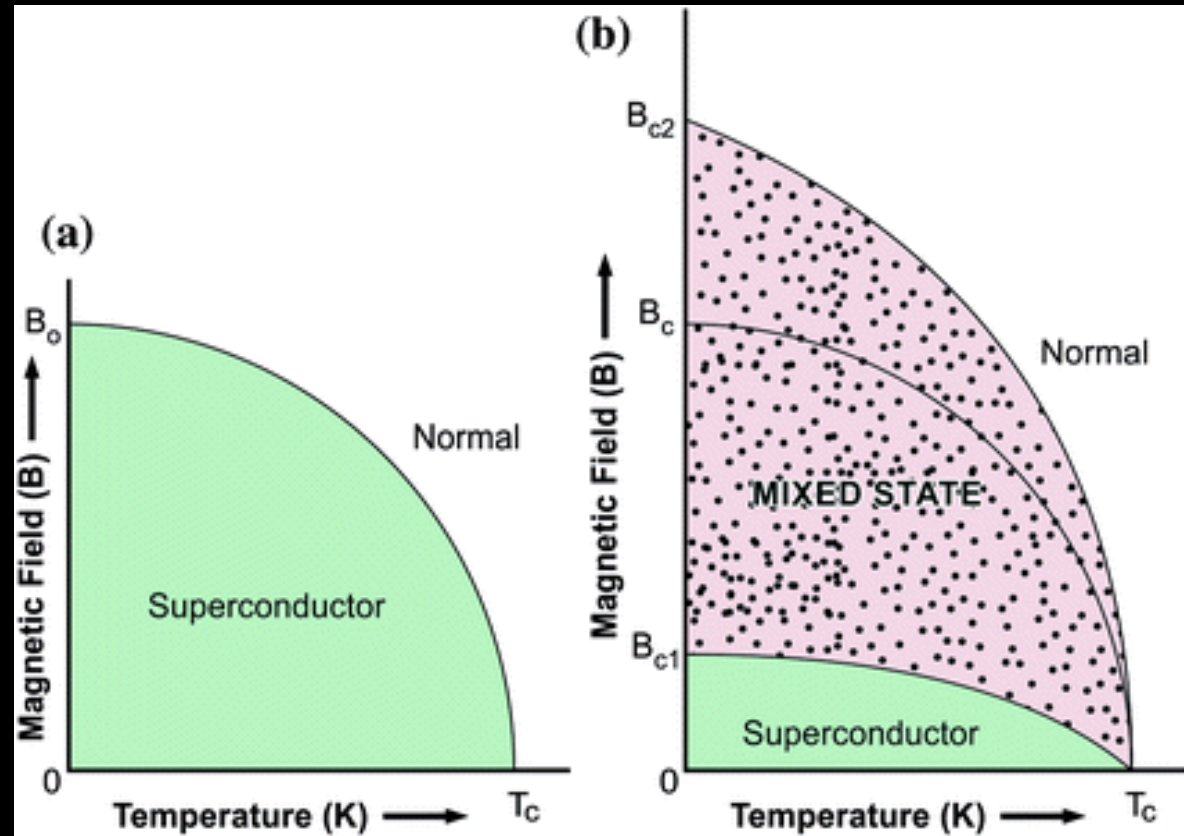
Superconductor

Topological material

Type of superconductors:

Type I

Type II



R. G. Sharma

# Type of materials

Metal

Insulator

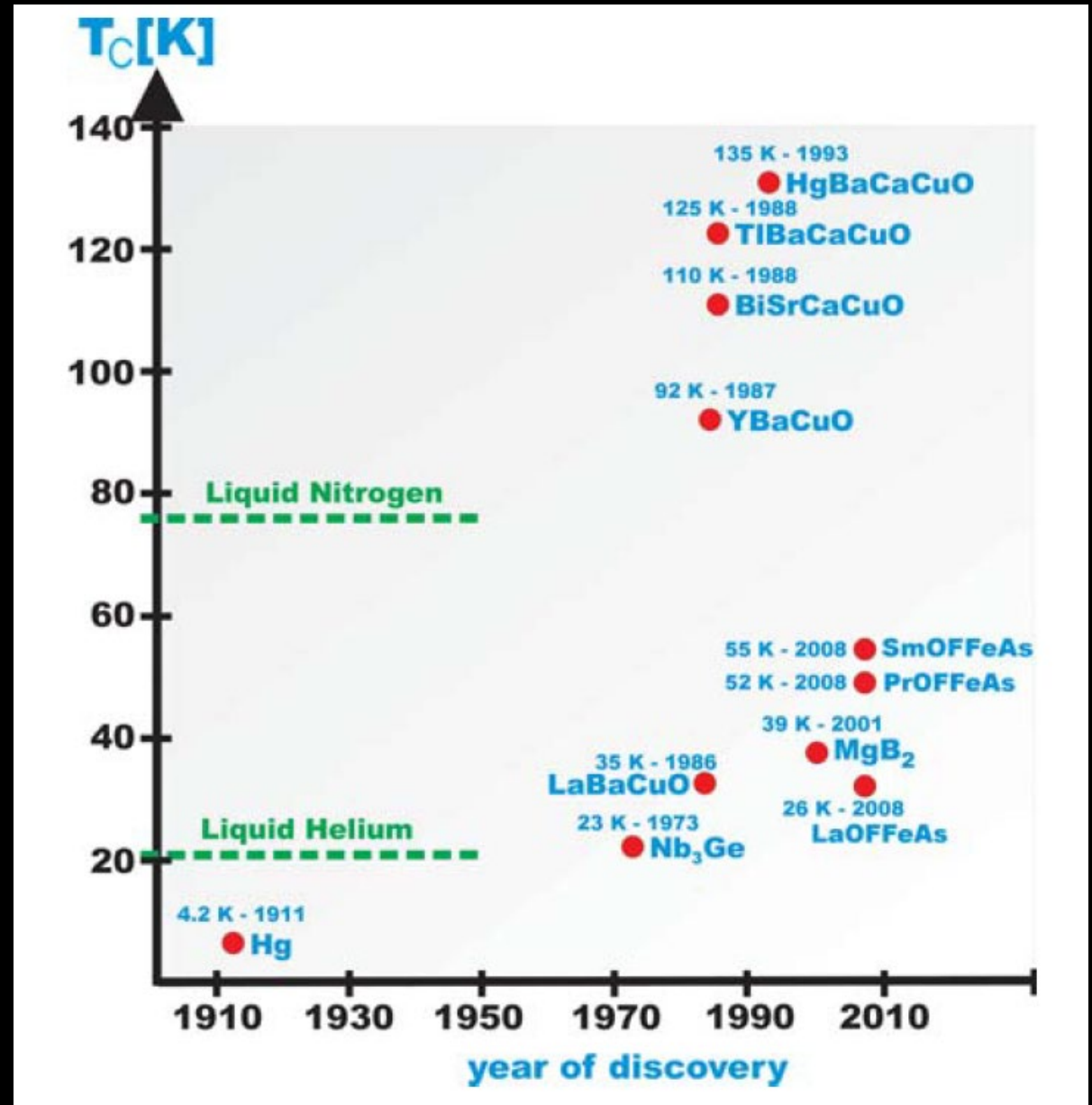
Semiconductor

Superconductor

Topological material

Type of superconductors:

High  $T_c$  superconductors



# Type of materials

Metal

Insulator

Semiconductor

Superconductor

Topological material

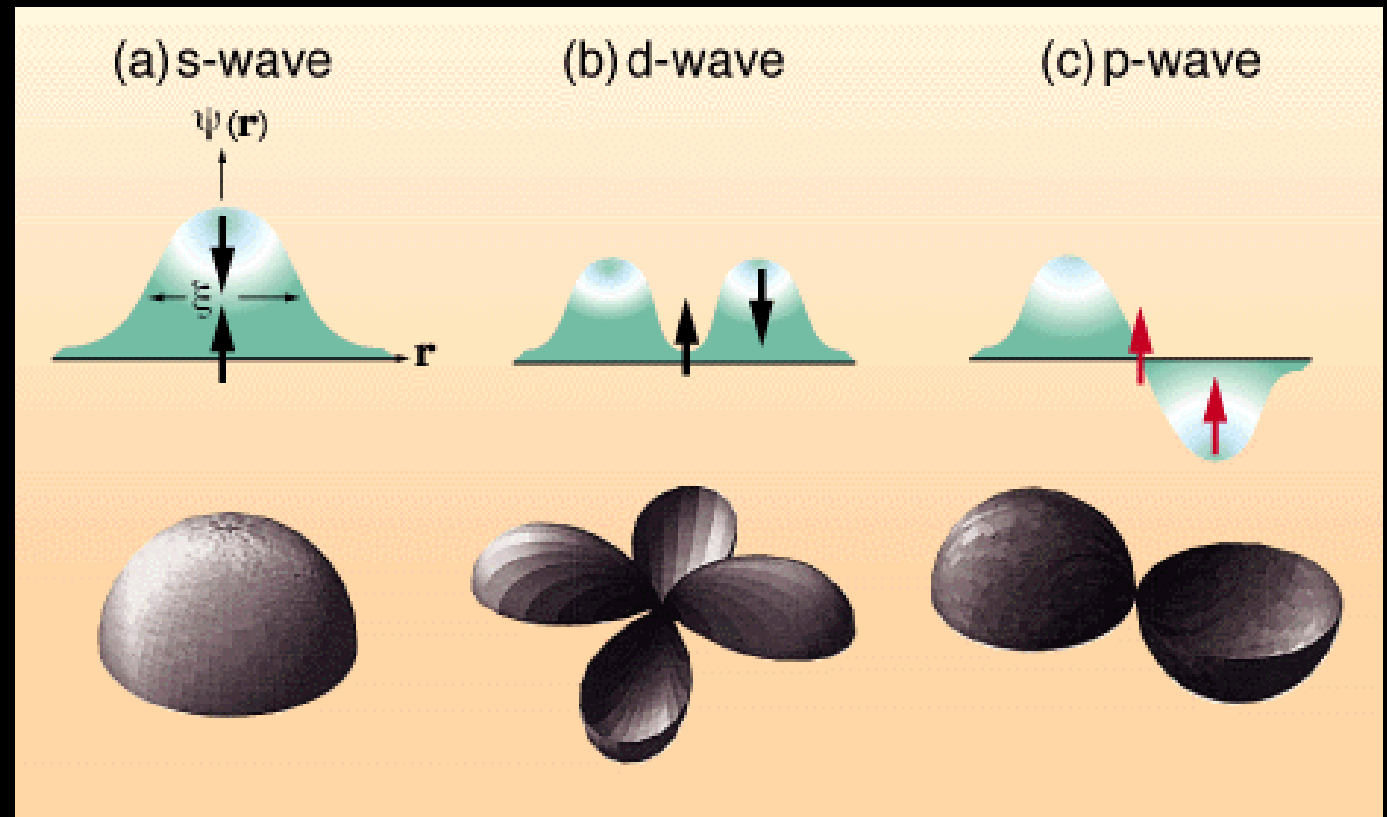
Type of superconductors:

s-wave

d-wave

p-wave?

Order parameter symmetry



# Type of materials

Metal

Insulator

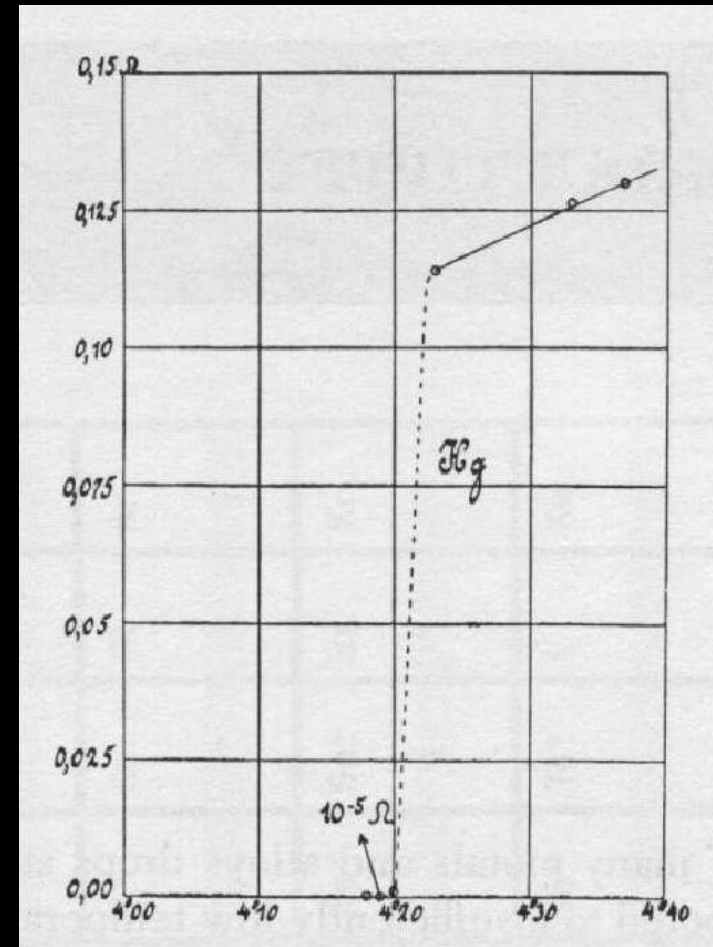
Semiconductor

Superconductor

Topological material

Bogoliubov–de Gennes equations

A theory to describe excitation spectrum for inhomogeneous superconductors



Kittel, Introduction  
to Solid State Physics

# Type of materials

Metal

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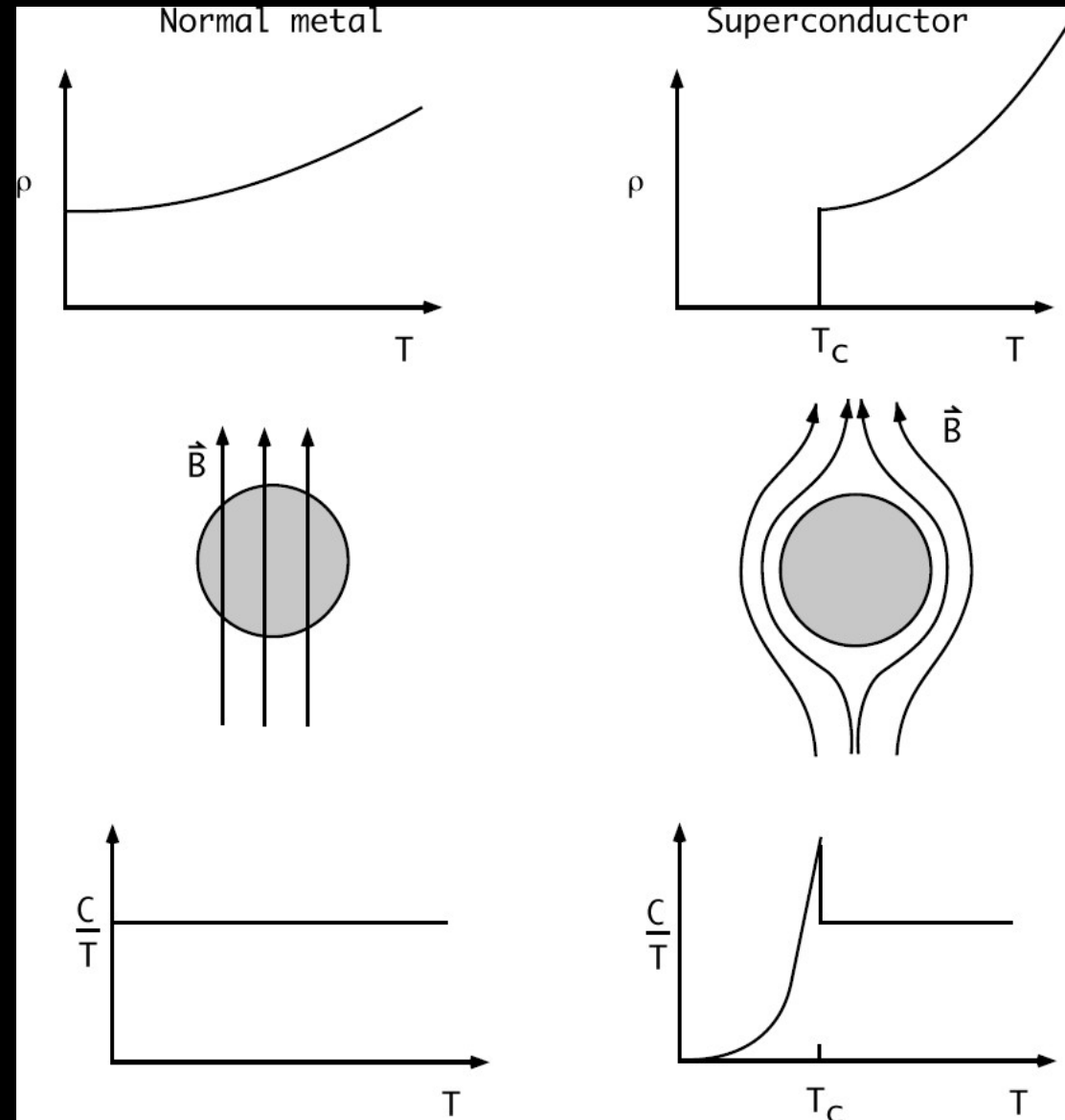
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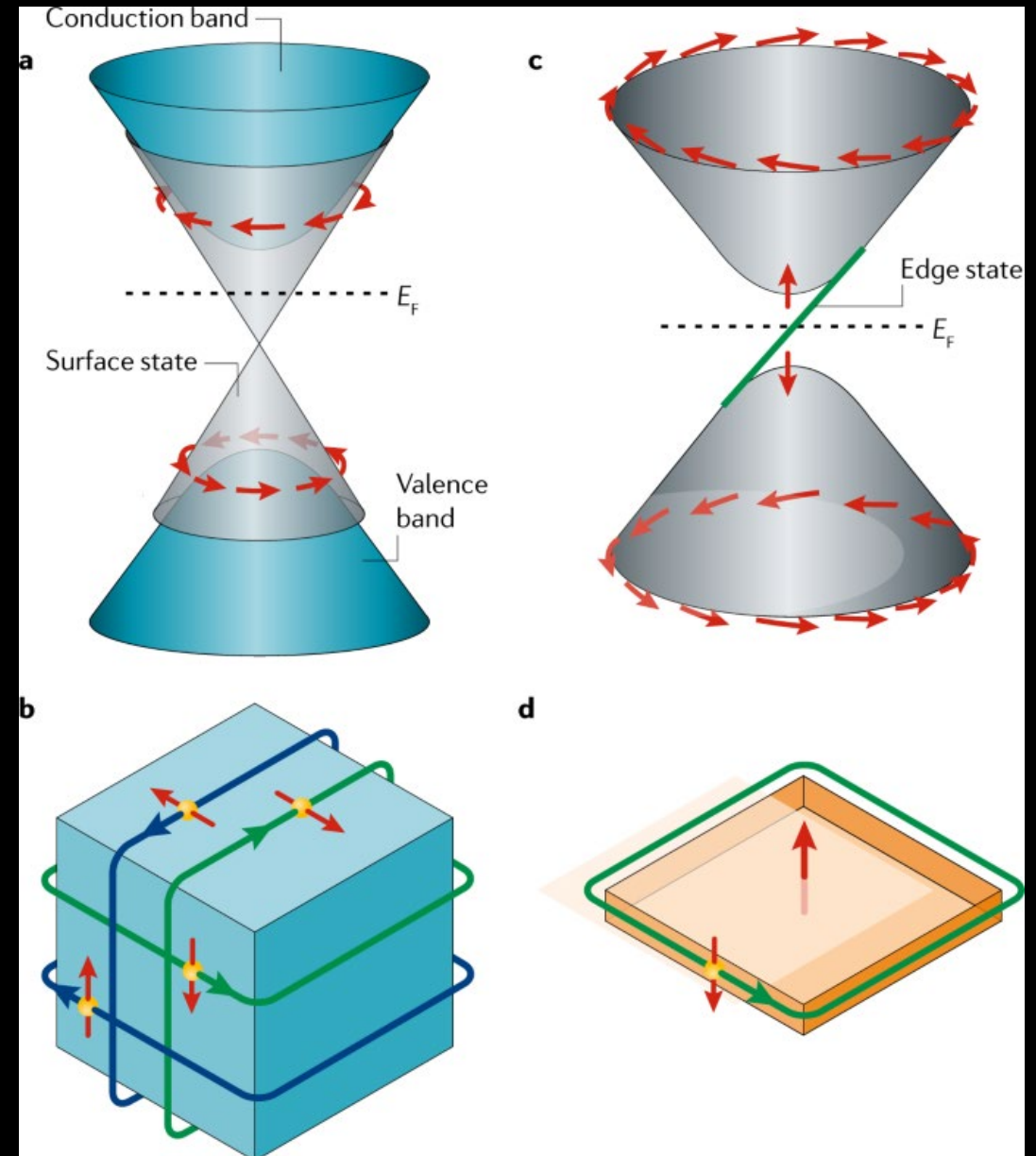
Semiconductor

Superconductor

Topological material

Some materials are expected to be boring band insulators, however, it turns out they have very unique band structure at the boundaries.

One material family for example is the topological insulators such as  $\text{Bi}_2\text{Se}_3$ , HgTe/CdTe heterostructure etc.



# Type of materials

Metal

Insulator

Semiconductor

Superconductor

Topological material

## The Nobel Prize in Physics 2016



Ill: N. Elmehed. © Nobel Media 2016

**David J. Thouless**

Prize share: 1/2



Ill: N. Elmehed. © Nobel Media 2016

**F. Duncan M. Haldane**

Prize share: 1/4



Ill: N. Elmehed. © Nobel Media 2016

**J. Michael Kosterlitz**

Prize share: 1/4

# Type of materials

Metal

Insulator

Semiconductor

Superconductor

Topological material

Another way to look at the substances is based on the symmetries. The symmetry class is from the Lei group definition and the periodic table shows their symmetry/topological invariant.

T: 0, 1 and -1, P: 0, 1 and -1, C:0

[Altland and Zirnbauer \(1996\)](#)

class	$\mathcal{C}$	$\mathcal{P}$	$\mathcal{T}$	$d = 0$	1	2	3
A				$\mathbb{Z}$		$\mathbb{Z}$	
AI			1	$\mathbb{Z}$			
AII			-1	$2\mathbb{Z}$		$\mathbb{Z}_2$	$\mathbb{Z}_2$
AIII	1				$\mathbb{Z}$		$\mathbb{Z}$
BDI	1	1	1	$\mathbb{Z}_2$	$\mathbb{Z}$		
C		-1				$2\mathbb{Z}$	
CI	1	-1	1				$2\mathbb{Z}$
CII	1	-1	-1		$2\mathbb{Z}$		$\mathbb{Z}_2$
D		1		$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$	
DIII	1	1	-1		$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$

[https://topocondmat.org/w8\\_general/classification.html](https://topocondmat.org/w8_general/classification.html)

<https://math.ucr.edu/home/baez/tenfold.html>

# Type of materials

Metal

Insulator

Semiconductor

Superconductor

Topological material

- Metal with broken time-reversal symmetry: “Unitary” class A
- Spinless time-reversal invariant superconductor: class BDI
- Spin-1/2 superconductor with no physical symmetries: Class D

[Altland and Zirnbauer \(1996\)](#)

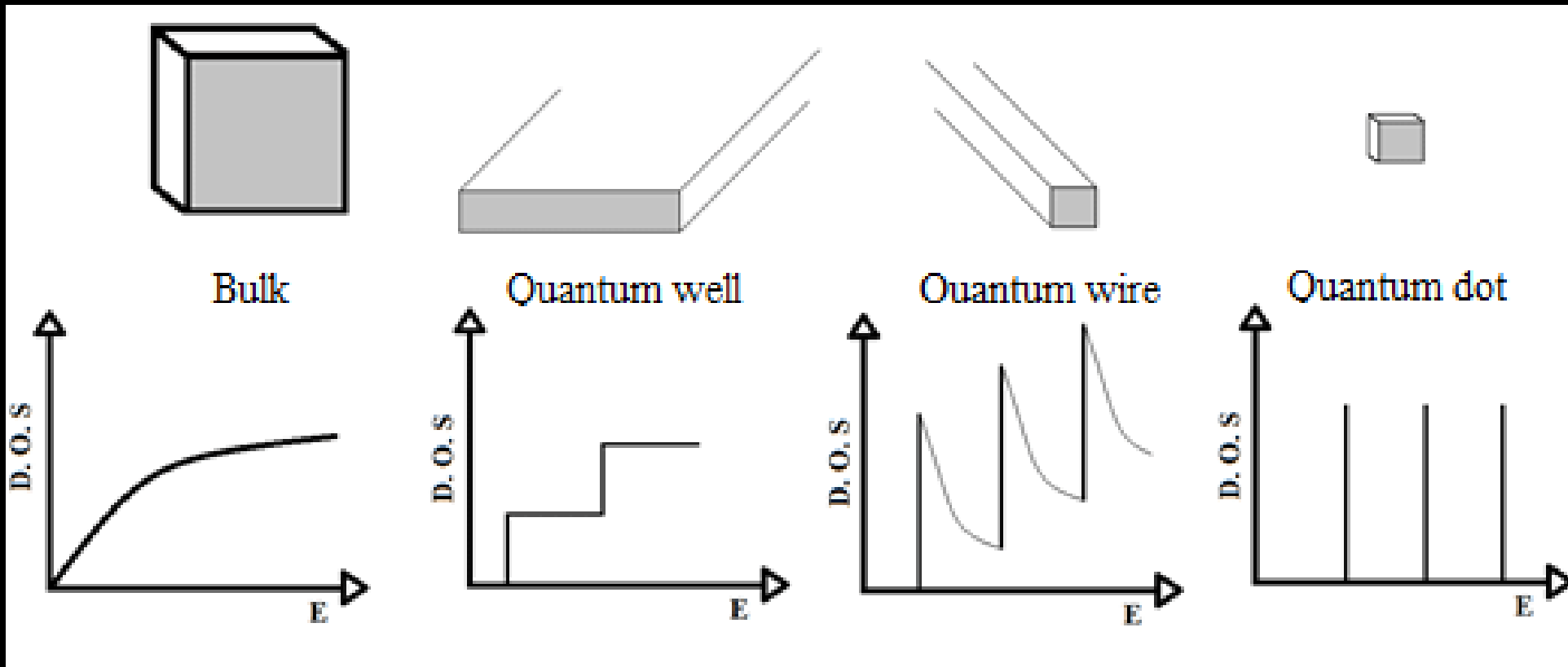
class	$\mathcal{C}$	$\mathcal{P}$	$\mathcal{T}$	$d = 0$	1	2	3
A				$\mathbb{Z}$		$\mathbb{Z}$	
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AII			-1	$2\mathbb{Z}$		$\mathbb{Z}_2$	$\mathbb{Z}_2$
AIII	1				$\mathbb{Z}$		$\mathbb{Z}$
BDI	1	1	1	$\mathbb{Z}_2$	$\mathbb{Z}$		
C		-1				$2\mathbb{Z}$	
CI	1	-1	1				$2\mathbb{Z}$
CII	1	-1	-1		$2\mathbb{Z}$		$\mathbb{Z}_2$
D		1		$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$	
DIII	1	1	-1		$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}$

[https://topocondmat.org/w8\\_general/classification.html](https://topocondmat.org/w8_general/classification.html)

<https://math.ucr.edu/home/baez/tenfold.html>

# Electron transport

## Different dimensions



# Electron transport

## Length scales

dimensions	coordinate region	spacing in $k$	Fermi region	number of electron, electron density, Fermi wave length <i><math>N</math>=Fermi region/spacing in <math>k</math>, <math>\lambda_F=2\pi/k_F</math></i>		
1	Length $L$	$2\pi/L$	$2k_F$	$N = \frac{4k_F}{2\pi/L}$	$n = \frac{N}{L} = \frac{4k_F}{2\pi}$	$\lambda_F = \frac{4}{n}$
2	Area $L^2$	$(2\pi/L)^2$	$\pi k_F^2$	$N = \frac{2\pi k_F^2}{(2\pi/L)^2}$	$n = \frac{N}{L^2} = \frac{k_F^2}{2\pi}$	$\lambda_F = \left(\frac{2\pi}{n}\right)^{1/2}$
3	Volume $L^3$	$(2\pi/L)^3$	$\frac{4}{3}\pi k_F^3$	$N = \frac{2(4\pi k_F^3/3)}{(2\pi/L)^3}$	$n = \frac{N}{L^3} = \frac{k_F^3}{3\pi^2}$	$\lambda_F = 2\left(\frac{\pi}{3n}\right)^{1/3}$

# Electron transport

## Mean Free Path

Drude model:  $J = \sigma E = \frac{ne^2\tau}{m} E$

$J = nev$   
 Drift velocity

Mean scattering time

$\tau = \frac{mv}{eE} = \frac{m\mu}{e}$   
 Electron mobility

$l_e = v_F \tau = \frac{\hbar k_F}{m} \frac{m\mu}{e} = \frac{\hbar\mu}{e} k_F$

Dimension	Fermi wavelength	Mean free path
1	$\lambda_F = \frac{4}{n}$	$l_e = \frac{\hbar\mu n\pi}{e 2}$
2	$\lambda_F = \left(\frac{2\pi}{n}\right)^{1/2}$	$l_e = \frac{\hbar\mu}{e} \sqrt{2\pi n}$
3	$\lambda_F = 2 \left(\frac{\pi}{3n}\right)^{1/3}$	$l_e = \frac{\hbar\mu}{e} (3n)^{1/3} \pi^{2/3}$

# Electron transport

## Diffusion coefficient

Diffusive current flow:  $J = -D \nabla n$  (due to the density gradient),  $D$  is the diffusion constant

Einstein relation  
(Brownian motion):

$$D = \frac{\mu k_B T}{e}$$

$$\sigma = \frac{ne^2 \tau}{m} = ne\mu \Rightarrow \mu = \frac{e\tau}{m}$$

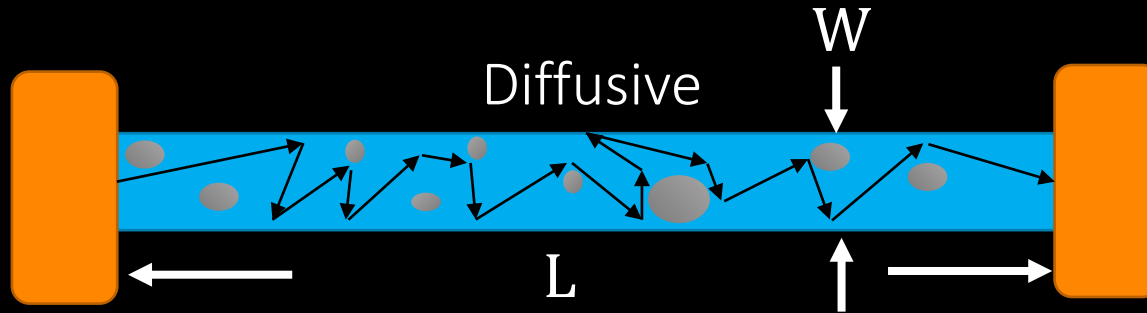
$$l_e = v_F \tau$$

Dimension	Equipartition theorem	Diffusion constant
1	$\frac{1}{2} m v_F^2 = \frac{1}{2} k_B T$	$D = \frac{l_e v_F}{d}, d = 1, 2, 3$
2	$\frac{1}{2} m v_F^2 = k_B T$	
3	$\frac{1}{2} m v_F^2 = \frac{3}{2} k_B T$	

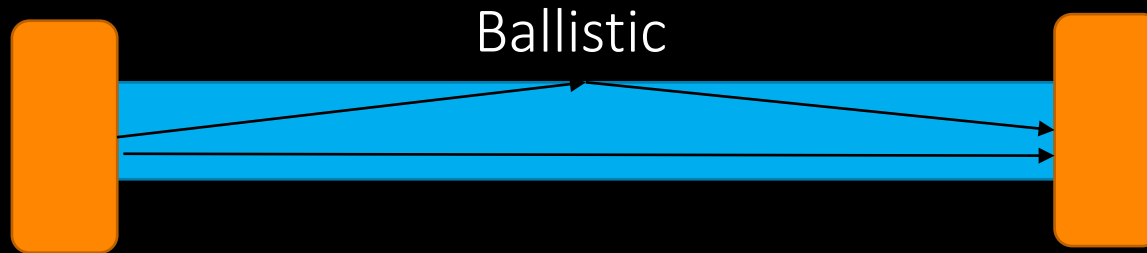
# Electron transport

Diffusion vs. Ballistic  $l_e = v_F \tau$

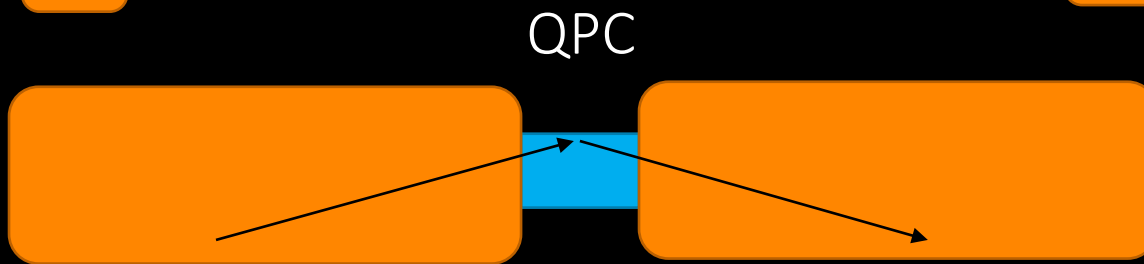
$l_e \ll W$  and  $L$



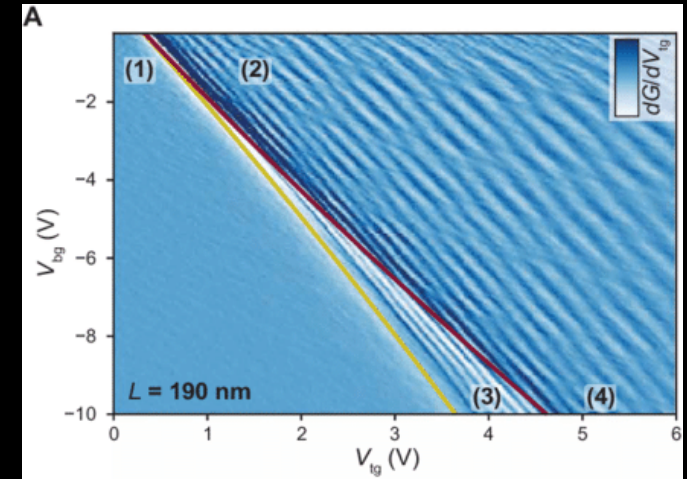
$l_e > W$  and  $L$



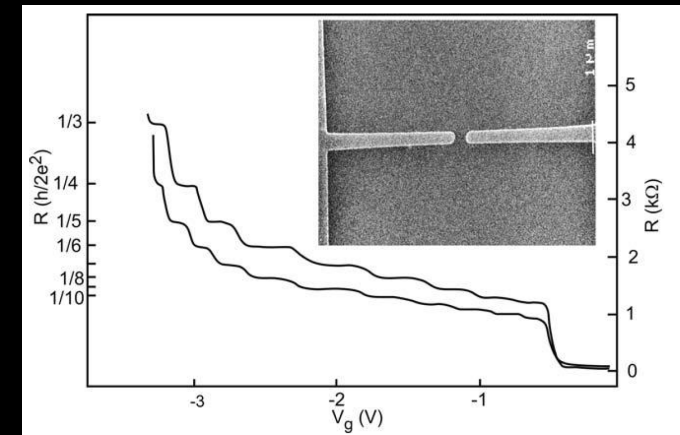
$l_e \gg W$  and  $L$



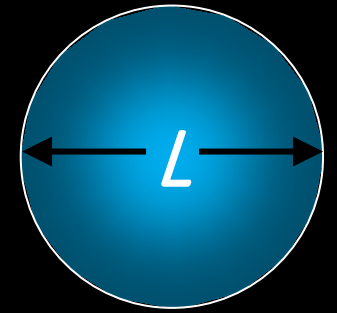
## Fabry-Perot oscillations



Peter Rickhaus et al. Science Advances (2020)

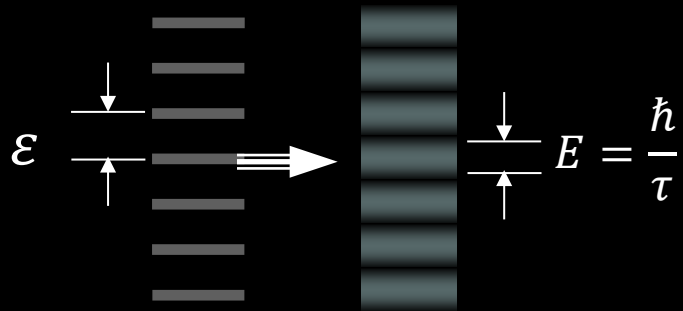


# Electron transport



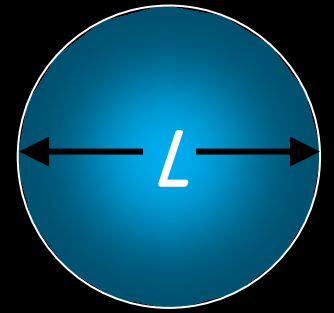
## Thouless Energy: $E_{Th}$

Here, one can consider a diffusive system with size  $L$ , the quantum levels have a spacing of  $\varepsilon = 1/N(\varepsilon_F) \cdot L^d$ .



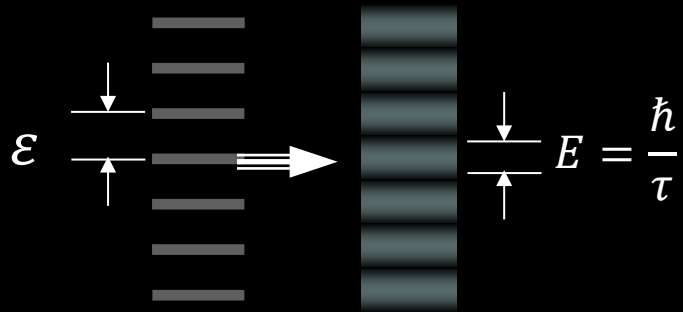
In the diffusive system, another characteristic energy scale is the Thouless energy  $E_{Th} = \frac{\hbar D}{L^2}$ , it can be considered as the traveling time (depending on the diffusion time) through the system.

# Electron transport



## Thouless Energy: $E_{Th}$

Here, one can consider a diffusive system with size  $L$ , the quantum levels have a spacing of  $\varepsilon = 1/N(\varepsilon_F) \cdot L^d$ .



In the diffusive system, another characteristic energy scale is the Thouless energy  $E_{Th} = \frac{\hbar D}{L^2}$ , it can be considered as the traveling time (depending on the diffusion time) through the system.

Conductance (Einstein relation)  $G = \sigma L^{d-2} = \frac{e^2 N(\varepsilon_F) L^d D}{L^2} = \sigma_0 g(L)$  where  $\sigma_0 = \frac{e^2}{\hbar}$   
 and  $g(L) = \frac{\hbar D / L^2}{1/N(\varepsilon_F) L^d} = \frac{E_{Th}}{\varepsilon}$  (dimensionless Thouless conductance)

$g(L) < 1$  ( $R > \frac{\hbar}{e^2}$ )  $\Rightarrow$  localized state

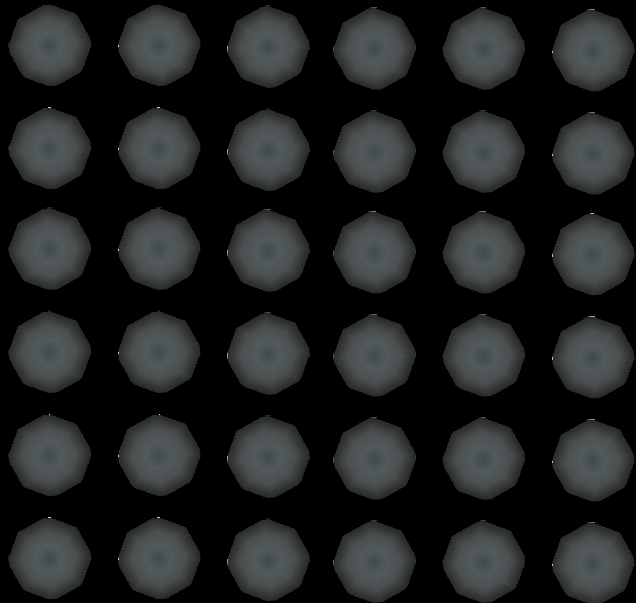
$g(L) > 1$  ( $R < \frac{\hbar}{e^2}$ )  $\Rightarrow$  extended state

# Electron transport

## Anderson localization

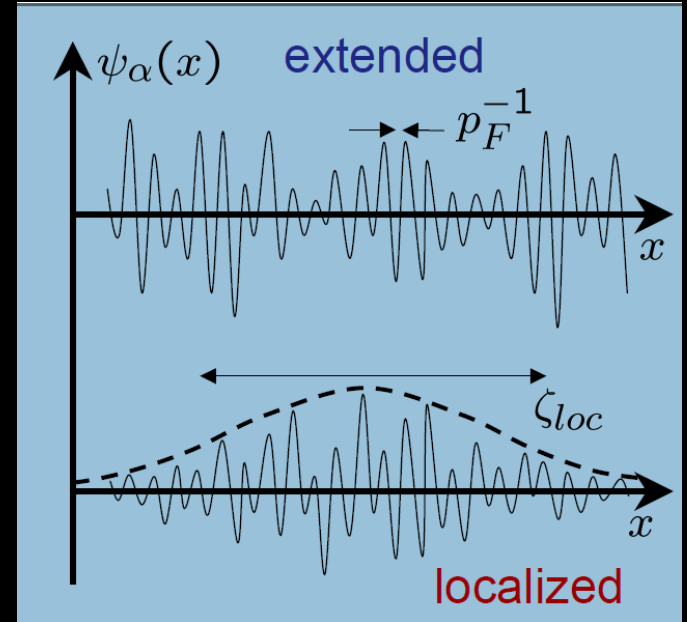
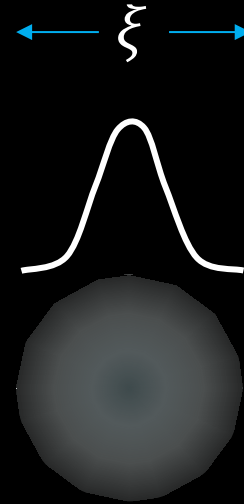
$$g(L) < 1 \Rightarrow \text{localized state} \quad G \propto e^{-L/\xi}$$
$$g(L) > 1 \Rightarrow \text{extended state} \quad G \propto L^{d-2}$$

## Anderson model



Lattice is considered with the Tight binding  
Random on-site energy on the lattice  
Only the nearest-neighbor hopping.

As the result, there will be a critical value,  $I_c$   
 $I < I_c$  (localized, insulator)  
 $I > I_c$  (extended, metal)



Boris Altshuler lecture

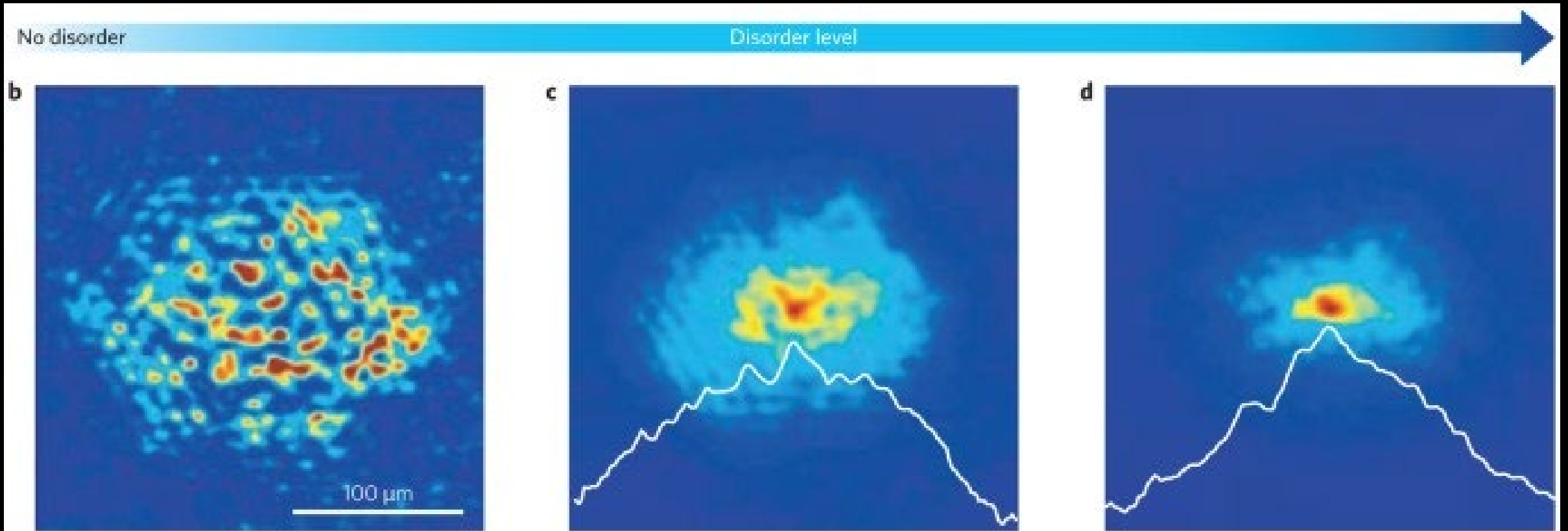
# Electron transport

## Anderson localization

Ballistic

diffusive

localization



# Electron transport

## Anderson localization

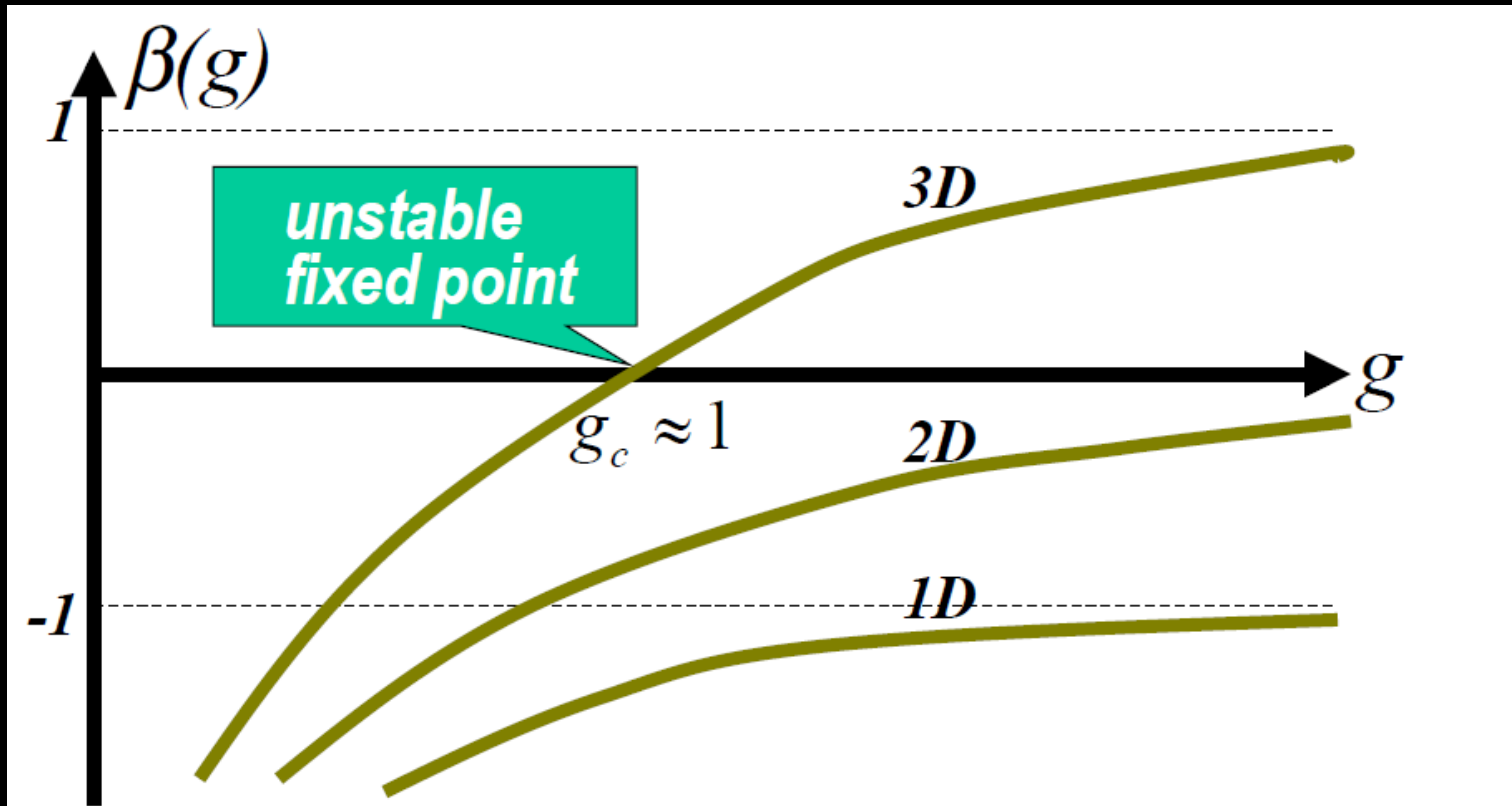
Scaling theory of localization, dimensionless  $g$  is function of  $L$

$$\frac{d \log(g)}{d \log(L)} = \beta(g)$$



It's universal and material independent. It only matters with global symmetry.

Metal-insulator transition in 3D case but all states in 2D and 1D are localized.

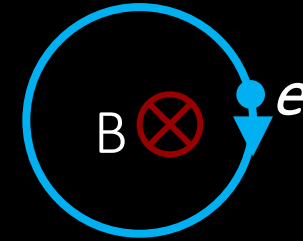


# Electron transport

In a magnetic field

Magnetic length:

Cyclotron motion



Cyclotron frequency

$$F = evB = mr_c\omega_c^2$$

Cyclotron radius

$$r_c\omega_c = v_F \longrightarrow r_c = \frac{v_F}{\omega_c} = \frac{mv_F}{eB} = \frac{\hbar k_F}{eB}$$

$l_B =$  magnetic length

flux quantization

$$B \cdot \pi r_c^2 = n\Phi_0 = \frac{nh}{e} \longrightarrow r_c = \sqrt{\frac{2n\hbar}{eB}} \equiv \sqrt{2n} l_B$$

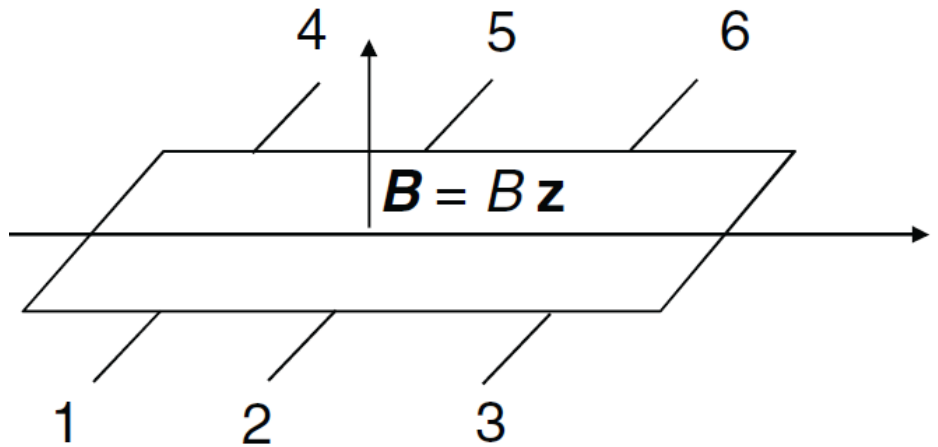
$$2\pi l_B^2 \cdot B = \Phi_0$$

$$B = \frac{\hbar^2 k_F^2}{2ne\hbar} = \frac{mE_F}{ne\hbar}$$

$\longrightarrow$  Quantizing magnetic field

# Electron transport

## Quantum Hall effect



Use the following conditions:

$$\begin{aligned}\rho_{xx} &= \rho_{yy} \\ \rho_{yx} &= -\rho_{xy} = B/|q|n_{2d} \\ V_x &= E_x L, V_H = E_y w\end{aligned}$$

$$\frac{m\mathbf{v}_d}{\tau} = q[\mathbf{E} + \mathbf{v}_d \times \mathbf{B}].$$

$$I \begin{pmatrix} E_x \\ E_y \end{pmatrix} = \begin{pmatrix} m/q^2 n_{2d} \tau & -m\mu B/q^2 n_{2d} \tau \\ m\mu B/q^2 n_{2d} \tau & m/q^2 n_{2d} \tau \end{pmatrix} \begin{pmatrix} J_x \\ J_y \end{pmatrix}$$

One can obtain:

$$n_{2d} = \frac{I/|q|}{dV_H/dB}, \quad \text{Carrier density}$$

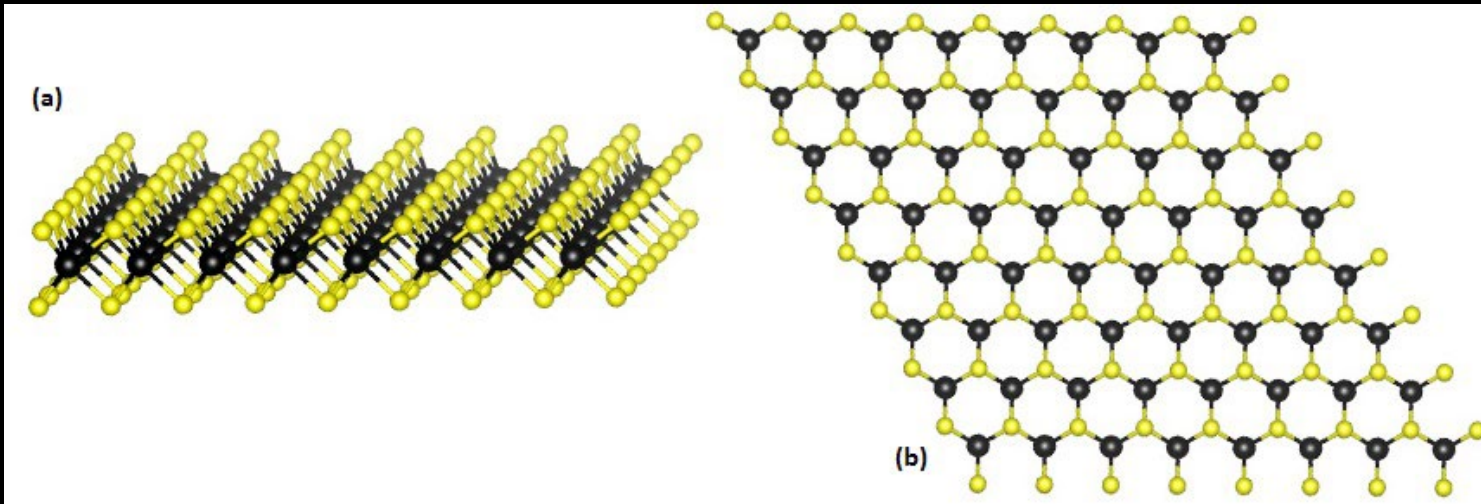
$$\mu = \frac{I/|q|}{n_{2d} V_x w/L}. \quad \text{Mobility}$$

# Electron transport

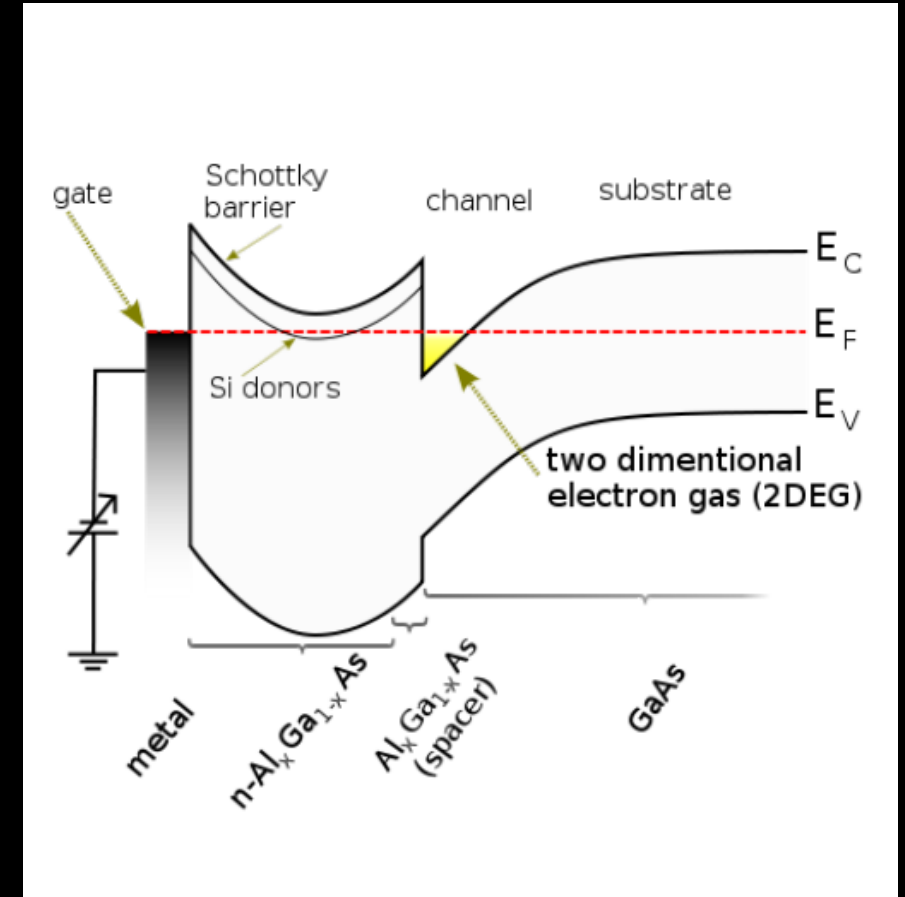
## 2D electron gas

In a quantum well type structure, the potential well confines electrons/holes in a 2D plane. Charges only allow moving in the X-Y plane

Another type is real 2d material such as graphene or transition metal dichalcogenide



wiki



# Electron transport

## Quantum Hall effect

Developing high mobility samples has a long history, GaAs quantum wells.

It took almost three decades to boost the mobility from 10k to 10 M  $\text{cm}^2/\text{V}\cdot\text{s}$  along with this development amazing physics was discovered.



Photo from the Nobel Foundation archive.  
Klaus von Klitzing



Photo from the Nobel Foundation archive.  
Robert B. Laughlin



Photo from the Nobel Foundation archive.  
Horst L. Störmer

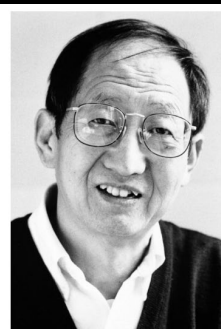
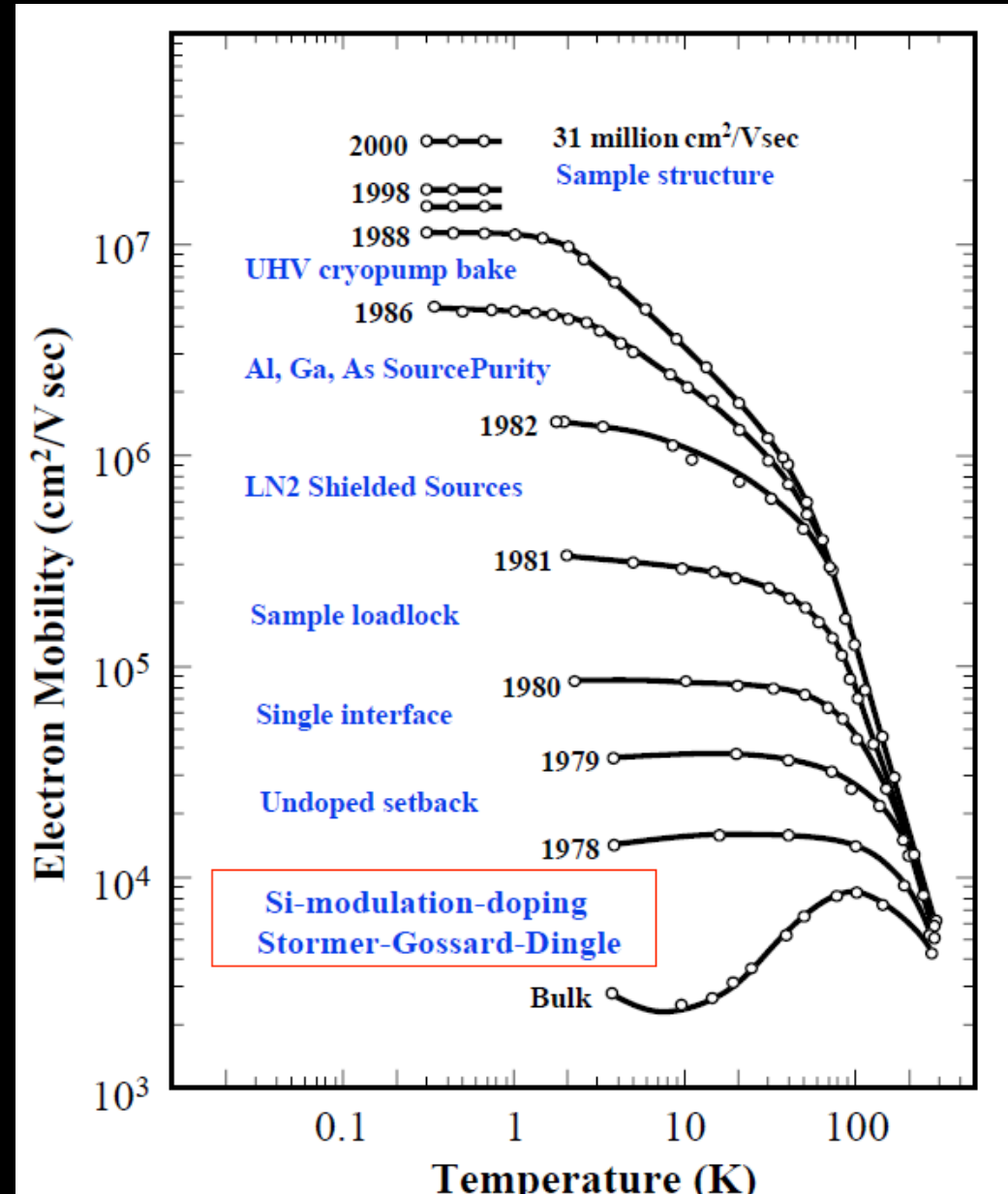


Photo from the Nobel Foundation archive.  
Daniel C. Tsui

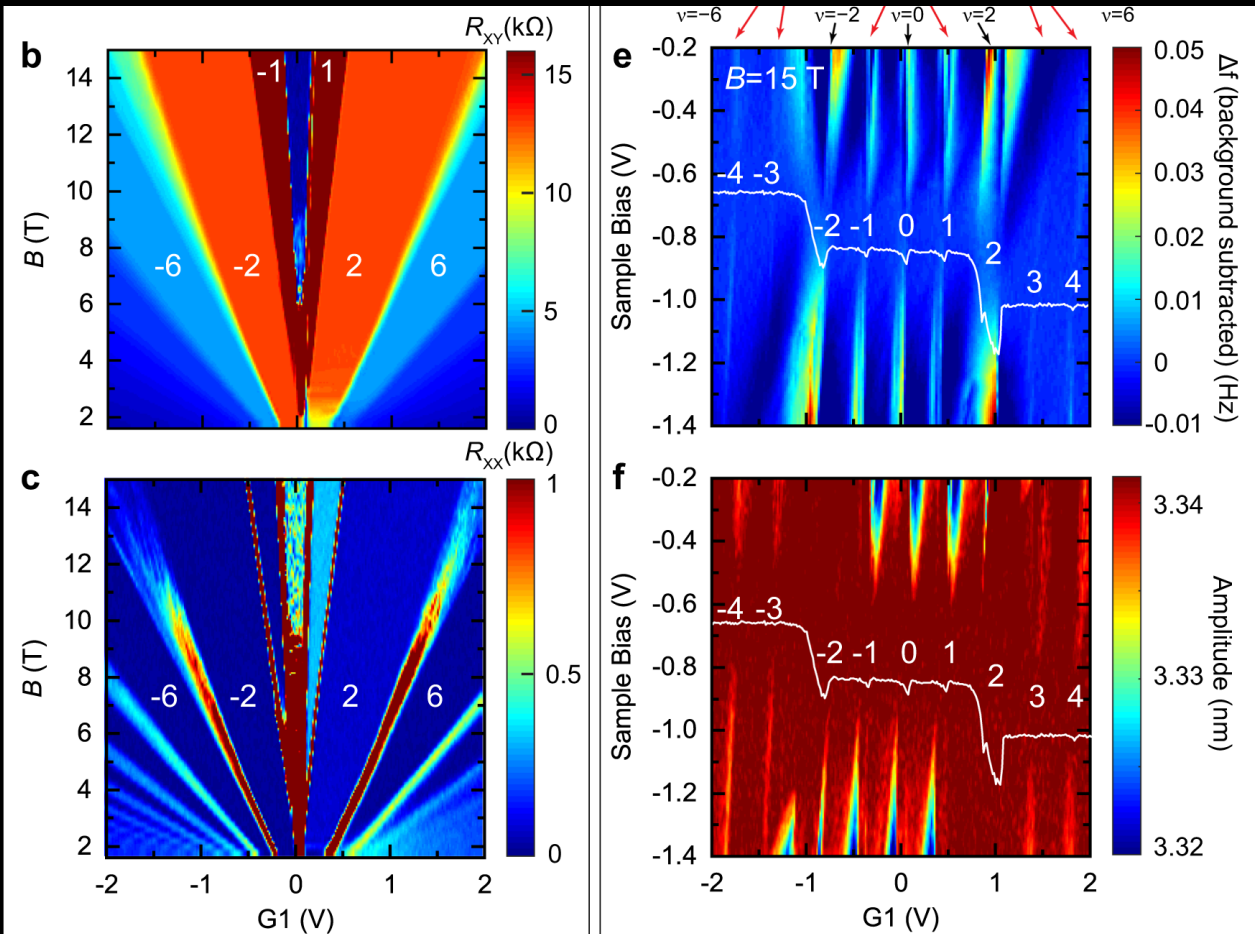
Quantum Hall effect,  
Nobel prize 1985

Fractional quantum Hall effect,  
Nobel prize 1998



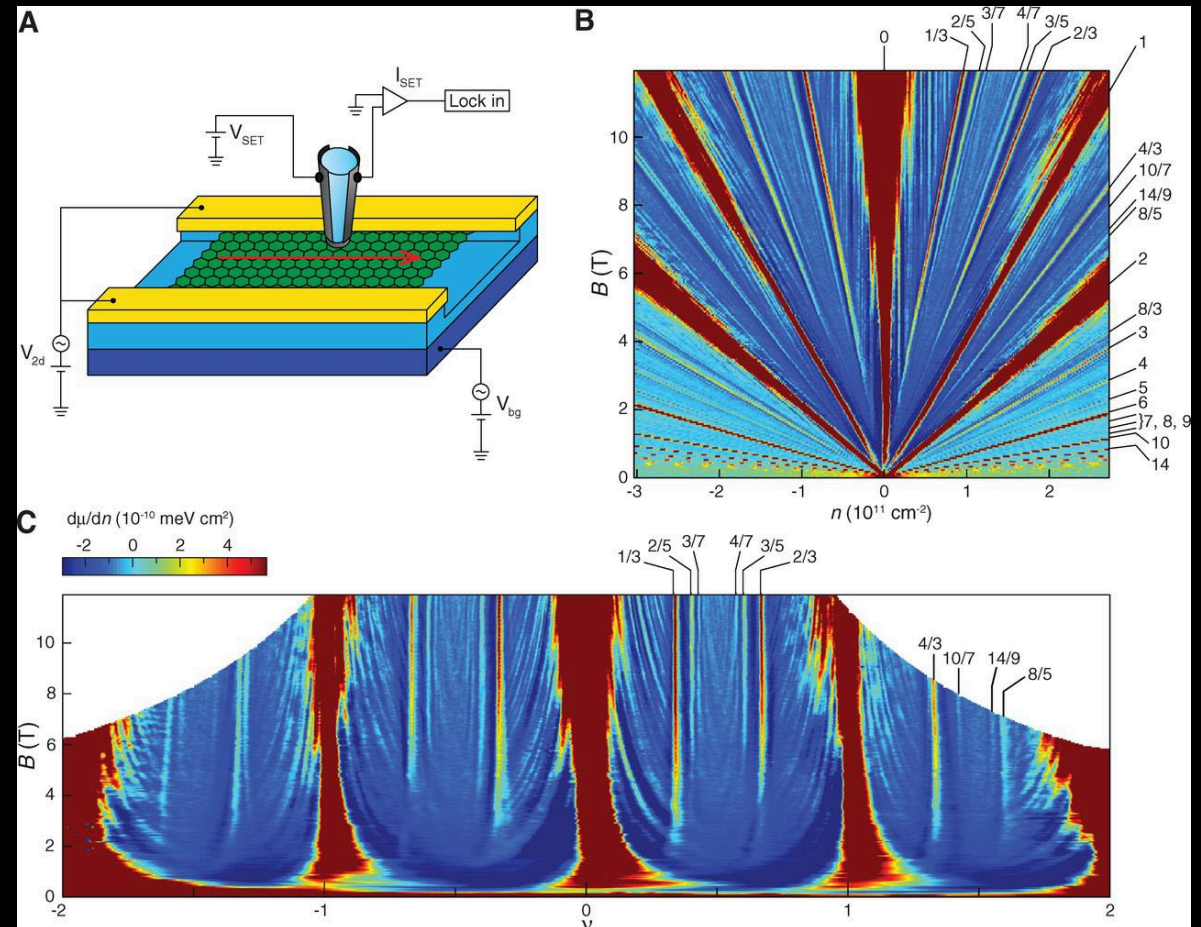
# Electron transport

## Quantum Hall effect



Kim et al. Nat. Commun. (2021)

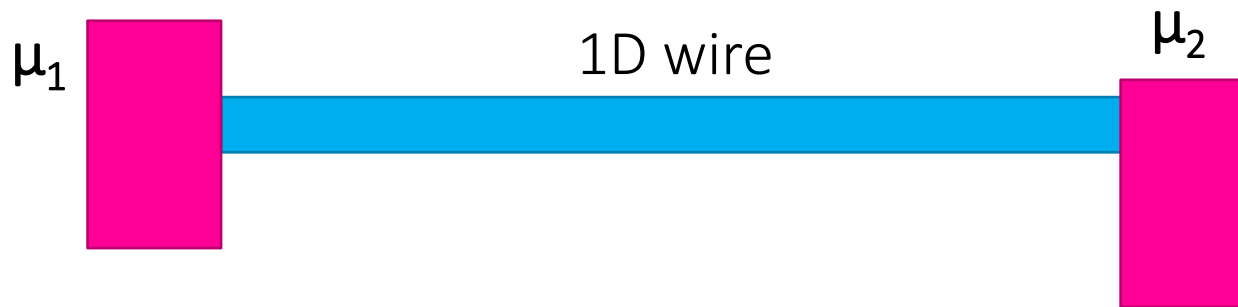
## Fractional quantum Hall effect



Yacoby's group Science (2012)

# Electron transport

## Quantum wire(1D)



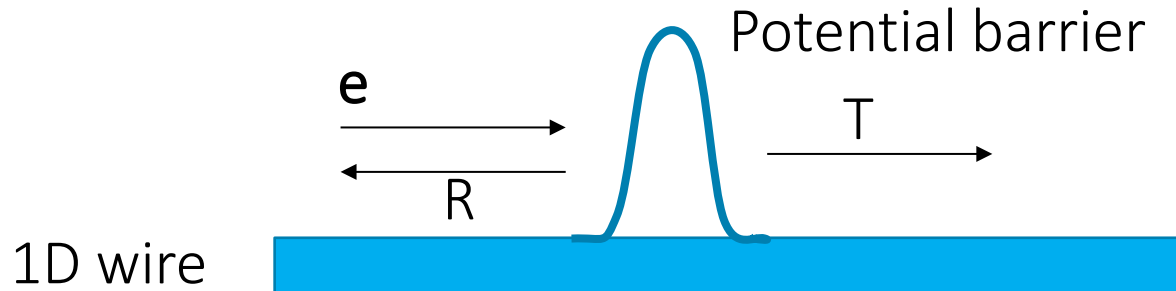
$$I = \int_{\mu_1}^{\mu_2} \underset{\substack{\text{velocity} \\ \nearrow}}{ev(E)} \left( \underset{\substack{\text{spin} \\ \nearrow}}{2} \frac{\underset{\substack{\text{1D density} \\ \nearrow}}{1}}{2} g_{1D}(E) \right) dE = \int_{\mu_1}^{\mu_2} ev(E) \left( \frac{2}{hv(E)} \right) dE \quad \longrightarrow \quad G = I/V = \frac{2e^2}{h}$$
$$= \frac{2e}{h}(\mu_2 - \mu_1) = \frac{2e}{h}(eV)$$

Conductance is a fixed value regardless of the length of the wire.

# Electron transport

## Quantum wire(1D)

$$G = I/V = \frac{2e^2}{h}$$



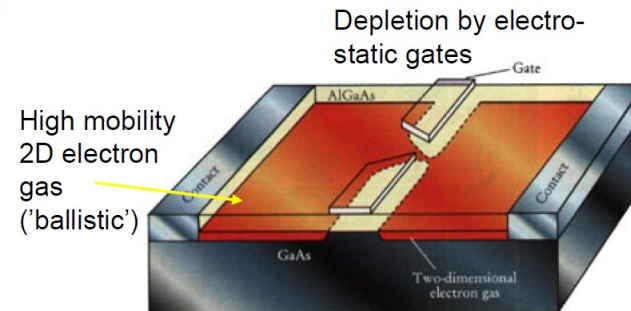
Now become

Landauer formula

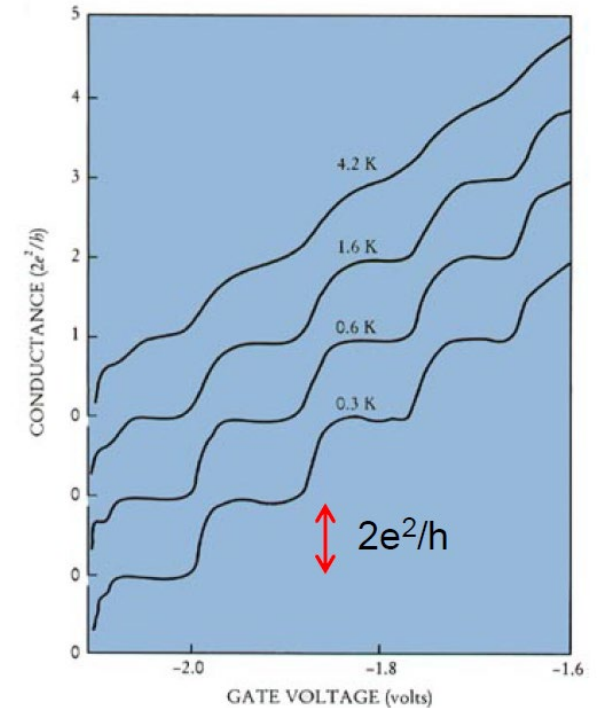
$$G = \frac{2e^2}{h} T \quad (\text{transmission probability } T)$$

With more channels (sub-bands)

$$G(E_F) = \frac{2e^2}{h} \sum_n T_n(E_F) \quad (T = 0)$$



'Quantum Point Contact'

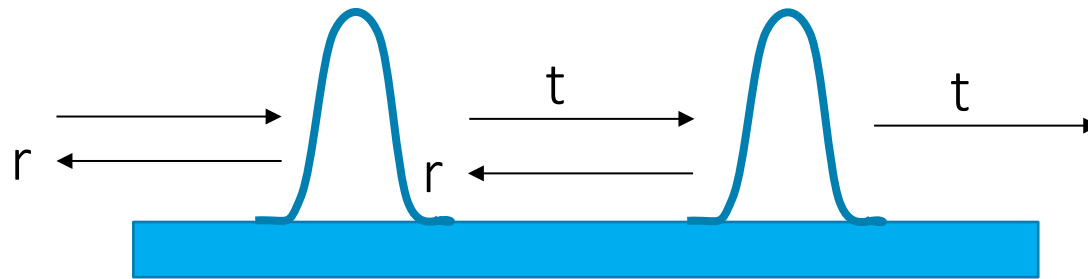


Also good to review Landauer–Buttiker formalism

# Electron transport

## Quantum dot (0D system)

1D wire with two identical barriers under a **coherent transport**



$$t = |t|e^{i\phi_t}$$
$$r = |r|e^{i\phi_r}$$

Total transmission:

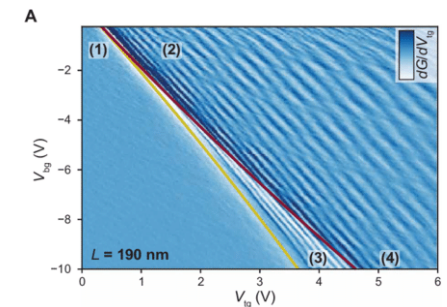
$$T_{\text{total}} = \frac{|t|^4}{1 + |r|^4 - 2|r|^2 \cos(\phi)}, \quad \phi = 2kL + \phi_{r1} + \phi_{r2}$$

For the resonant transmission (round trip with a phase of  $2\pi n$ ):

$$\text{For } \phi = 2\pi n: \quad T_{\text{total}} = \frac{|t|^4}{(1 - |r|^2)^2} = \frac{T^2}{(1 - R)^2} = \frac{T^2}{T^2} = 1$$

Resulting in a total transmission even  $T = |t|^2 < 1$  for individual barriers

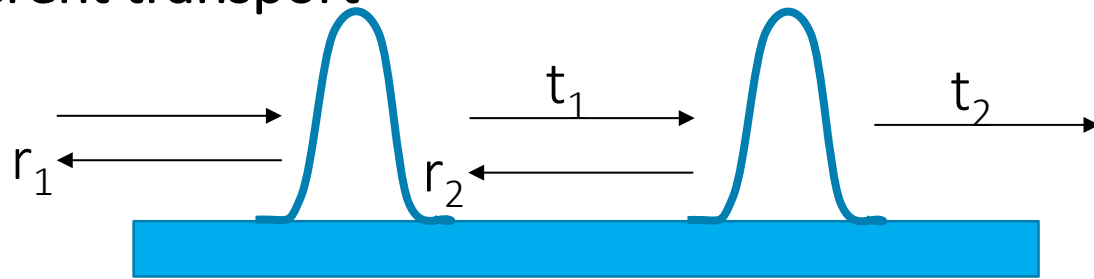
Resonance condition:  
 $kL = \pi n$



# Electron transport

## Quantum dot (0D system)

### Incoherent transport



Total transmission:

$$T_{\text{total}} = \frac{|t_1|^2 |t_2|^2}{1 - |r_1|^2 |r_2|^2}$$

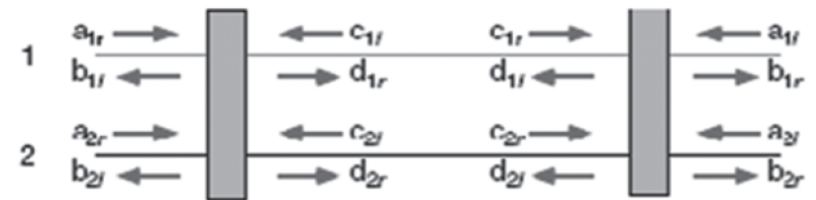
The resistance is like resistors in series:

$$\text{Resistance} = \frac{h}{2e^2} \left( 1 + \frac{|r_1|^2}{|t_1|^2} + \frac{|r_2|^2}{|t_2|^2} \right)$$

Jesper Nygård  
Lecture note

### Scattering matrix:

$$\mathbf{b} = \tilde{S} \cdot \mathbf{a}, \quad \begin{pmatrix} b_1 \\ b_2 \end{pmatrix} = \begin{pmatrix} r & t' \\ t & r' \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \end{pmatrix}$$



$$S_T = S_L \otimes S_N \otimes S_R$$

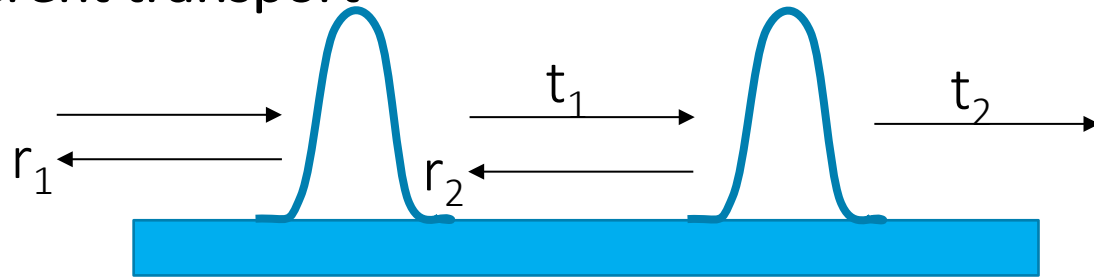
$$\begin{pmatrix} d_{1r} \\ d_{2r} \\ b_{1l} \\ b_{2l} \end{pmatrix} = S_L \begin{pmatrix} a_{1r} \\ a_{2r} \\ c_{1l} \\ c_{2l} \end{pmatrix}, \quad \begin{pmatrix} c_{1r} \\ c_{2r} \\ c_{1l} \\ c_{2l} \end{pmatrix} = S_N \begin{pmatrix} d_{1r} \\ d_{2r} \\ d_{1l} \\ d_{2l} \end{pmatrix}, \quad \begin{pmatrix} b_{1r} \\ b_{2r} \\ d_{1l} \\ d_{2l} \end{pmatrix} = S_R \begin{pmatrix} c_{1r} \\ c_{2r} \\ a_{1l} \\ a_{2l} \end{pmatrix}$$

$$\begin{pmatrix} b_{1r} \\ b_{2r} \\ b_{1l} \\ b_{2l} \end{pmatrix} = S_T \begin{pmatrix} a_{1r} \\ a_{2r} \\ a_{1l} \\ a_{2l} \end{pmatrix} = \begin{pmatrix} t_{1r,1r} & t_{1r,2r} & r_{1r,1l} & r_{1r,2l} \\ t_{2r,1r} & t_{2r,2r} & r_{2r,1l} & r_{2r,2l} \\ r_{1l,1r} & r_{1l,2r} & t_{1l,1l} & t_{1l,2l} \\ r_{2l,1r} & r_{2l,2r} & t_{2l,1l} & t_{2l,2l} \end{pmatrix} \begin{pmatrix} a_{1r} \\ a_{2r} \\ a_{1l} \\ a_{2l} \end{pmatrix}$$

# Electron transport

## Quantum dot (0D system)

### Incoherent transport



Total transmission:

$$T_{\text{total}} = \frac{|t_1|^2 |t_2|^2}{1 - |r_1|^2 |r_2|^2}$$

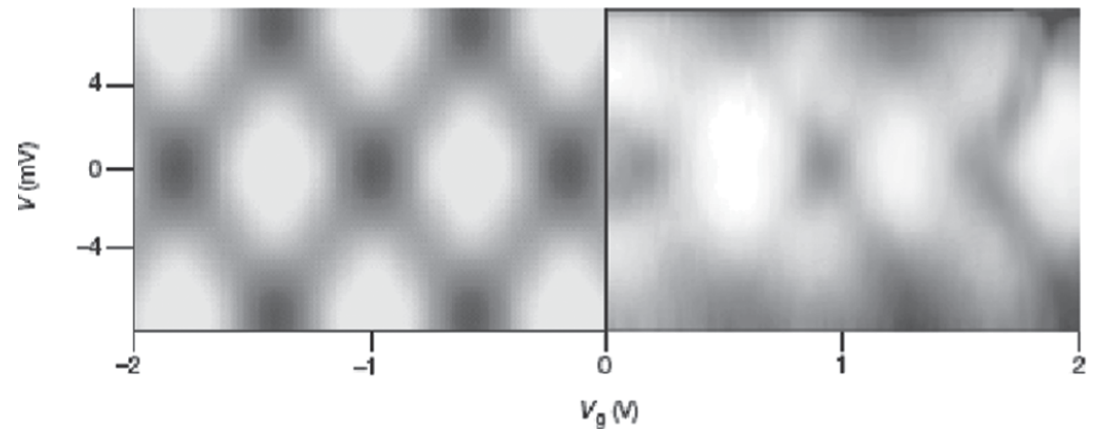
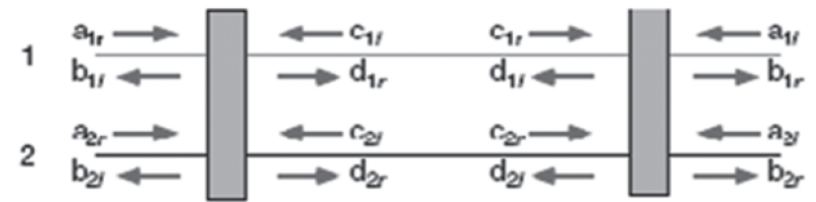
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$$\text{Resistance} = \frac{h}{2e^2} \left( 1 + \frac{|r_1|^2}{|t_1|^2} + \frac{|r_2|^2}{|t_2|^2} \right)$$

Jesper Nygård  
Lecture note

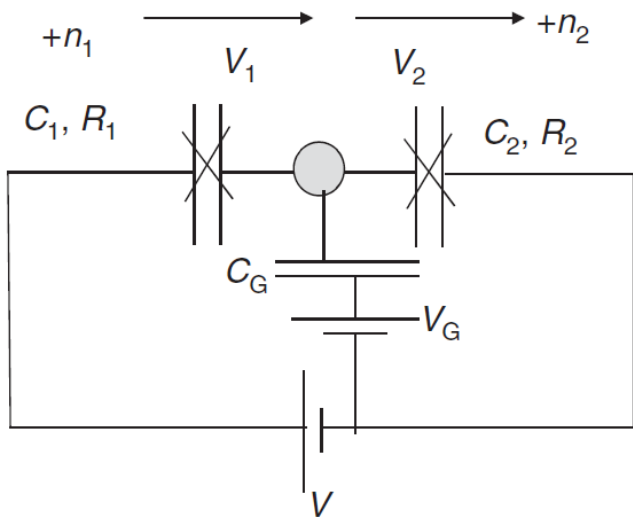
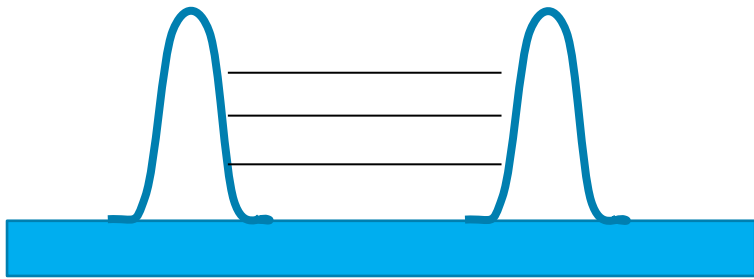
### Scattering matrix:

$$\mathbf{b} = \tilde{S} \cdot \mathbf{a}, \quad \begin{pmatrix} b_1 \\ b_2 \end{pmatrix} = \begin{pmatrix} r & t' \\ t & r' \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \end{pmatrix}$$



# Electron transport

## Quantum dot (single electron transition)



The total charge on the island

$$Q = Q_2 - Q_1 - Q_G \quad \text{Where, } Q_G = C_G(V_G - V_2)$$

The voltage drop on each junctions (barriers)

$$V_1 = \frac{1}{C_{\text{tot}}} ((C_G + C_2)V_{\text{DS}} - C_G V_G + ne),$$

$$V_2 = \frac{1}{C_{\text{tot}}} (C_1 V_{\text{DS}} + C_G V_G - ne).$$

Total energy for adding e from left

$$\Delta E_{\text{tot}} = \frac{e}{C_{\text{tot}}} \left( \frac{e}{2} + (en + (C_2 + C_G)V_{\text{DS}} - C_G V_G) \right)$$

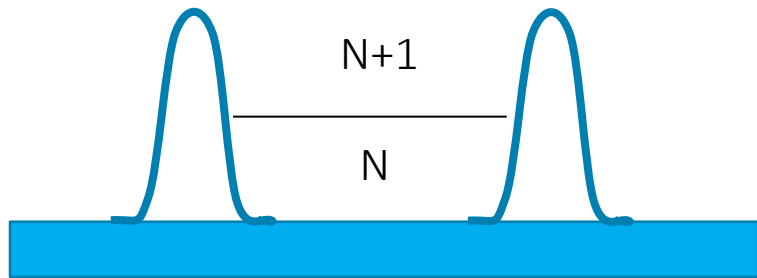
The conditions for tunneling one electron

$$\mp [en + (C_G + C_2)V_{\text{DS}} - C_G V_G] > \frac{e}{2} \quad \text{or}$$

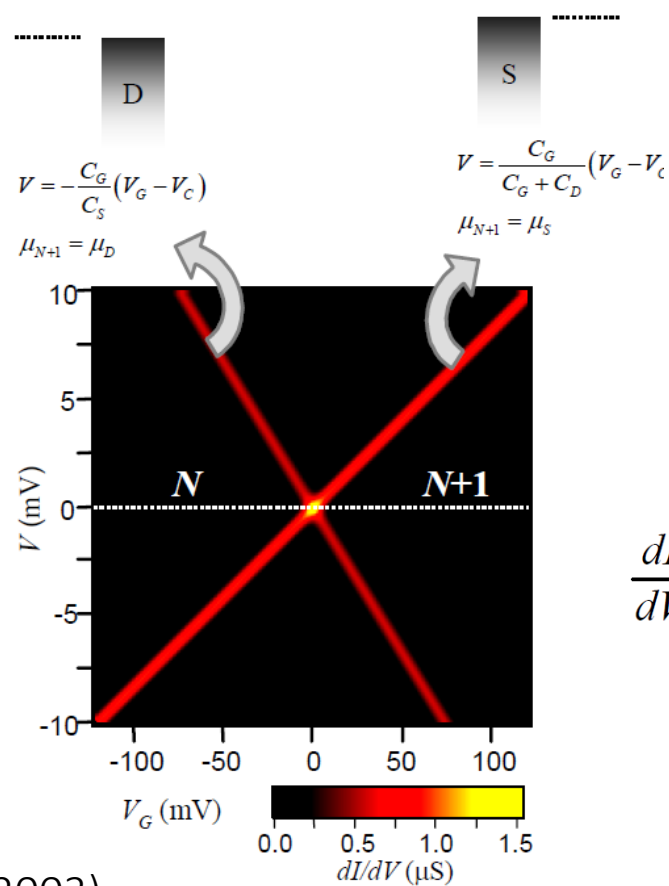
$$\pm [en - C_1 V_{\text{DS}} - C_G V_G] > \frac{e}{2}.$$

# Electron transport

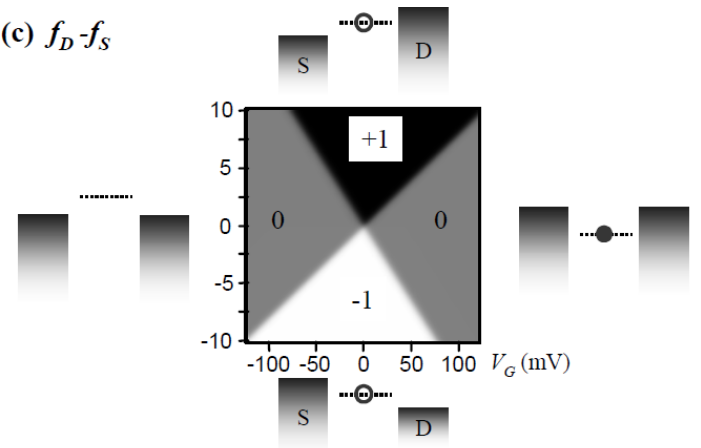
## Quantum dot (single electron transition)



The conditions create the charge stability diagram. If we only consider a one-level system.



(c)  $f_D \cdot f_S$



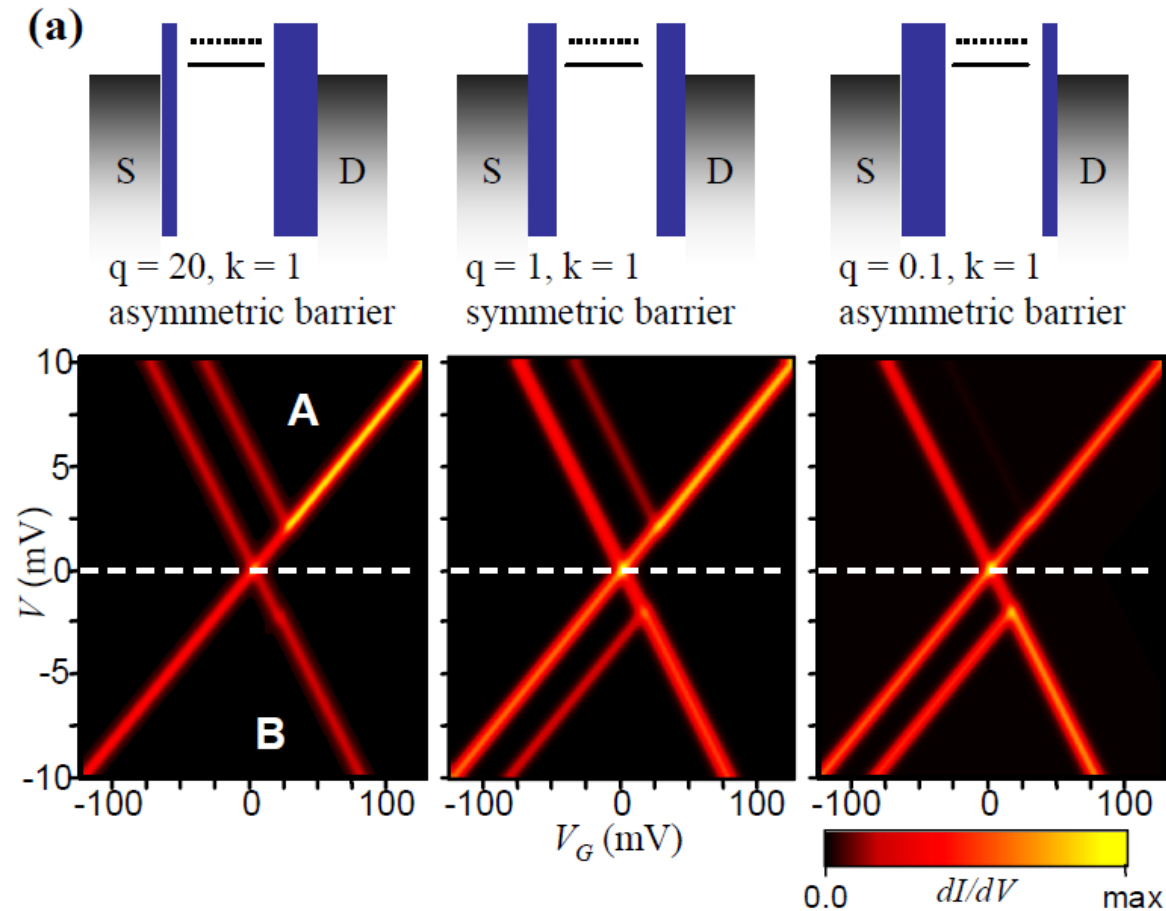
$$\frac{dI}{dV} = \frac{e^2 \Gamma}{k_B T} \left( (1 - f_D) f_D \frac{C_S}{C_{total}} + (1 - f_S) f_S \frac{C_D + C_G}{C_{total}} \right)$$

$$f_D = \left( 1 + \exp\left(\frac{\mu_{N+1} - \mu_D}{k_B T}\right) \right)^{-1} = \left( 1 + \exp\left(\frac{\mu_{N+1}}{k_B T}\right) \right)^{-1}$$

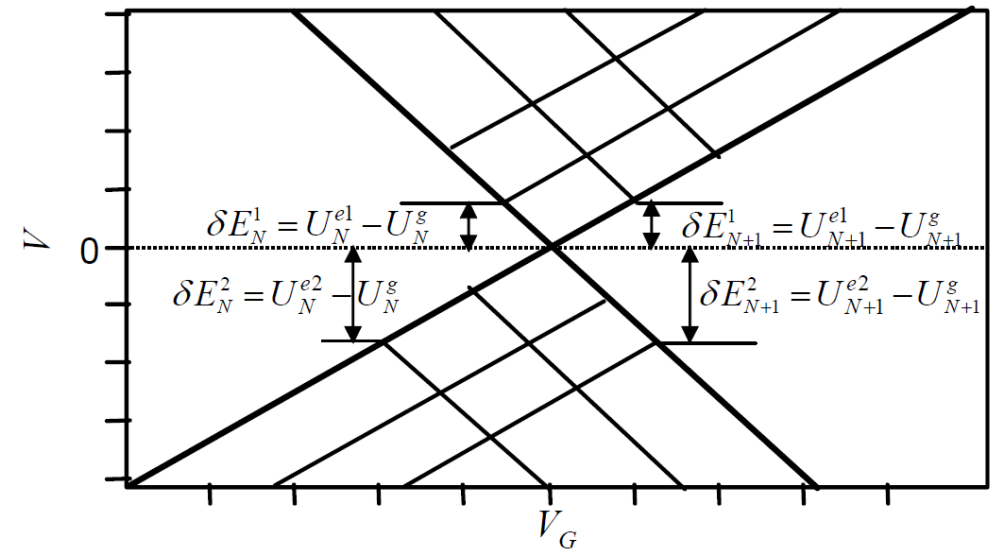
$$f_S = \left( 1 + \exp\left(\frac{\mu_{N+1} - \mu_S}{k_B T}\right) \right)^{-1} = \left( 1 + \exp\left(\frac{\mu_{N+1} + |e|V}{k_B T}\right) \right)^{-1}$$

# Electron transport

Quantum dot (single electron transition)



Multi-levels quantum dot

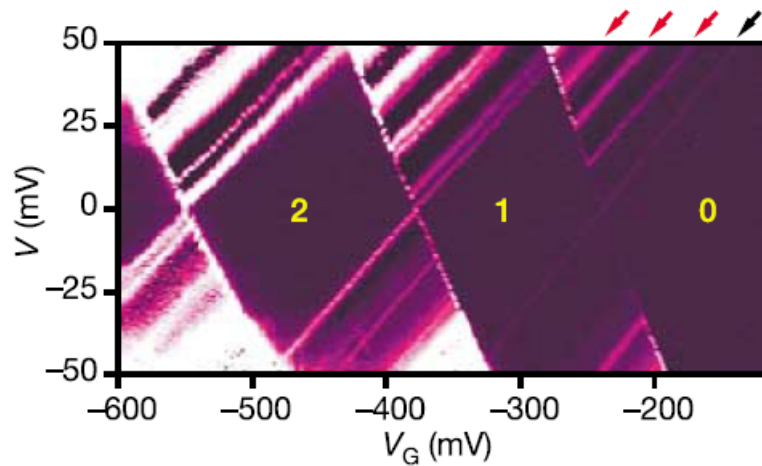
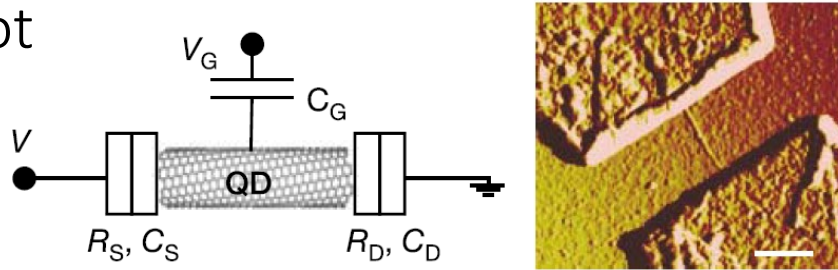


Jiwoong Park Ph.D. thesis (2003)

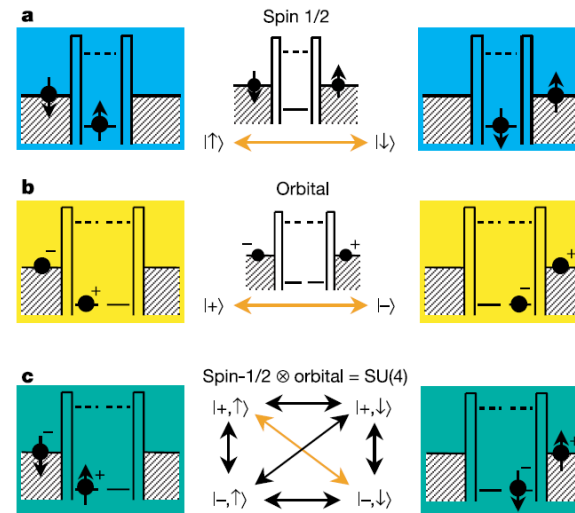
# Electron transport

## Quantum dot (single electron transition)

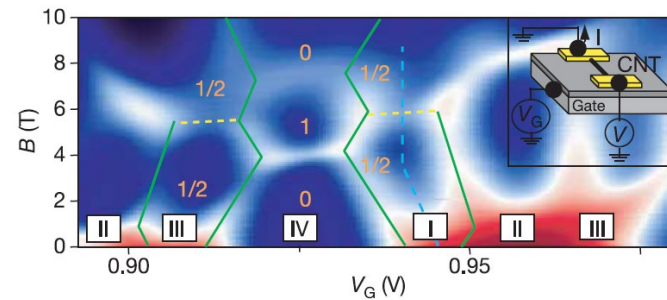
Carbon nanotube quantum dot



P. Jarillo-Herrero et al. Nature (2004)



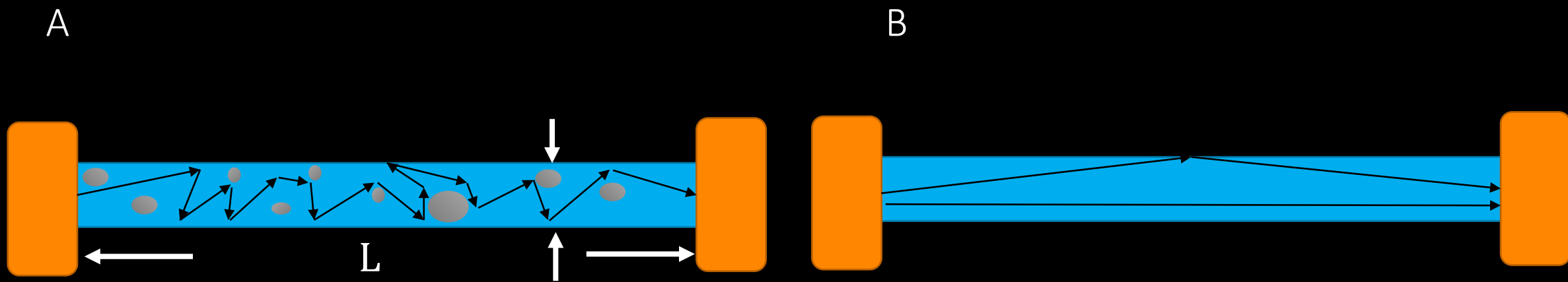
Spin related cotunneling process: Kondo effect



P. Jarillo-Herrero et al. Nature (2005)

# Quiz

1. Which is diffusive and which is ballistic



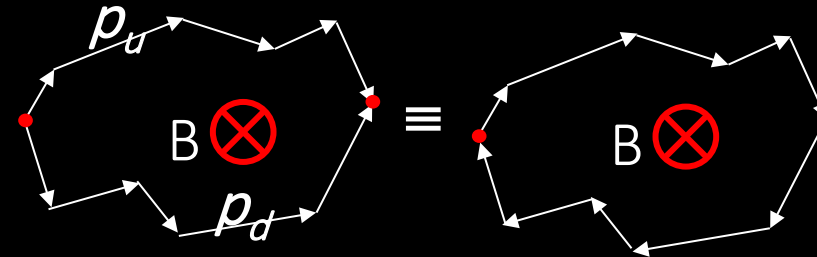
# Electron transport(extra)

## Quantum phase under a field

In a field  $B = \nabla \times A$  Canonical momentum  
 $p = mv - eA$

Magnetic field: break the time reversal symmetry

electrons pick a phase  $\phi$  when traveling along with a path P



phase difference between two paths with the same ends

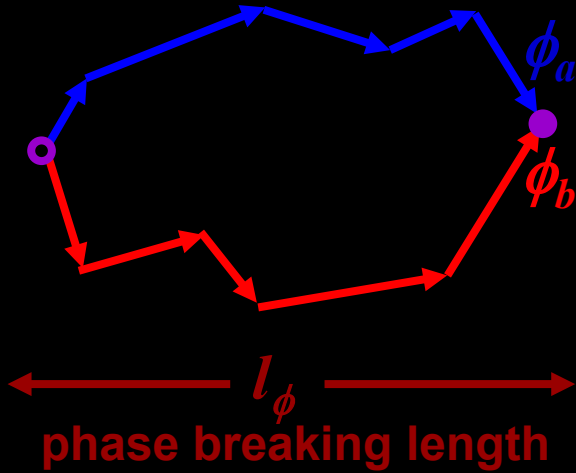
$$\delta\phi = \frac{1}{\hbar} \int_P^Q p_u \cdot dl_1 - \frac{1}{\hbar} \int_P^Q p_d \cdot dl_2 = \frac{1}{\hbar} \int_P^Q p_u \cdot dl_1 + \frac{1}{\hbar} \int_Q^P p_d \cdot dl_2 = \frac{1}{\hbar} \oint p \cdot dl$$

$$= \frac{e}{\hbar} \int (\nabla \times A) \cdot dS = \frac{e}{\hbar} \int B dS = 2\pi \frac{B \cdot S}{h/e}$$

acquired phase around a loop

# Electron transport(extra)

## Phase Coherence Length



Phase-breaking :

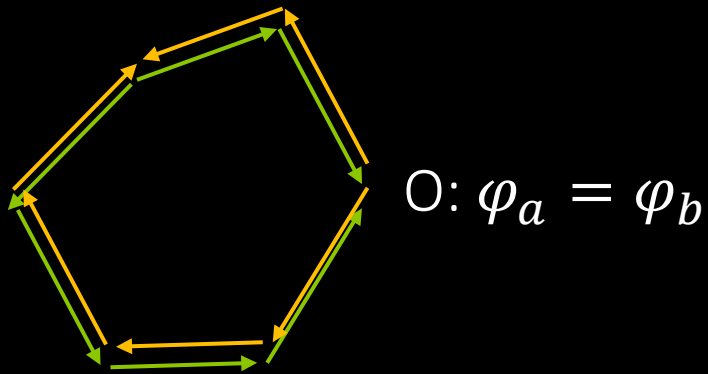
Collisions between electrons, electron-phonon scattering  
Collisions with impurities that have an internal degree of freedom

$$L_\varphi = V_F \tau_\varphi \quad L_\varphi = \sqrt{D \tau_\varphi}$$

Dimension	Note: (1) Dimensionality in terms of $l_\phi$ (2) $l_\phi > l$ Localization correction $\delta\sigma$ to the Drude conductivity
1	$\delta\sigma_{1D} = -\frac{e^2 L_\varphi}{\pi \hbar}$
2	$\delta\sigma_{2D} = -\frac{e^2}{2\pi^2 \hbar} \ln \frac{L_\varphi}{l}$
3	$\delta\sigma_{3D} = -\frac{e^2}{2\pi^2 \hbar} \left[ \frac{1}{l} - \frac{1}{L_\varphi} \right]$

# Electron transport(extra)

Weak localization (disorder system)



$$W_{a \rightarrow b} = \left| \sum_i A_i \right|^2 = \sum_i |A_i|^2 + \sum_{i \neq j} A_i A_j^*$$

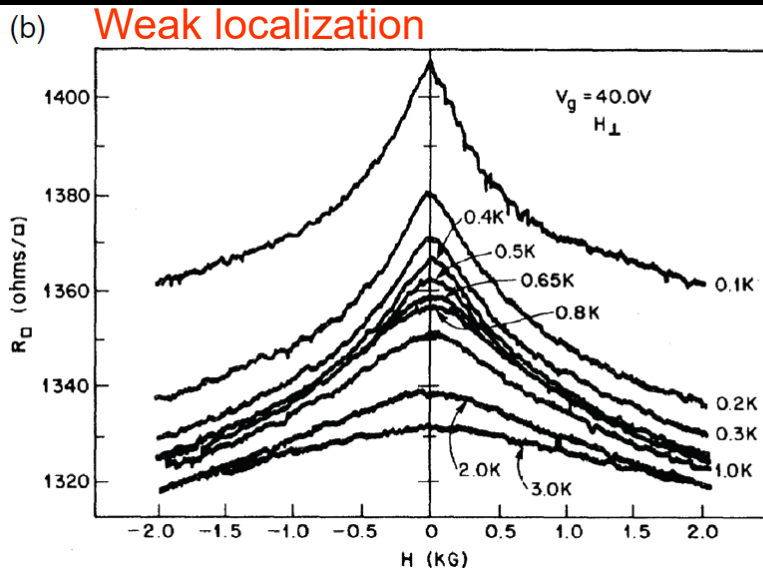
Classical diffusion
Quantum interference

In zero field,  $B=0$ ,  $A_+ = A_- = A$

Probability for back-scattering:

$$W_{0 \leftrightarrow 0} = |A_+ + A_-|^2 = 4|A|^2$$

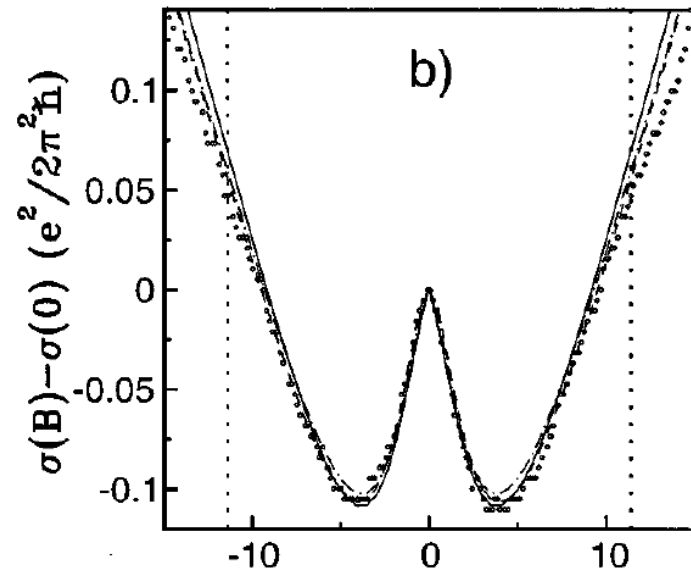
The probability of returning to the same position becomes higher. This means lower conductance thus higher resistance.



# Electron transport(extra)

## Weak anti-localization

A disordered system is under the influence of spin-orbit interaction which diminishes the localization due to spin processes. Now, the conductance is enhanced instead lower. Under a certain scenario, the conductance correction:



W. Knap et al. PRB (1996)

Only cubic term

$$\Delta\sigma(B) - \Delta\sigma(0) = \frac{e^2}{2\pi^2\hbar} \left\{ \Psi\left(\frac{1}{2} + \frac{H_\varphi}{B} + \frac{H_{SO}}{B}\right) + \frac{1}{2}\Psi\left(\frac{1}{2} + \frac{H_\varphi}{B} + 2\frac{H_{SO}}{B}\right) - \frac{1}{2}\Psi\left(\frac{1}{2} + \frac{H_\varphi}{B}\right) - \ln\frac{H_\varphi + H_{SO}}{B} - \frac{1}{2}\ln\frac{H_\varphi + 2H_{SO}}{B} + \frac{1}{2}\ln\frac{H_\varphi}{B} \right\}.$$

Only linear term

$$\Delta\sigma(B) - \Delta\sigma(0) = \frac{e^2}{2\pi^2\hbar} \left\{ \Psi\left(\frac{1}{2} + \frac{H_\varphi}{B}\right) - \ln\frac{H_\varphi}{B} \right\}$$

This allows us to study the spin-orbit effect of the system.

# Nanofabrication

How to manipulate materials

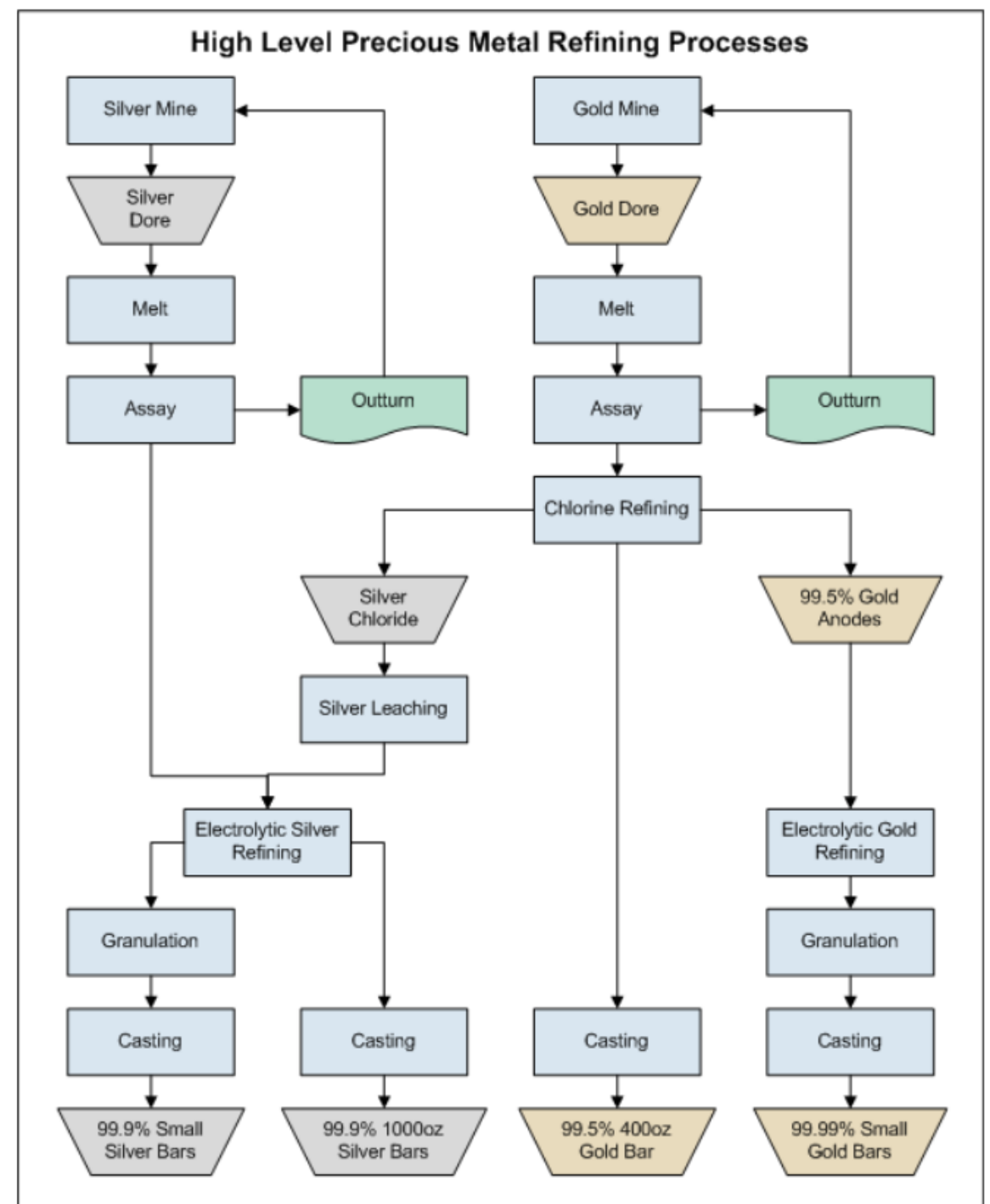
# Nanofabrication

How to make materials?

To be honest, it is very complicated!!

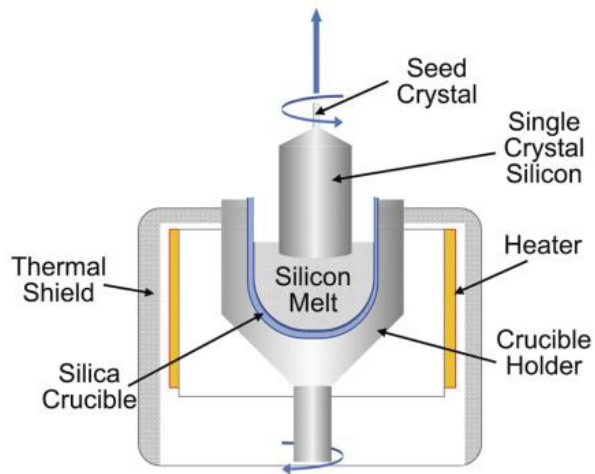
These are examples of two materials (Au and Ag) coming from mining. For other materials, there are a lot of different processes for various metals.

Adapted from Quora



# Nanofabrication

For semiconductors, Si is the most common one.

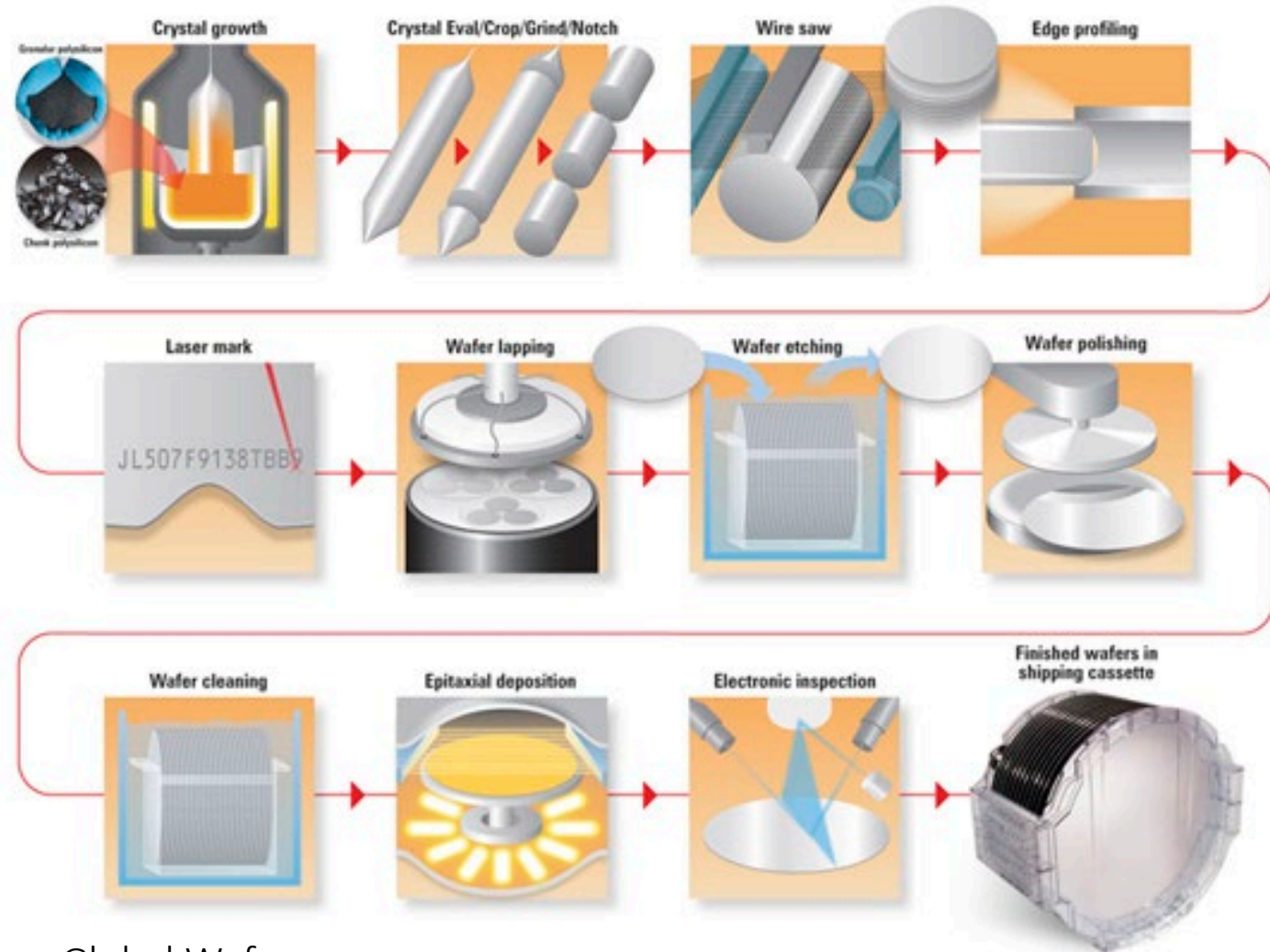


(a)

(b)

<https://www.mksinst.com/n/silicon-wafer-production>

MKS, (PVA TePla AG 2017)



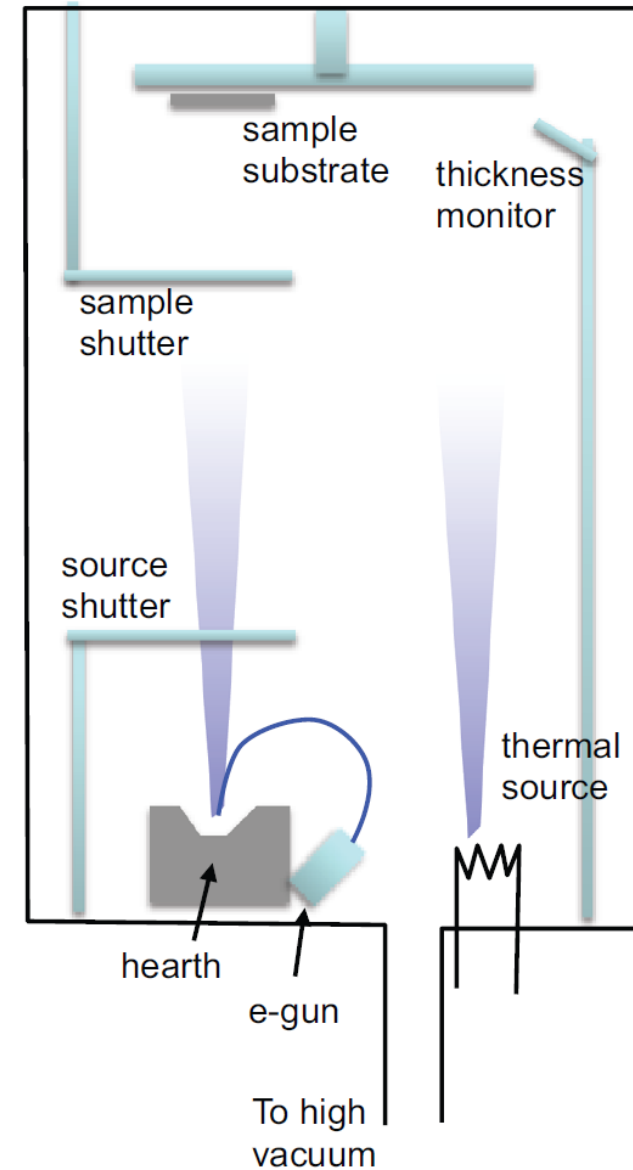
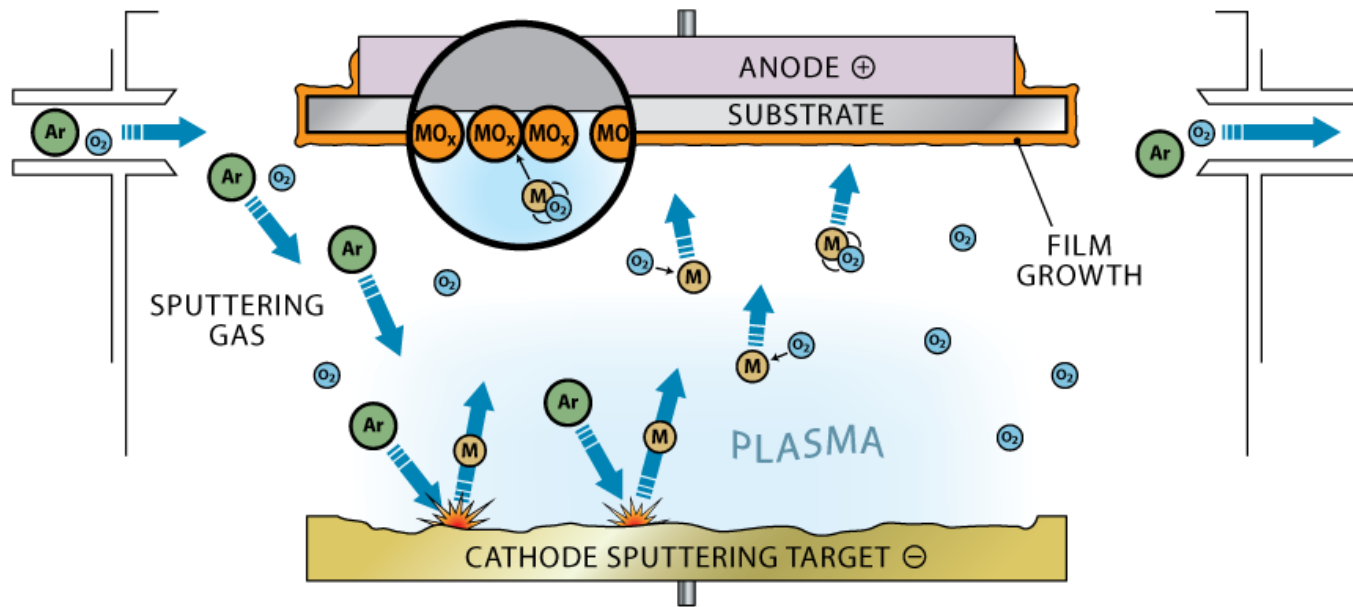
Global Wafers

# Nanofabrication

## Evaporation

### Physical Vapor Deposition

#### Sputtering

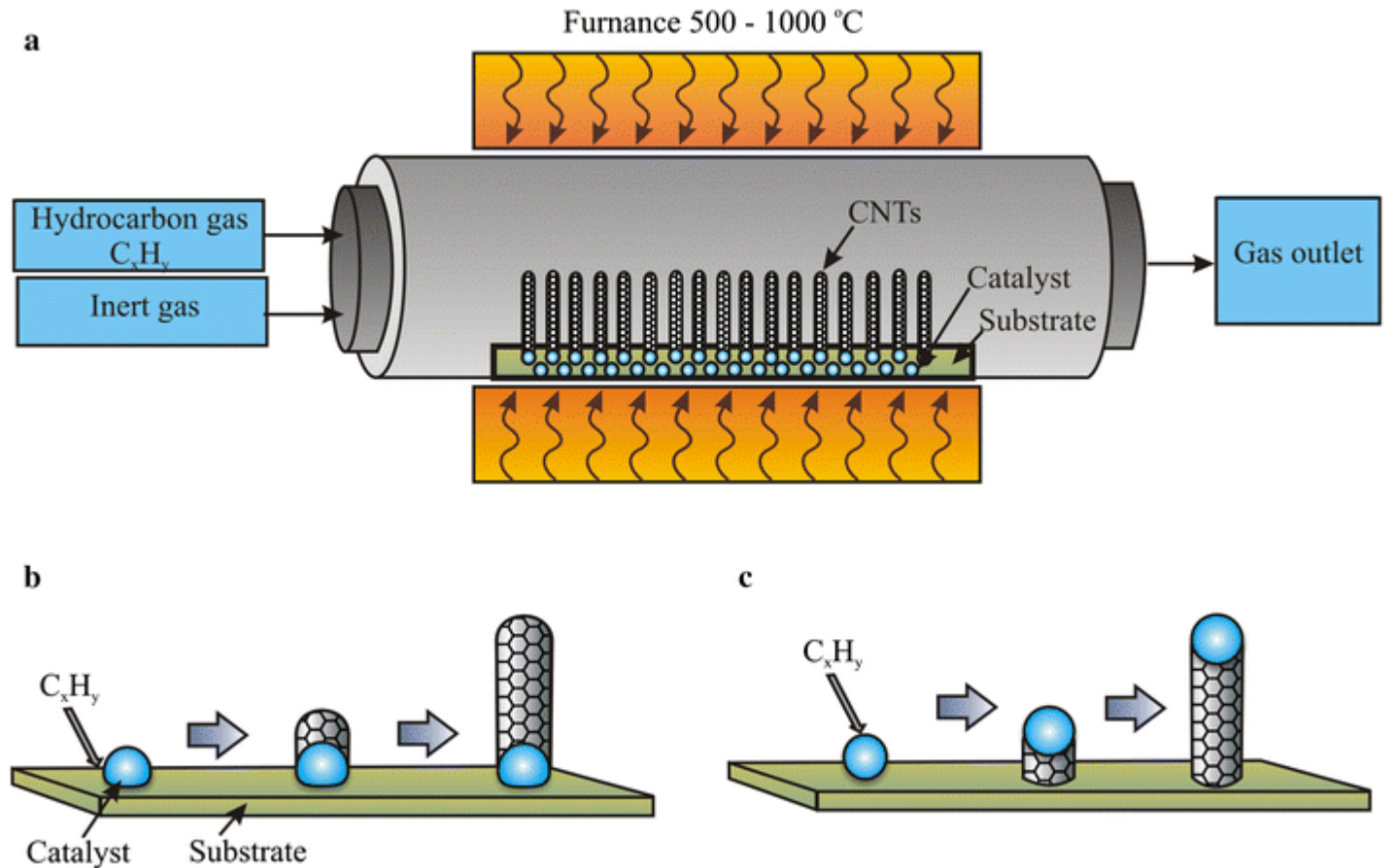


# Nanofabrication

## Chemical Vapor Deposition

Unlike the previous PVD, here we utilize the chemical reaction of gaseous chemicals (precursor compounds) at different temperatures for which chemicals may decompose then react in situ.

The sample can be grown on a substrate with a catalyst as the nucleation center. Often consider as an easy but dirty method.

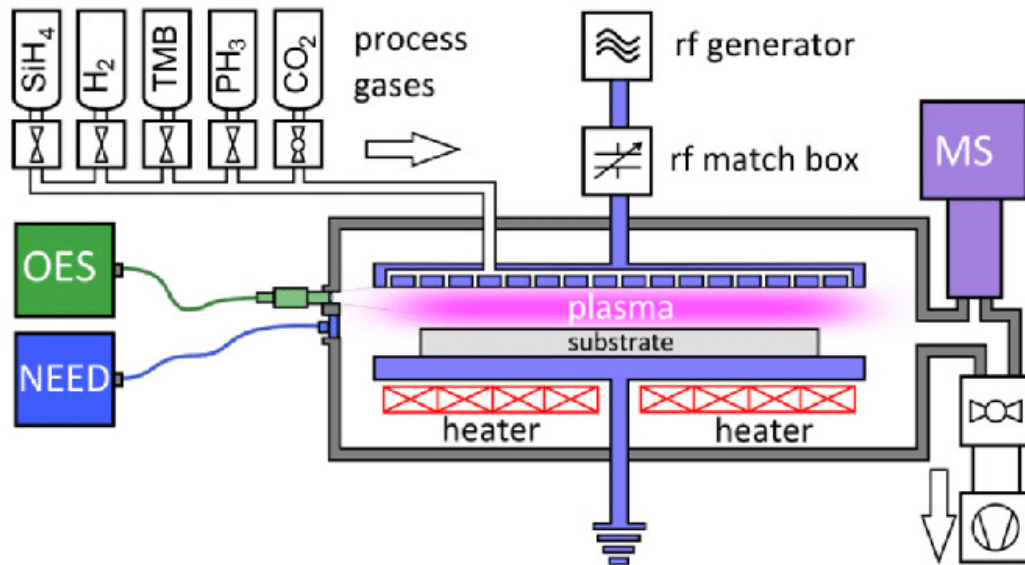


# Nanofabrication

## Plasma-Enhanced Chemical Vapor Deposition (PECVD)

Plasma reduces the required temperature for precursors, less power consumption.

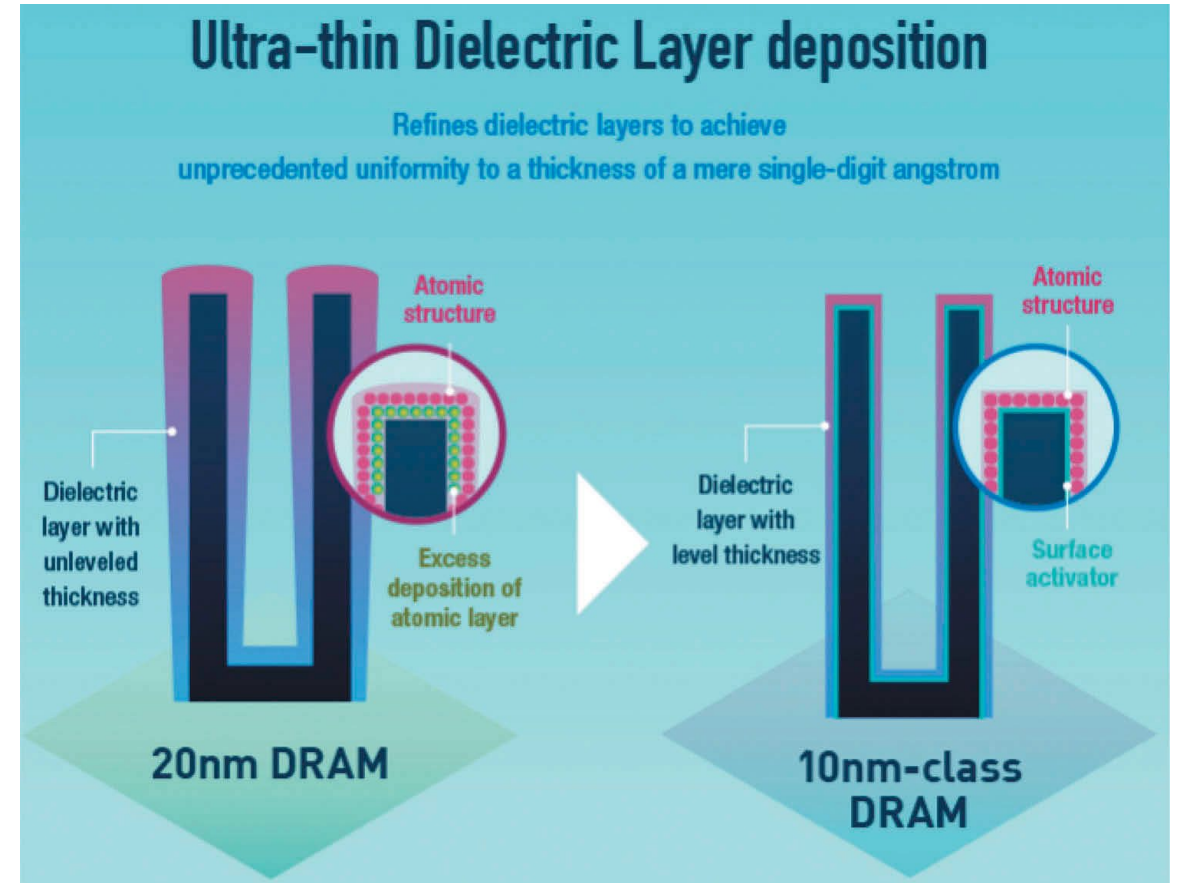
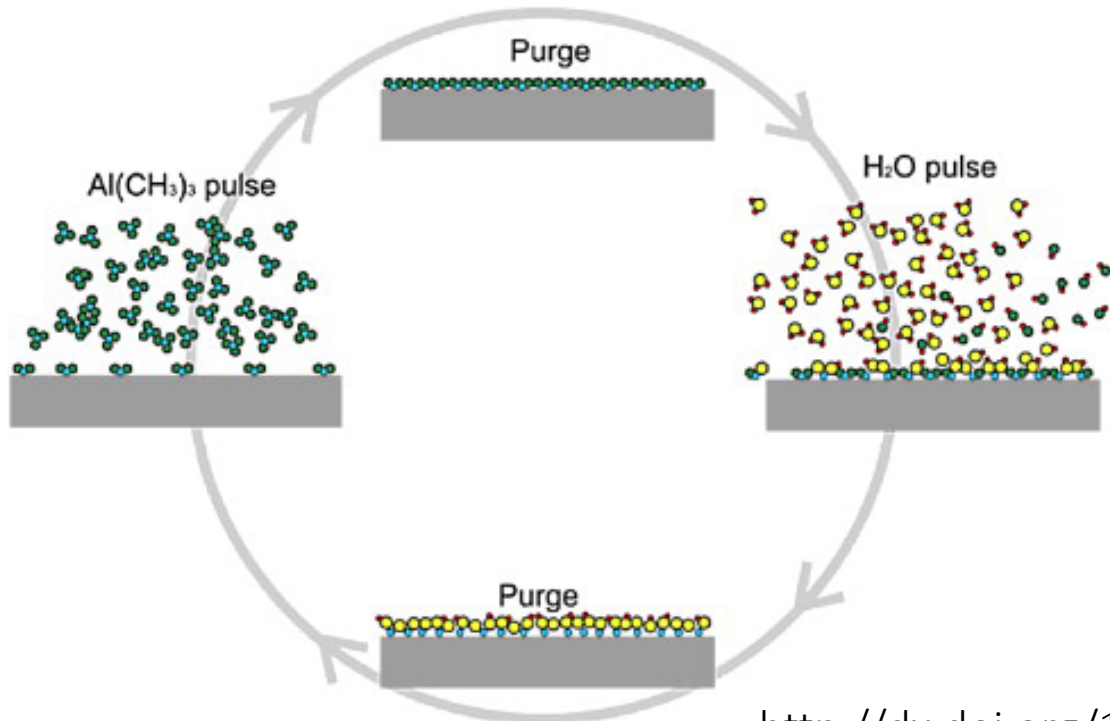
Applied Materials



# Nanofabrication

## Atomic Layer Deposition (ALD)

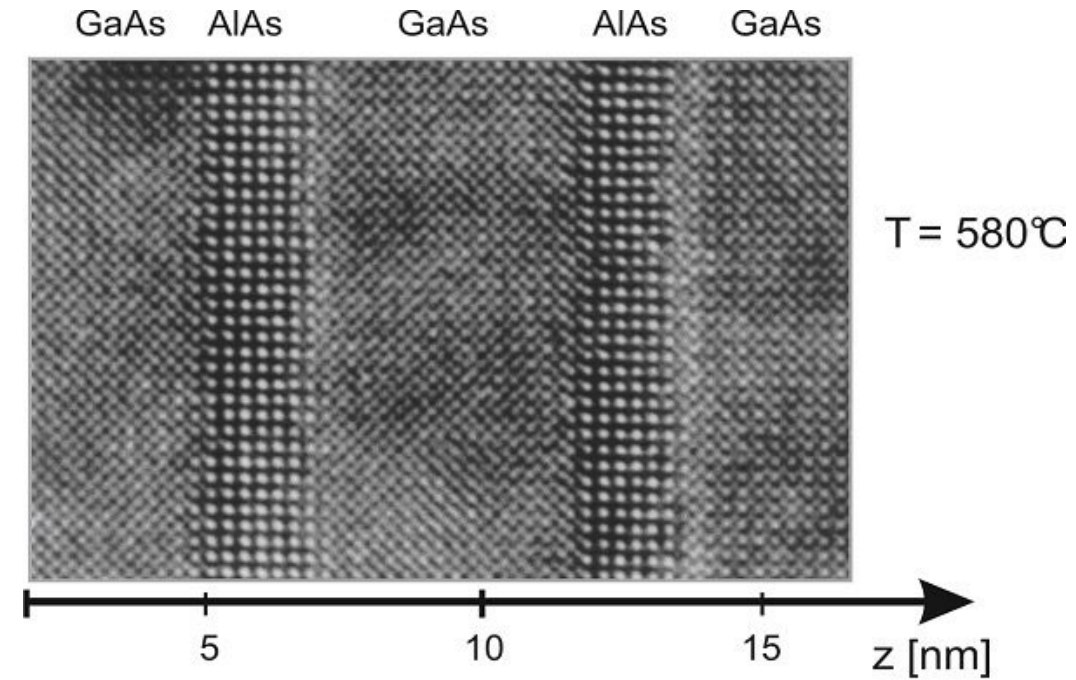
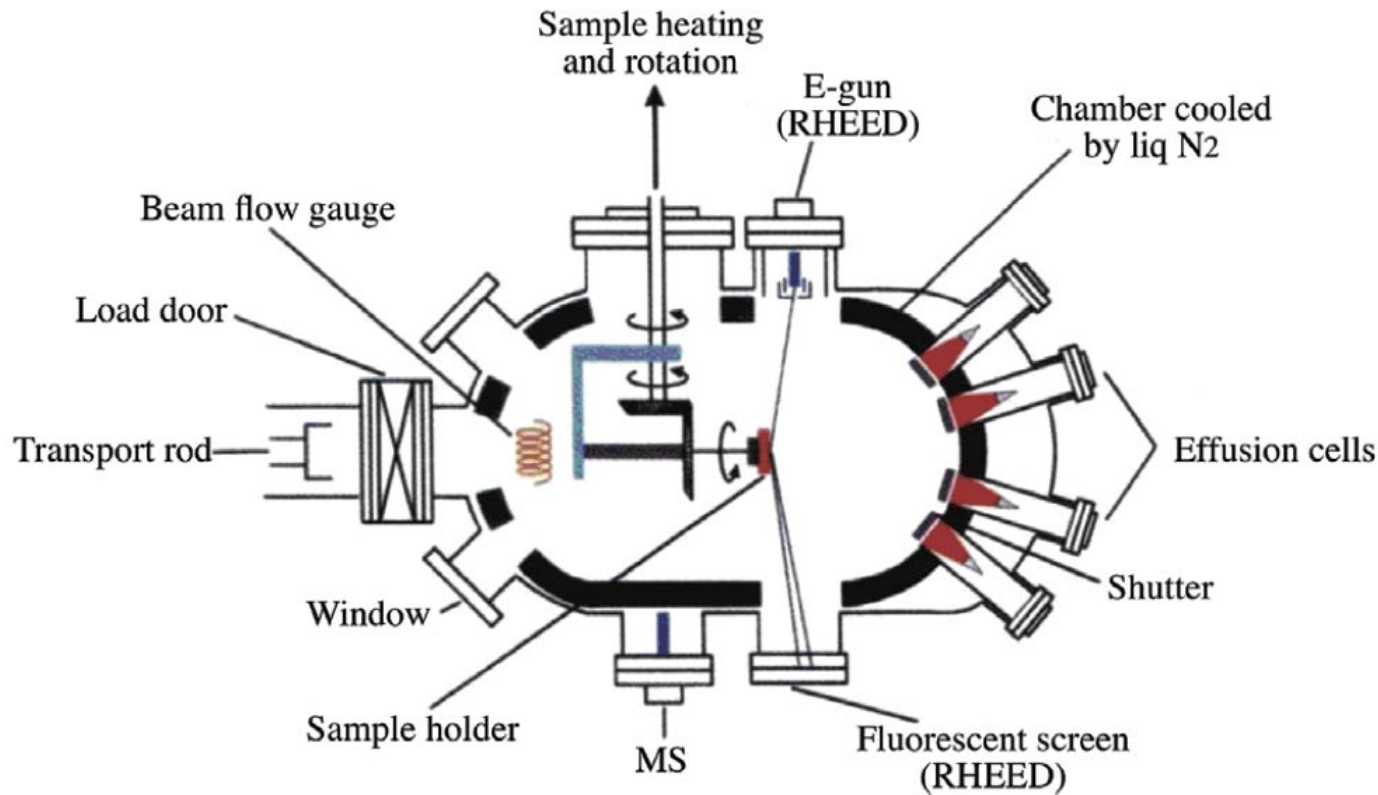
- A layer by layer growth process
- Very slow but good coverage



Samsung DRAM

# Nanofabrication

## Molecular beam epitaxy (MBE)



Simone Montanari Ph.D. thesis (2005)

- Atomically layer by layer growth process
- Very slow but extremely high quality
- UHV system, very expensive

# Nanofabrication

## **Material Removing techniques**

One can classify them into:

Chemical remove

Physical remove

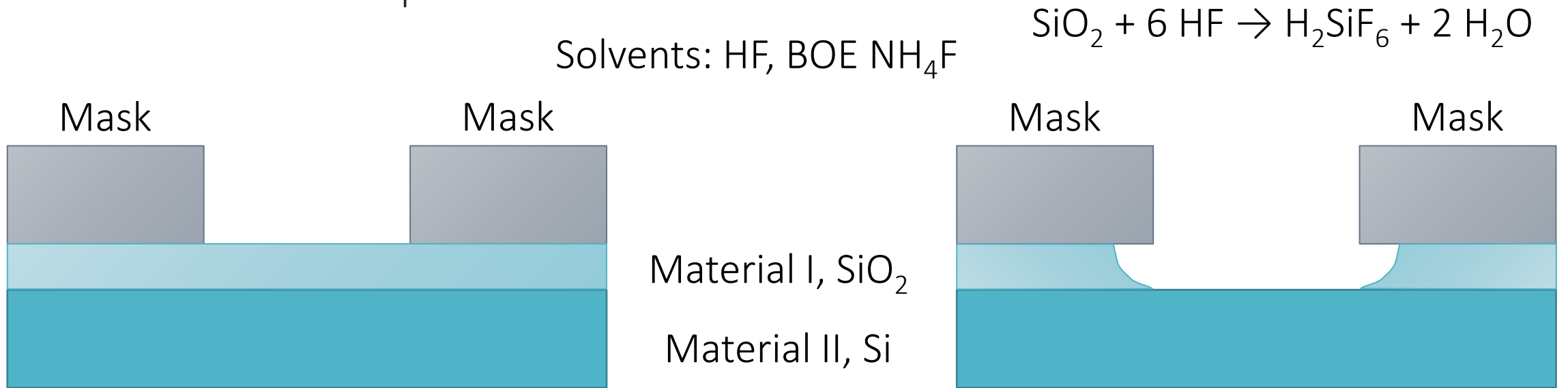
Physical Chemical remove

# Nanofabrication

## Chemical remove

A wet process, one can use chemicals to remove the unwanted materials.

Take SiO<sub>2</sub> as an example:

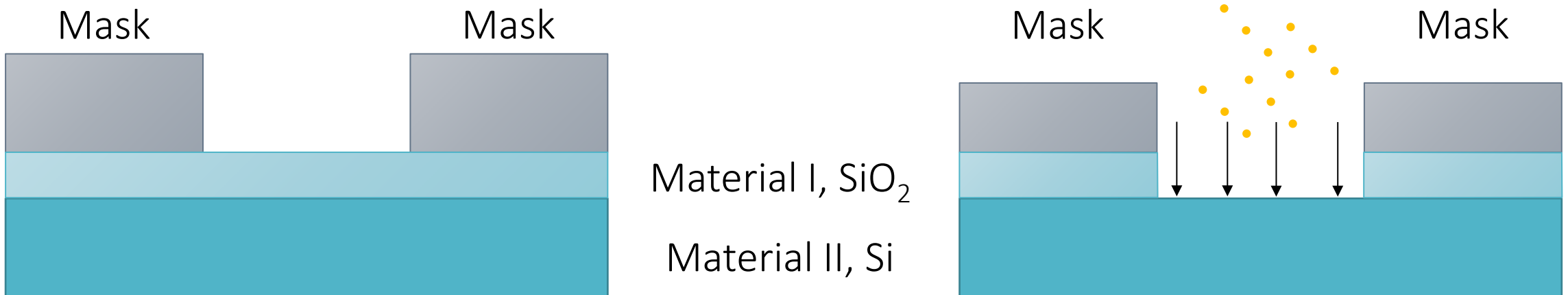


Etching rate(BOE\_7:1): to SiO<sub>2</sub> 80 nm/min at 20 C, to Si is almost zero, how about mask??

# Nanofabrication

## Physical remove

A dry etching process, use gas particle in a plasma environment to form ion bombardment on the material surface.



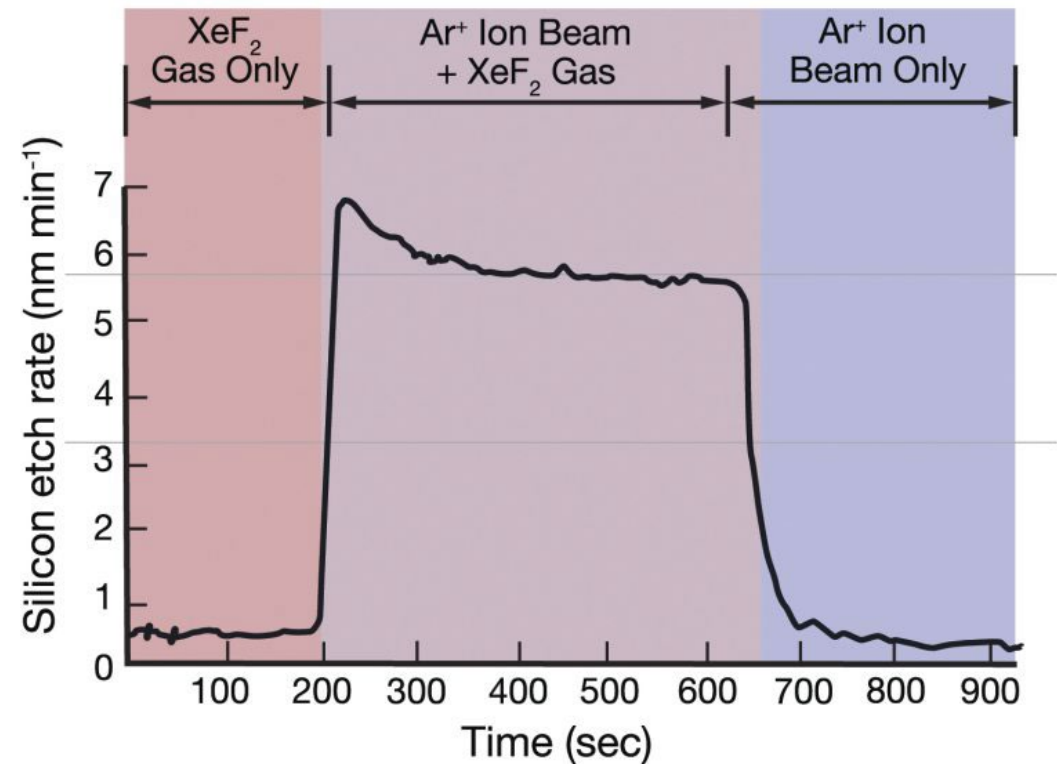
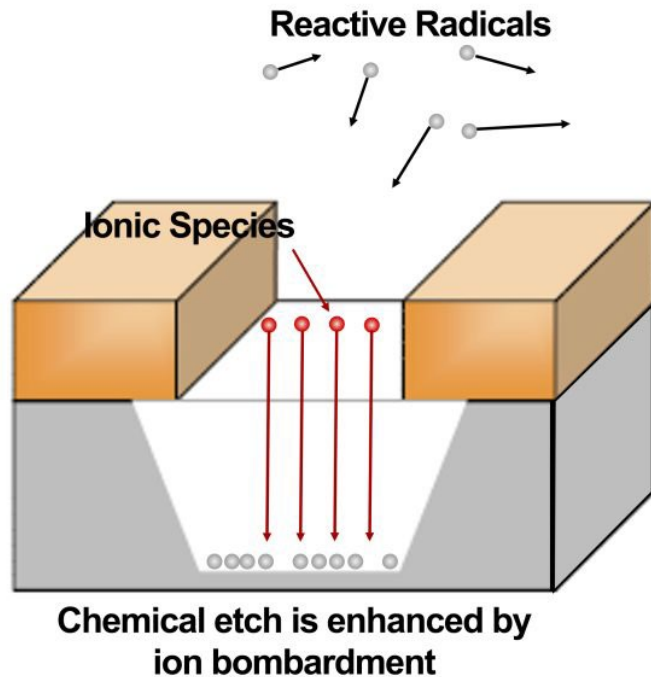
Etching rate: the same for everyone, therefore carefully calibration or endpoint detection is important

# Nanofabrication

Chemical and Physical remove

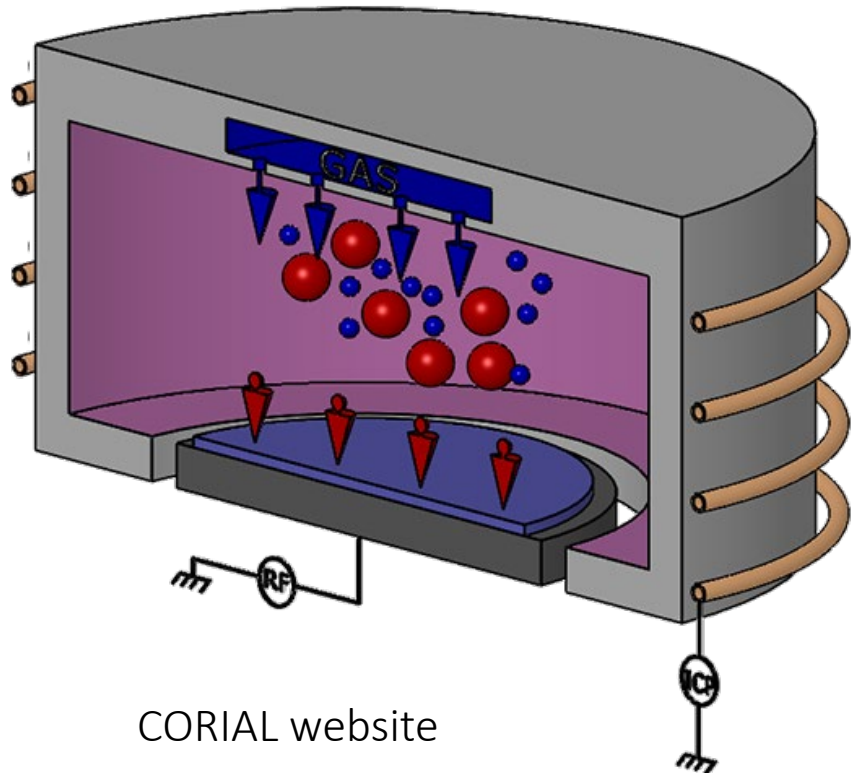
A combined process uses ions to enhance the chemical reaction.

## Reactive Ion Etching

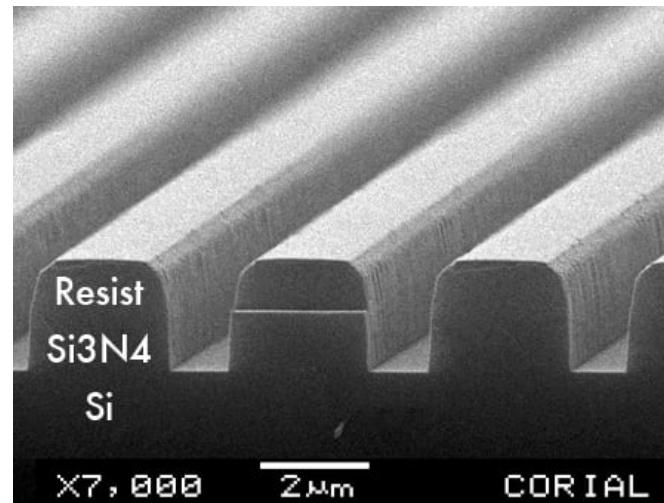


# Nanofabrication

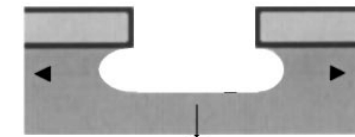
Chemical and Physical remove  
Inductively Coupled Plasma-RIE etch



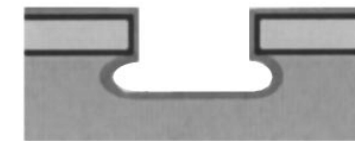
CORIAL website



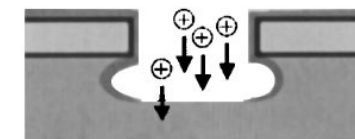
For high aspect ratio or VIA hole, Bosch process is needed



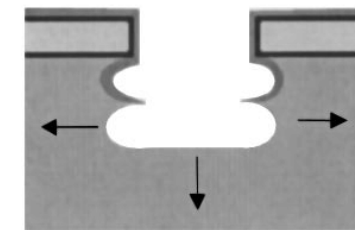
**First Etch**



**Passivate**



**Start of Second Etch**



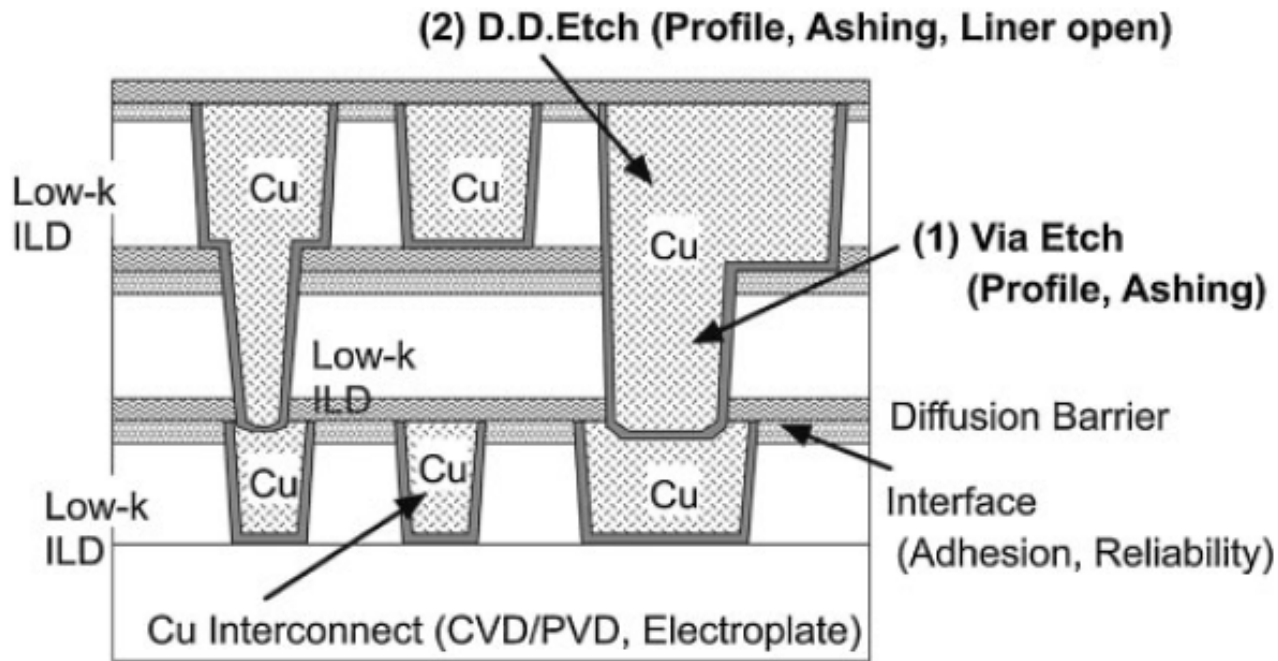
**Second Etch Continues**

C. J. D. Craigie et al  
<http://dx.doi.org/10.1116/1.1515910>

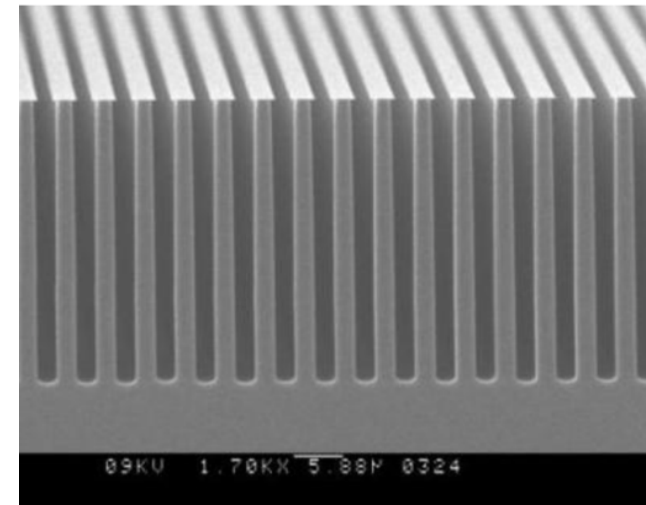
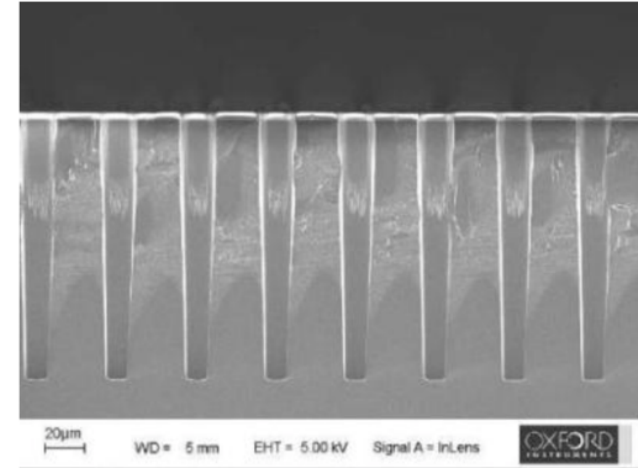
# Nanofabrication

Chemical and Physical remove

Advanced etching technique is important!!!



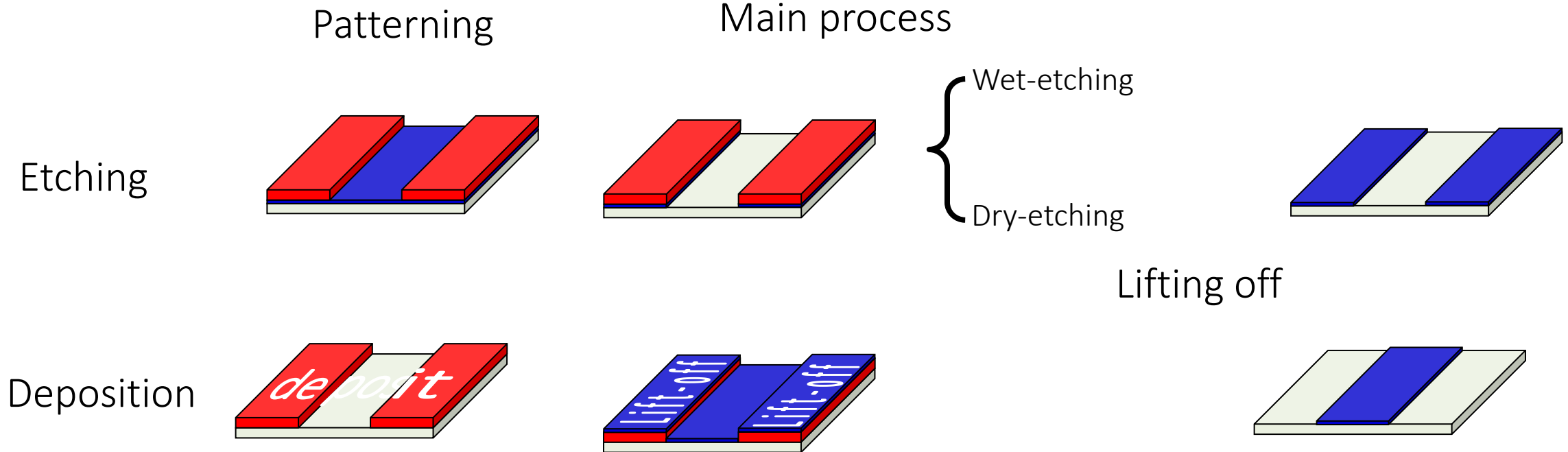
Haruhiko ABE et al. JJAP (2008)



AZoNano.com/Oxford

# Nanofabrication

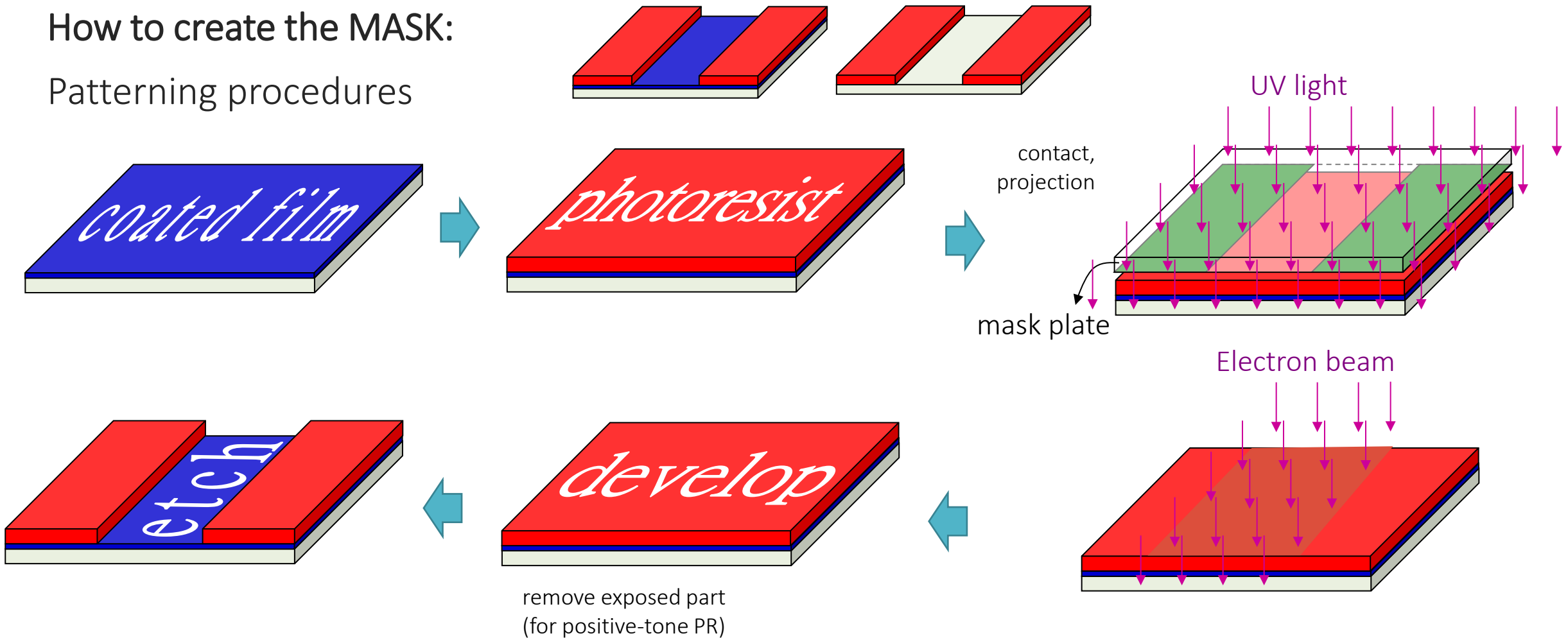
How to create the MASK: the workflow for lithography



# Nanofabrication

How to create the MASK:

Patterning procedures



# Nanofabrication

Resolution:  $R = k_1 (\lambda/NA)$

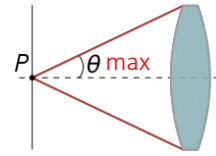
Depth of Focus  $DoF = k_2 (\lambda/NA^2)$

$NA = \sin\theta = \text{numerical aperture}$

$K_1 = \text{a constant for a specific lithography process}$   
 smaller  $K_1$  can be achieved by  
 improving the process or resist contrast

Calculated R and DoF values

UV wavelength	248 nm	13.4 nm
Typical NA	0.75	0.25
Production value of $k_1$	0.5	0.5
Resolution	0.17 $\mu\text{m}$	0.027 $\mu\text{m}$
DoF (assuming $k_2 = 1$ )	0.44 $\mu\text{m}$	0.21 $\mu\text{m}$



## SOURCES OF RADIATION FOR MICROLITHOGRAPHY

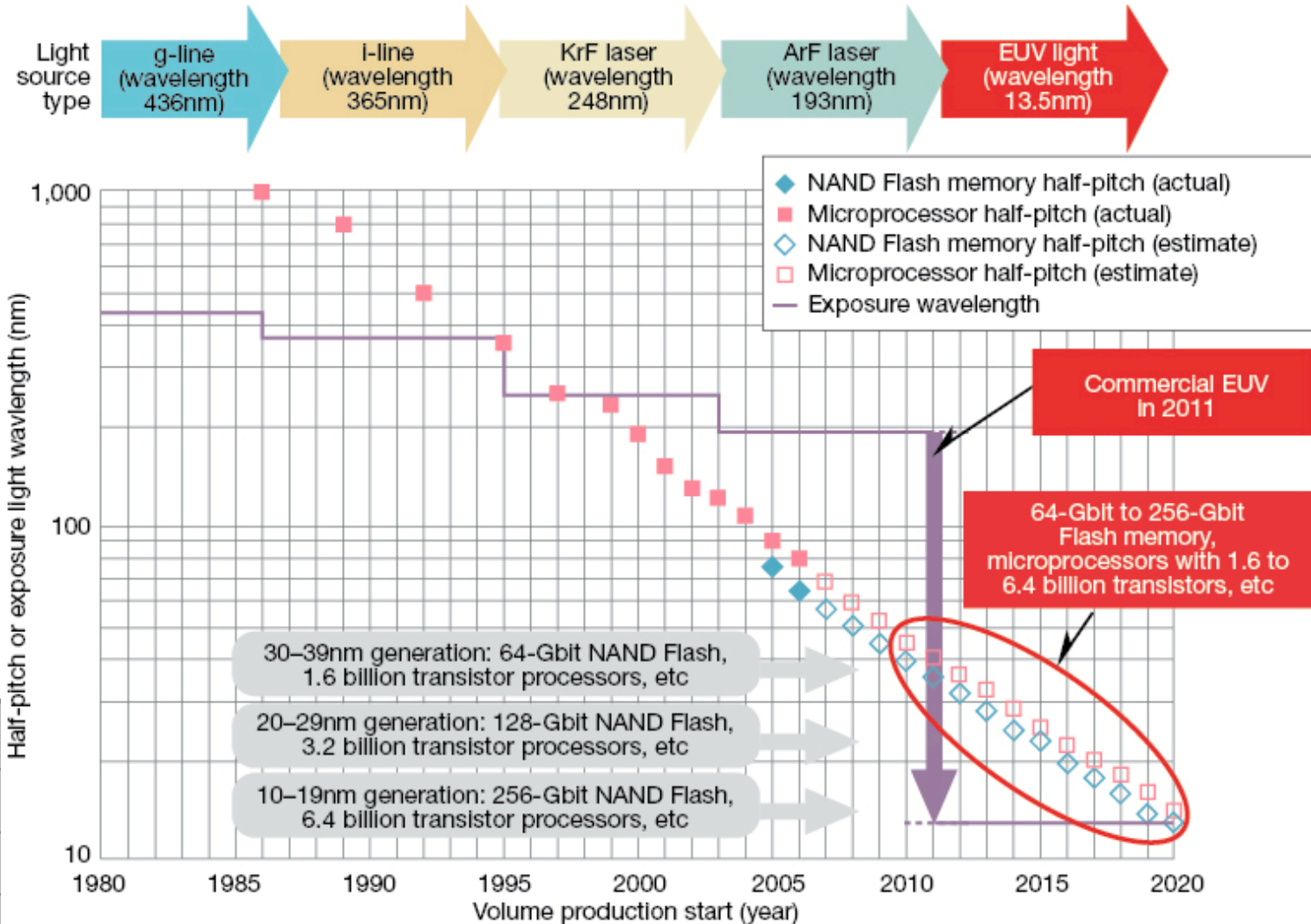
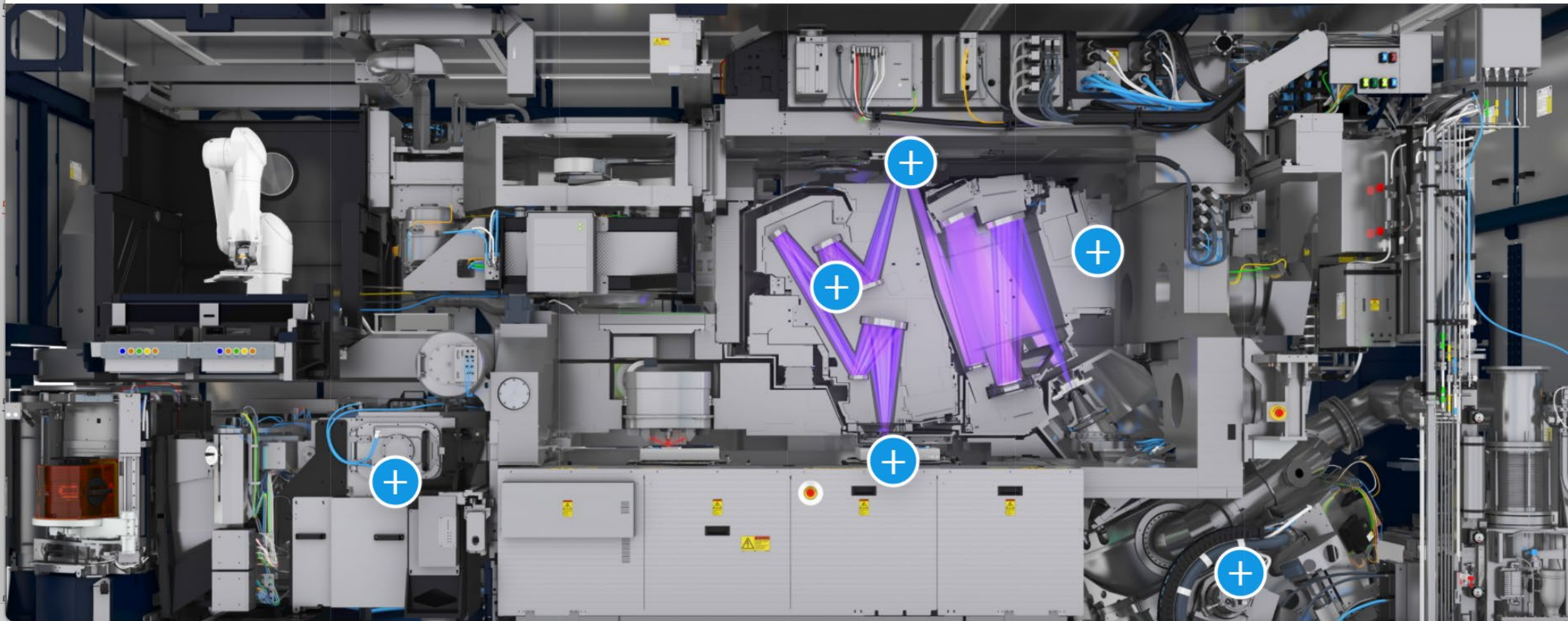


Diagram by Nikkei Electronics based on materials from Intel, International Technology Roadmap for Semiconductors (ITRS), etc. [http://www.newmaker.com/news\\_41958.html](http://www.newmaker.com/news_41958.html)

# Nanofabrication

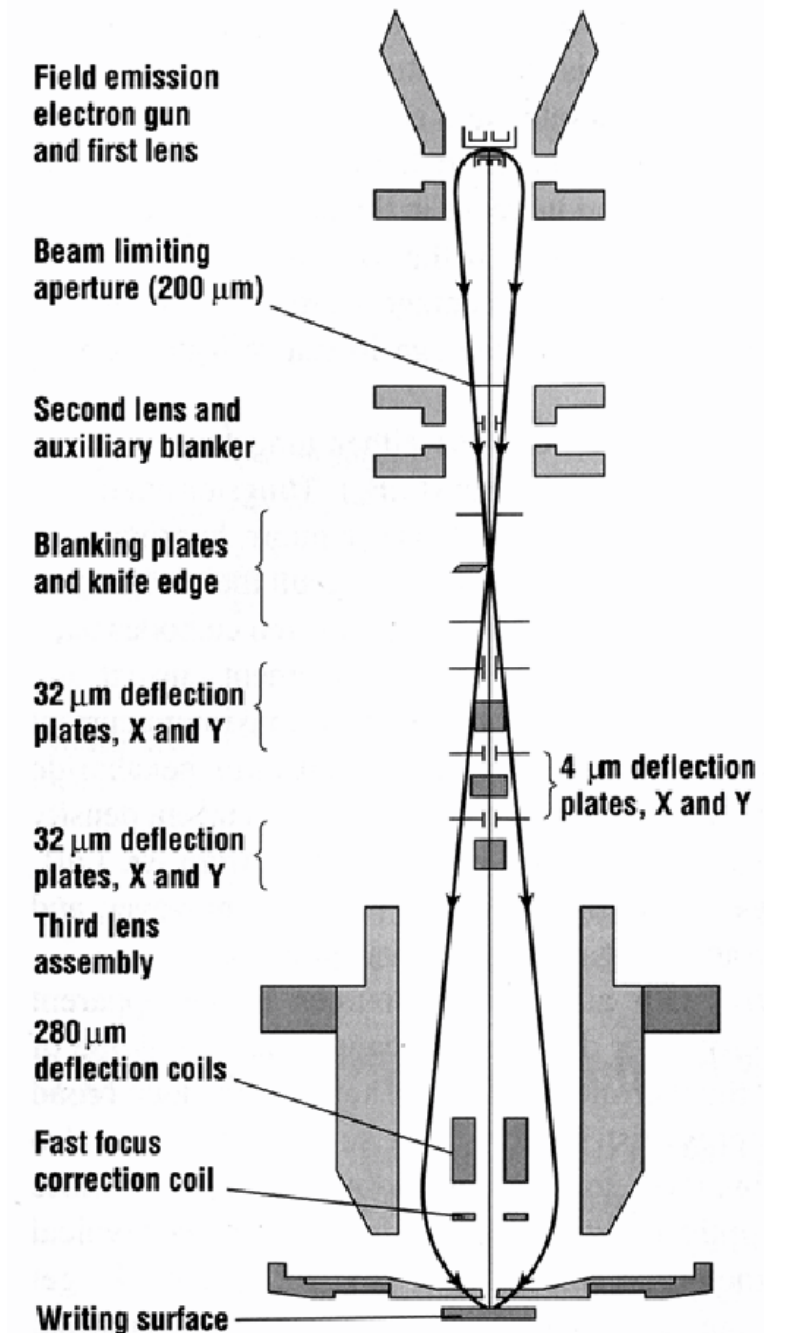
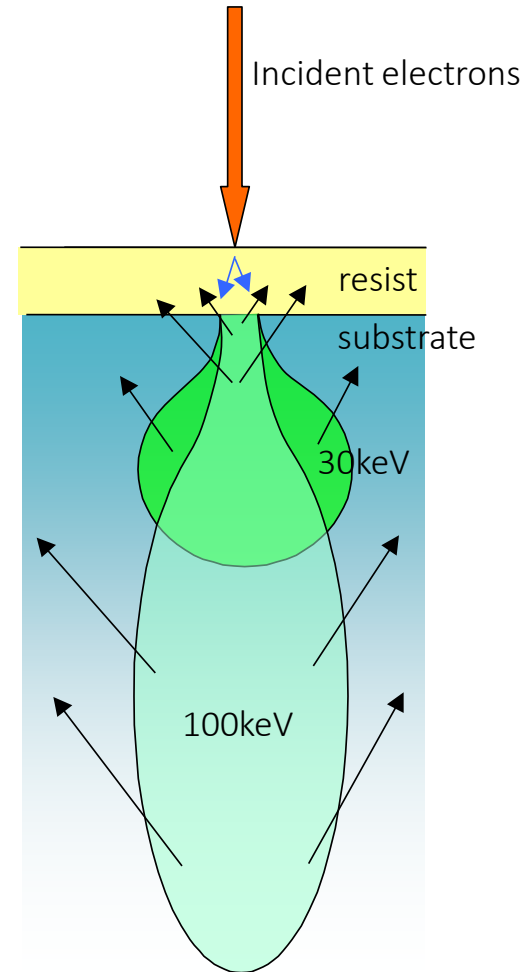
ASML EUV system NXE:3400B (ref: ASML website)



# Nanofabrication

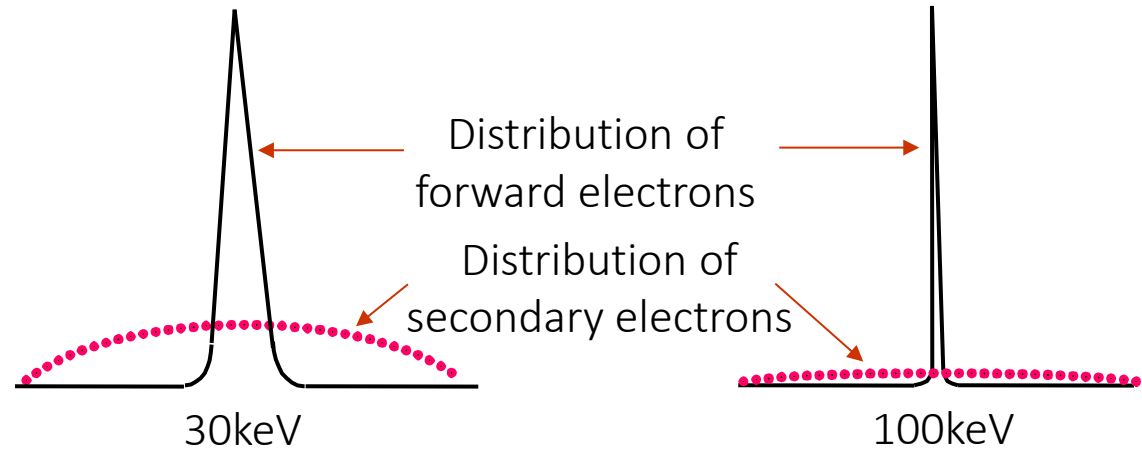
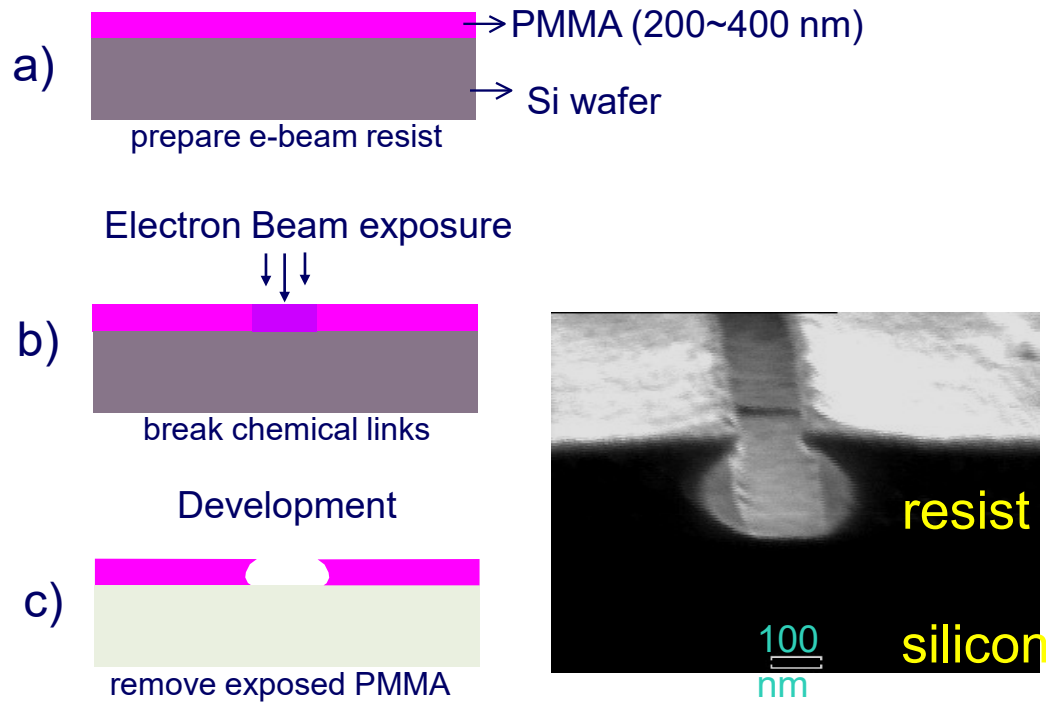
## e-beam lithography

- No mask is needed! (both pros and cons)
- the wavelength of electrons can be controlled, therefore fine structures can be realized.
- However, compared to photolithography, it is a much slower process.
- Incident electron energy, current can control the spot size of the beam, therefore, influence the feature as well as speed.
- It is very useful in research but not industry.



# Nanofabrication

## e-beam lithography

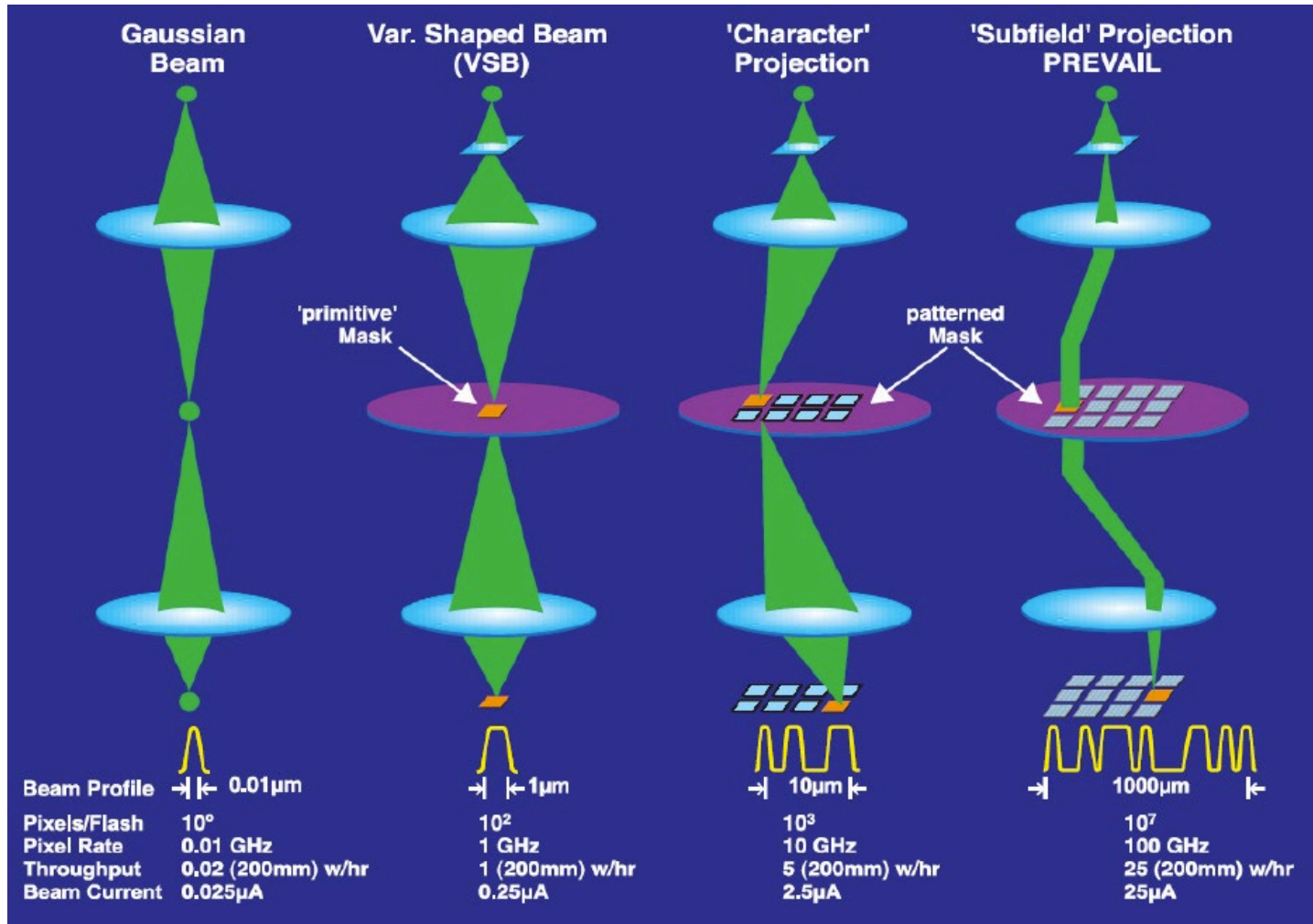


1. Good for the prototype test
2. Thin resist line-width < 30nm
3. Clear align key image
4. Good for lift-off process
5. Lack of stage stability

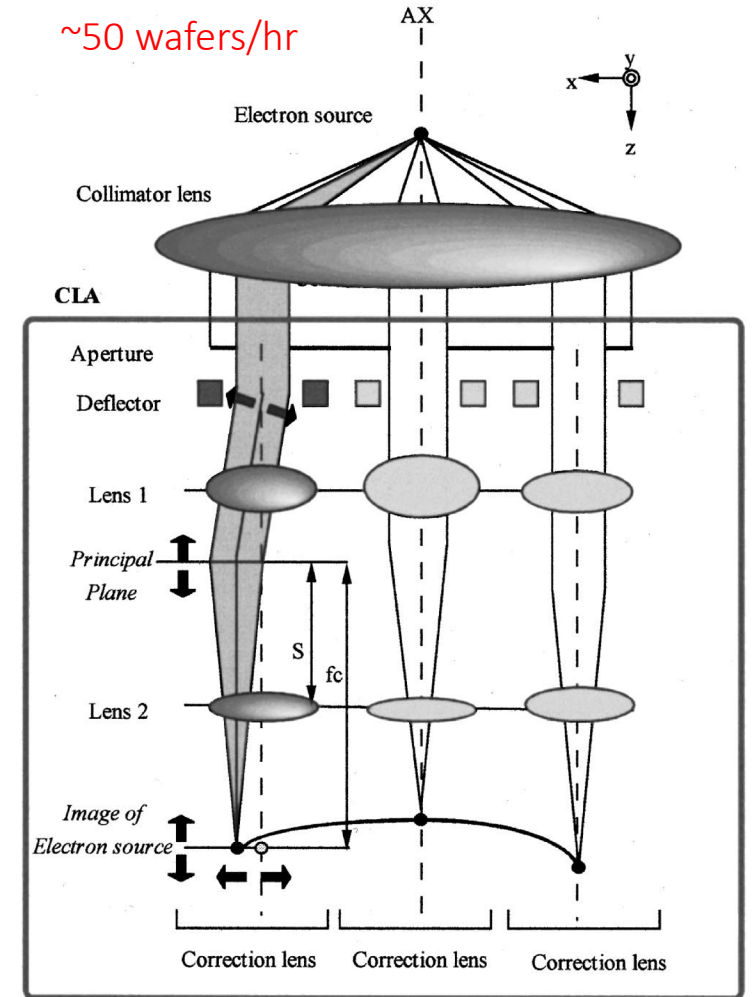
1. Good for large-area exposure
2. Thin resist line-width < 10nm
3. Require thick/clear align keys
4. Require extra resist engineering
5. Stable/accurate stage stability



# Nanofabrication



楊富量 (NDL), Outlook for 15nm CMOS Manufacture



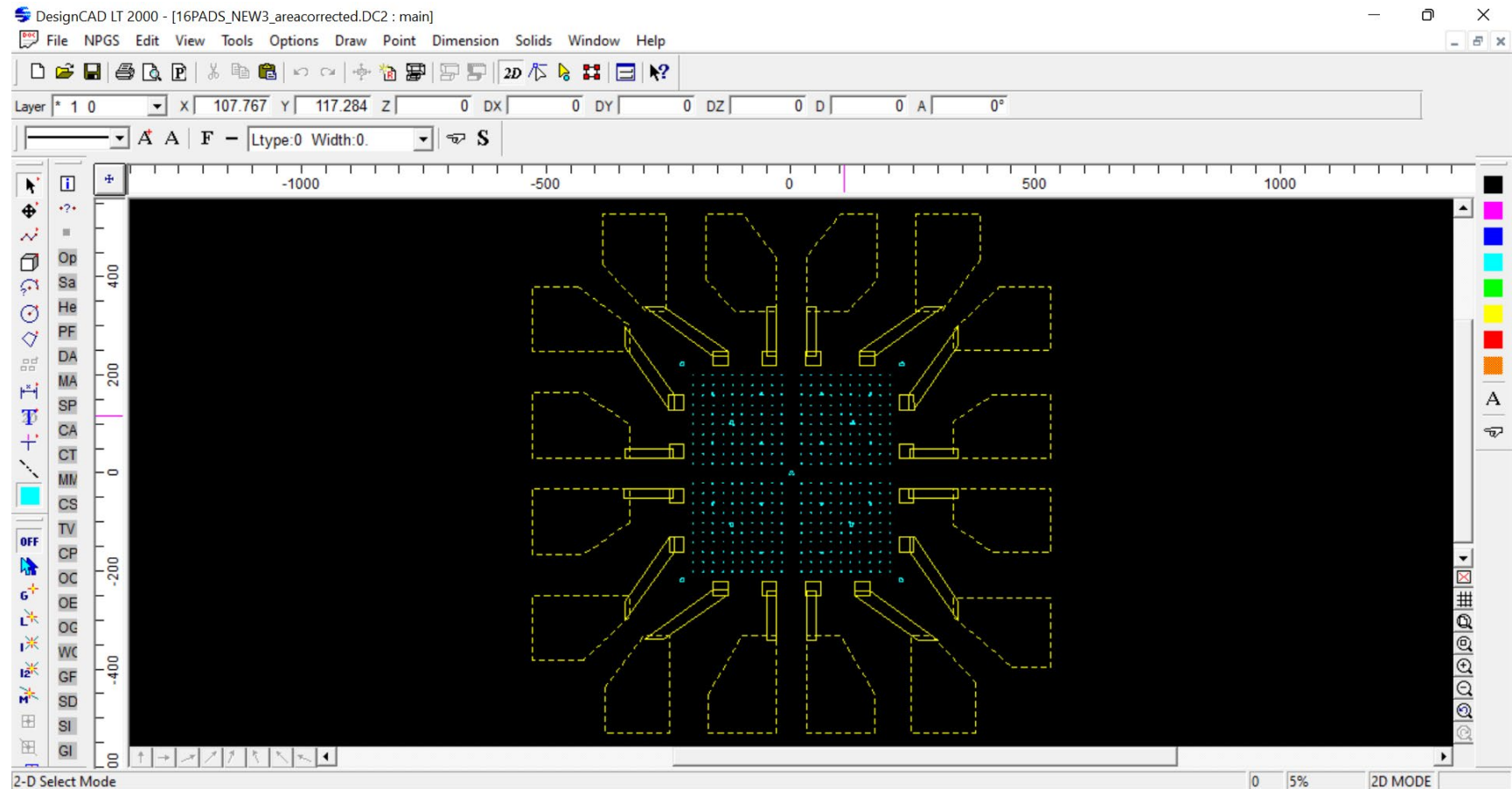
M. Muraki et al. J. Vac. Sci. Technol. B 18(6), 3061, 2000, Canon Inc.,

# Nanofabrication

## E-beam lithography

One also needs to generate the patterns for which you would like the e-beam system to write.

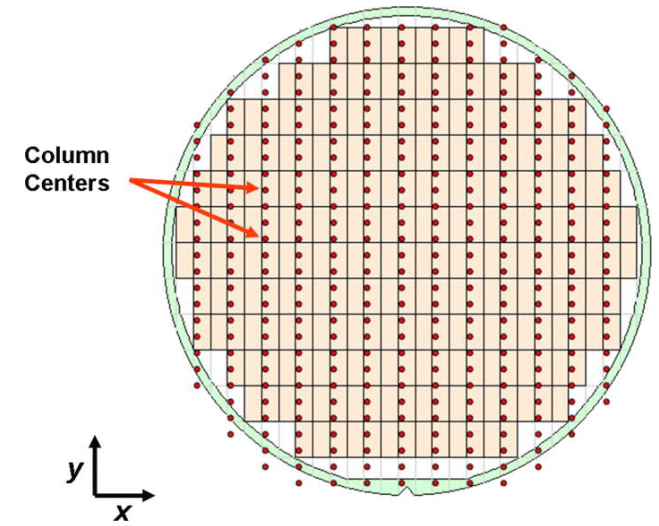
There is a lot of software for this purpose such as AutoCAD, K-layout, DesignCAD, etc...



# Nanofabrication

## E-beam lithography

Beam voltage: 50- 150 kV  
Beam current: 10<sup>th</sup> pA to 800 nA  
Field size: 0.5x 0.5 to 300x300 mm<sup>2</sup>



Dan Meisburger et al.  
[doi.org/10.1116/1.4931589](https://doi.org/10.1116/1.4931589)

RAITH



Elionix



# Nanofabrication

## Characterizations:

AFM,  
profilometer,

electrical measurement,

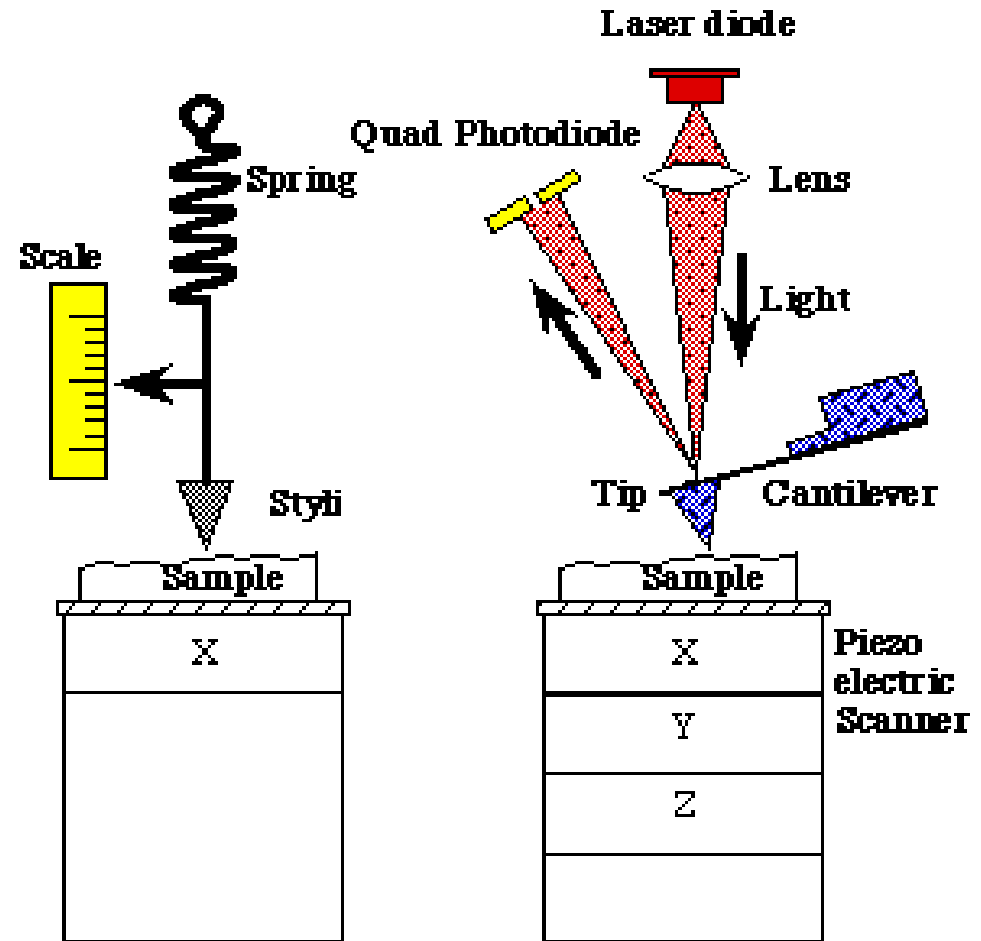
X-ray,

Photoluminescence,

Raman spectrum,

ARPES,

SEM/TEM



Idea of Stylus profilometer

Atomic Force Microscope

# Nanofabrication

## Characterizations:

AFM,

profilometer,

electrical measurement,

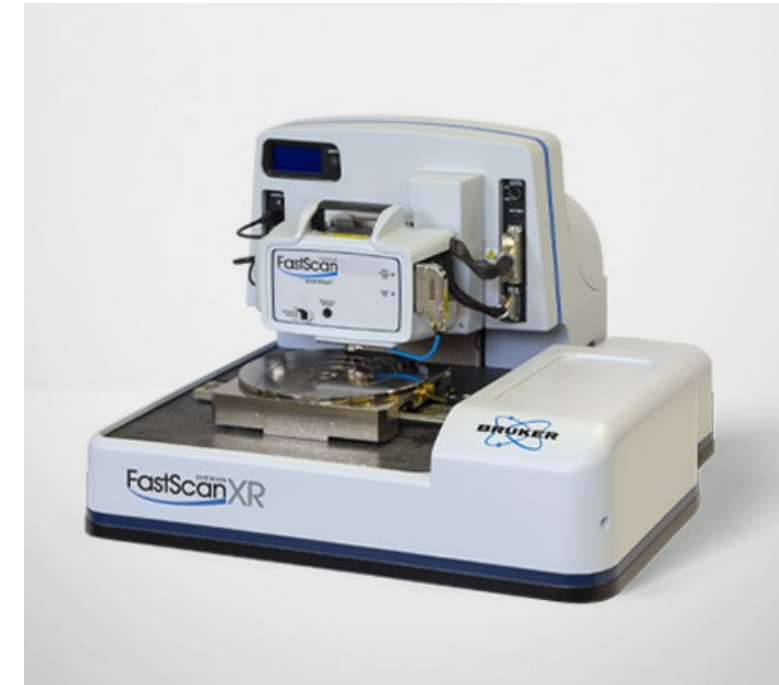
X-ray,

Photoluminescence,

Raman spectrum,

ARPES,

SEM/TEM



Source: Bruker, Park

# Nanofabrication

## Characterizations:

AFM,

profilometer,

electrical measurement,

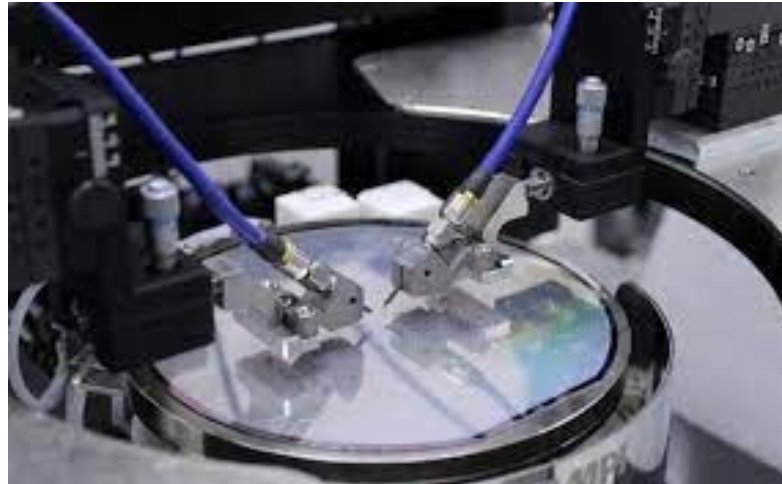
X-ray,

Photoluminescence,

Raman spectrum,

ARPES,

SEM/TEM



<https://ayscomdatatec.com/en/probe-stations/>

featuring the  
Model 336 controller



<https://www.photonicsonline.com/>

One can measure C-V, I-V, thermal properties, etc.

# Nanofabrication

## Characterizations:

AFM,

profilometer,

electrical measurement,

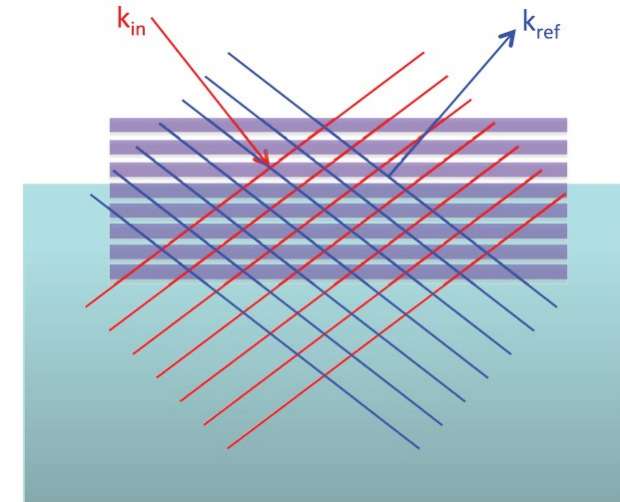
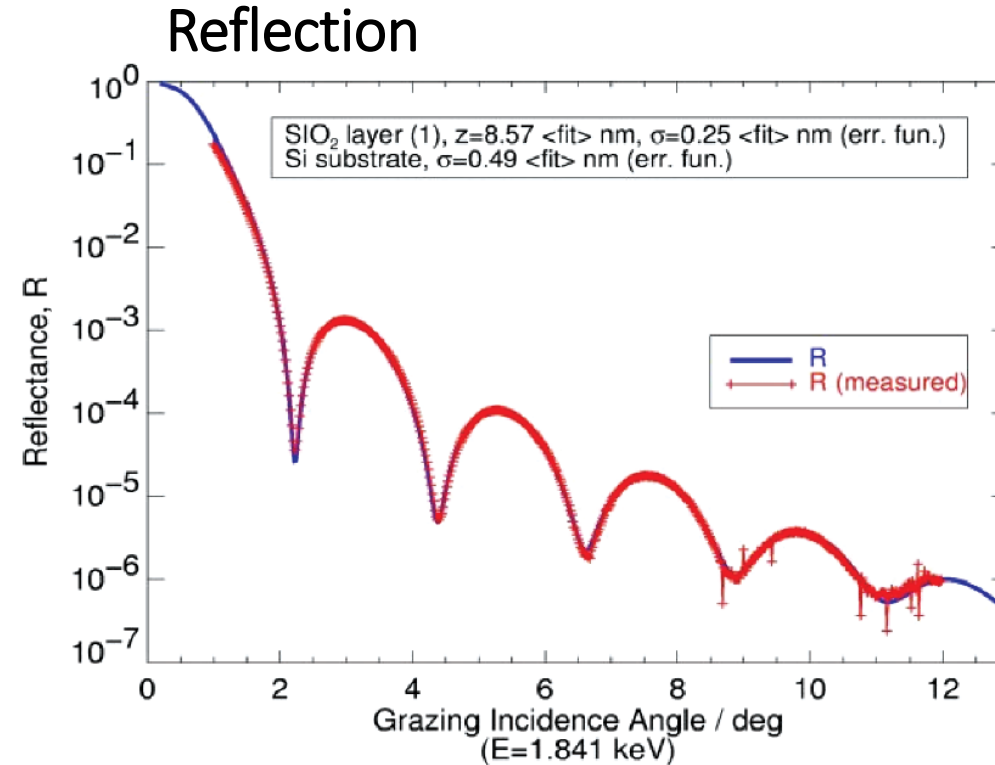
X-ray,

Photoluminescence,

Raman spectrum,

ARPES,

SEM/TEM



# Nanofabrication

## Characterizations:

AFM,

profilometer,

electrical measurement,

X-ray,

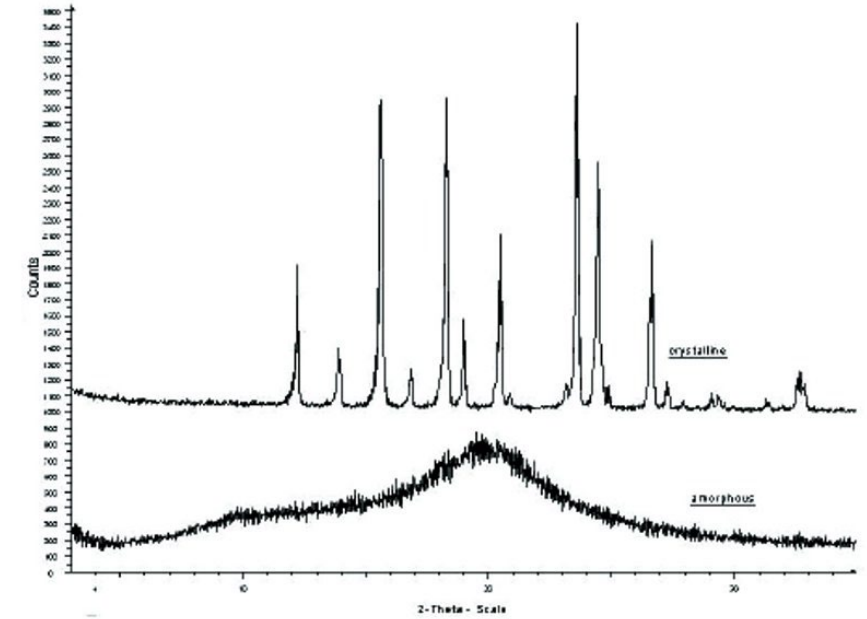
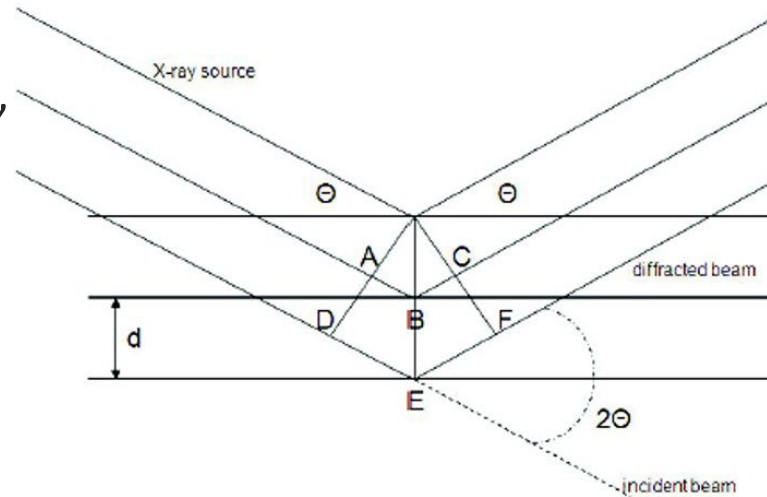
Photoluminescence,

Raman spectrum,

ARPES,

SEM/TEM

## Powder diffraction



Source: IOP and Anthony L. Young

# Nanofabrication

## Characterizations:

AFM,  
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electrical measurement,

X-ray,

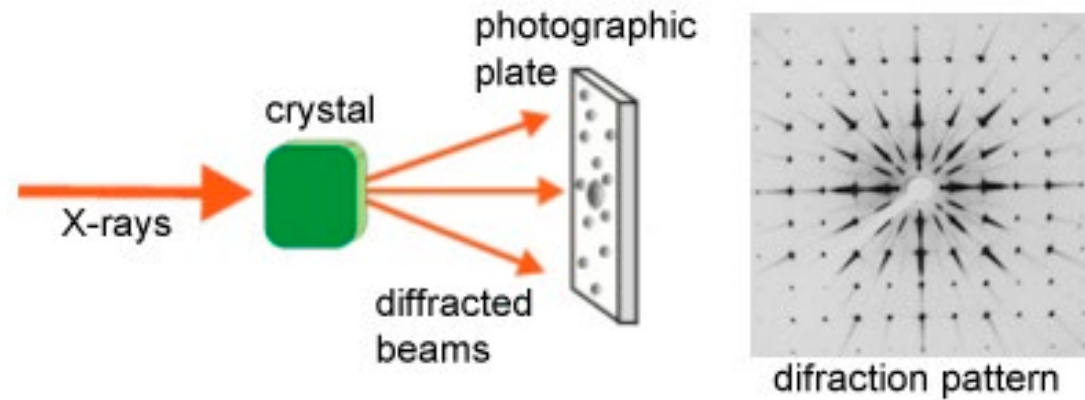
Photoluminescence,

Raman spectrum,

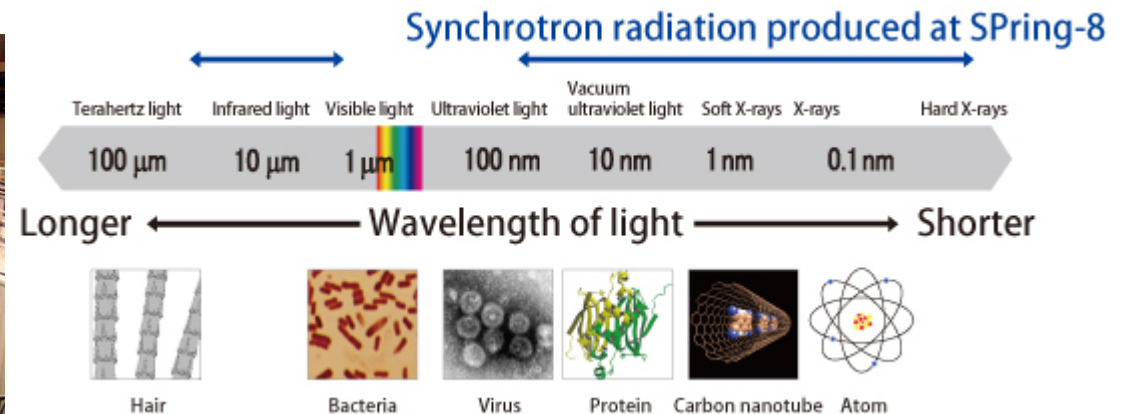
ARPES,

SEM/TEM

## Transmission



Spring 8



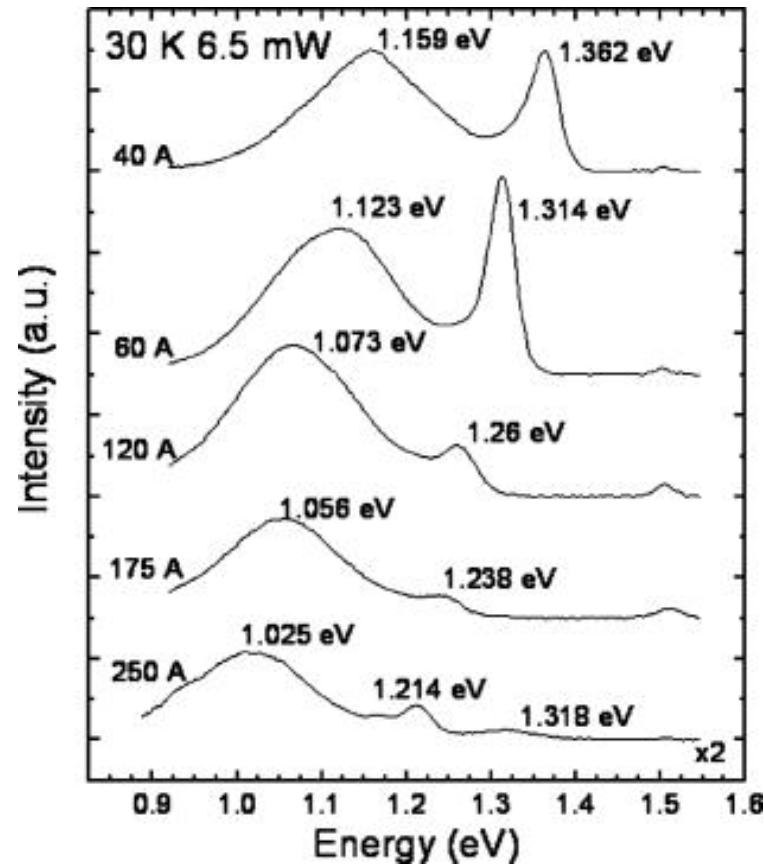
# Nanofabrication

## Characterizations:

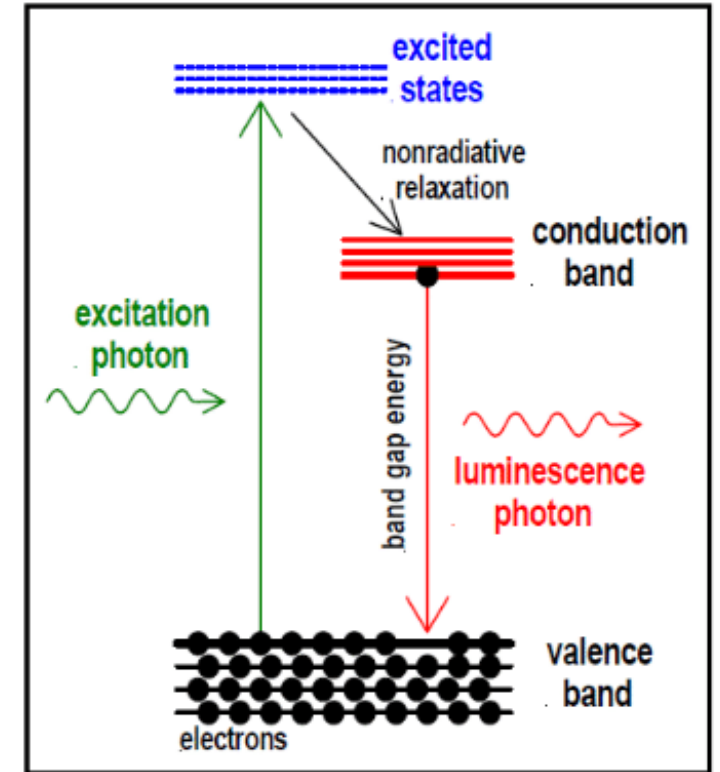
AFM,  
profilometer,  
electrical measurement,  
X-ray,

Photoluminescence,  
Raman spectrum,  
ARPES,

SEM/TEM



JF Chen, et al, JAP 2007



Puong Vuong, thesis

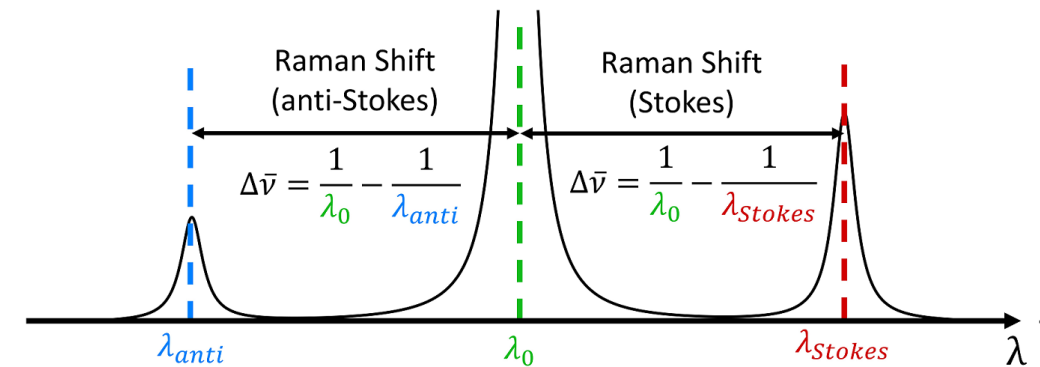
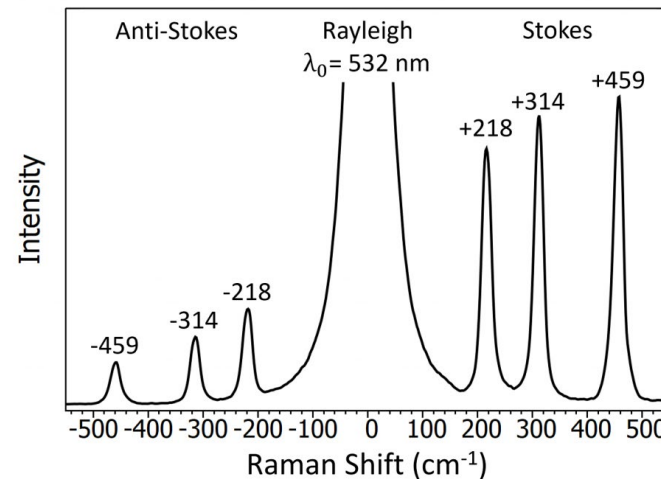
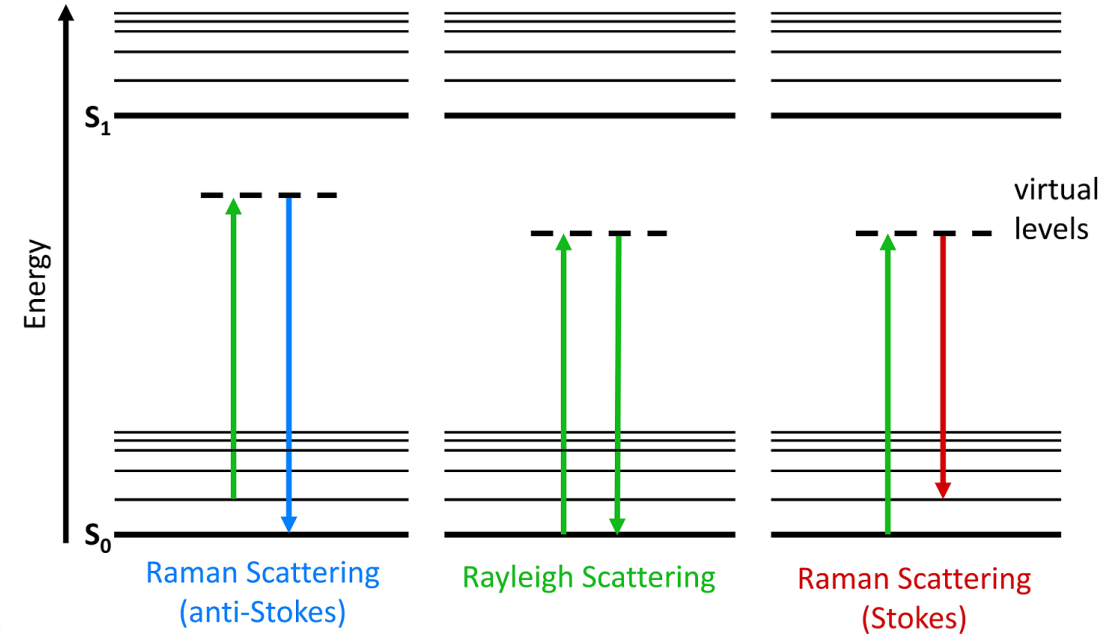
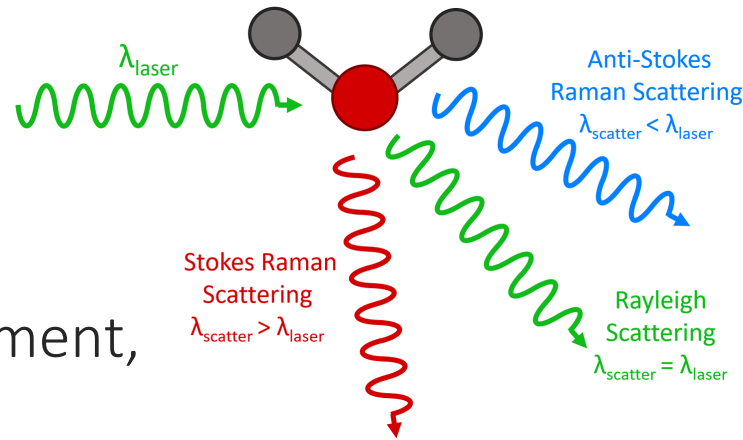
# Nanofabrication

Raman, an inelastic process in which photon electron transfer to molecule

## Characterizations:

AFM,  
profilometer,  
electrical measurement,  
X-ray,

Photoluminescence,  
Raman spectrum,  
ARPES,  
SEM/TEM



# Nanofabrication

## Characterizations:

AFM,

profilometer,

electrical measurement,

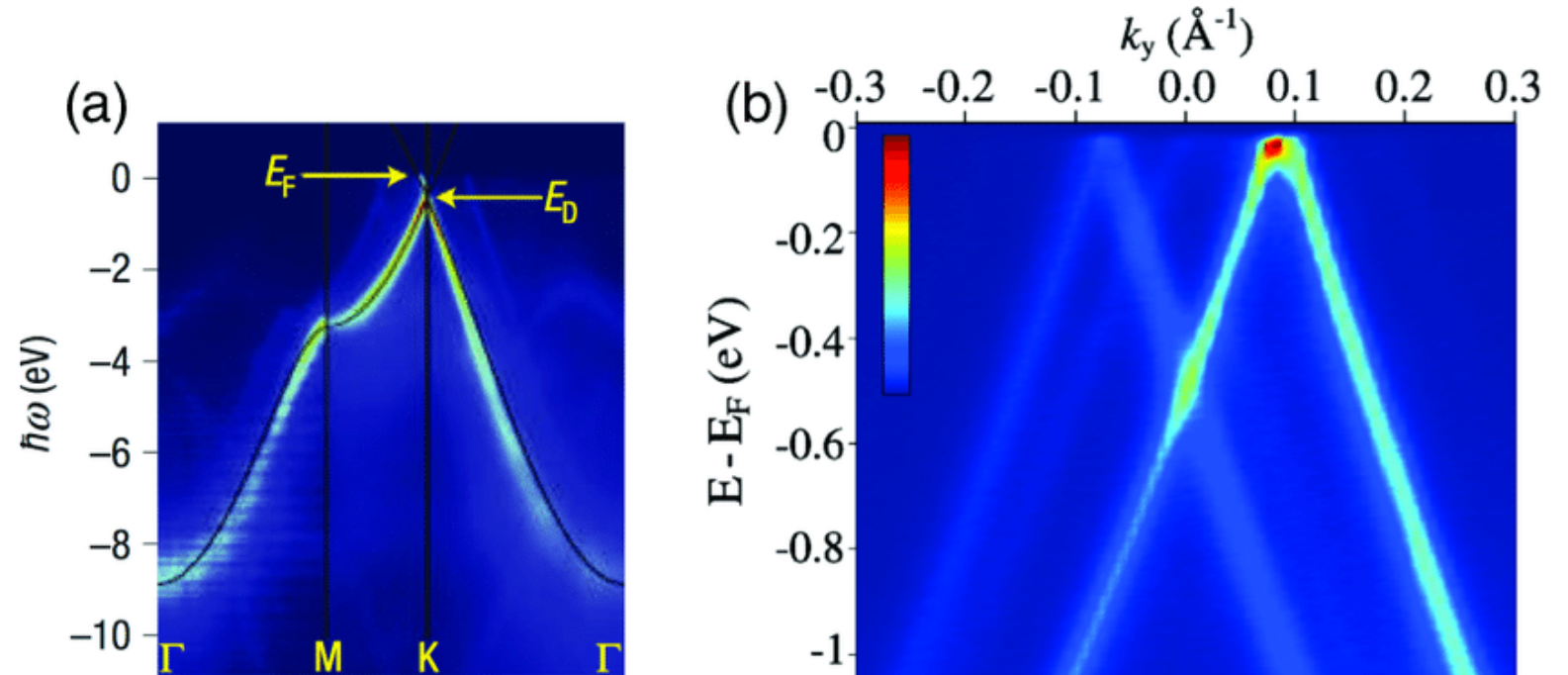
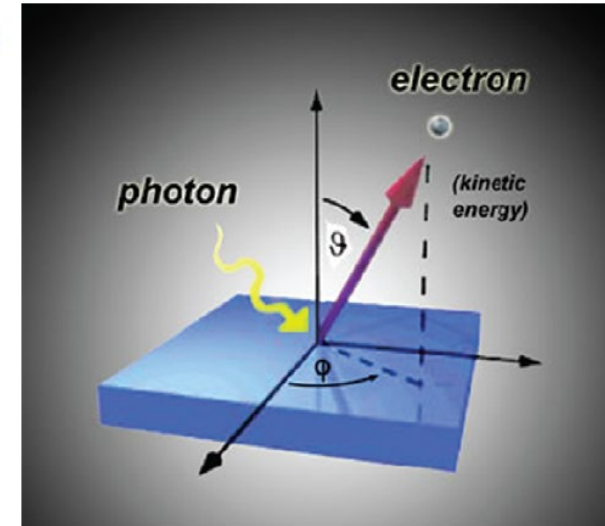
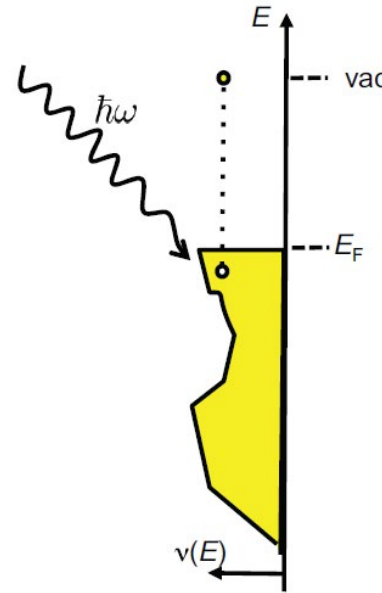
X-ray,

Photoluminescence,

Raman spectrum,

ARPES,

SEM/TEM

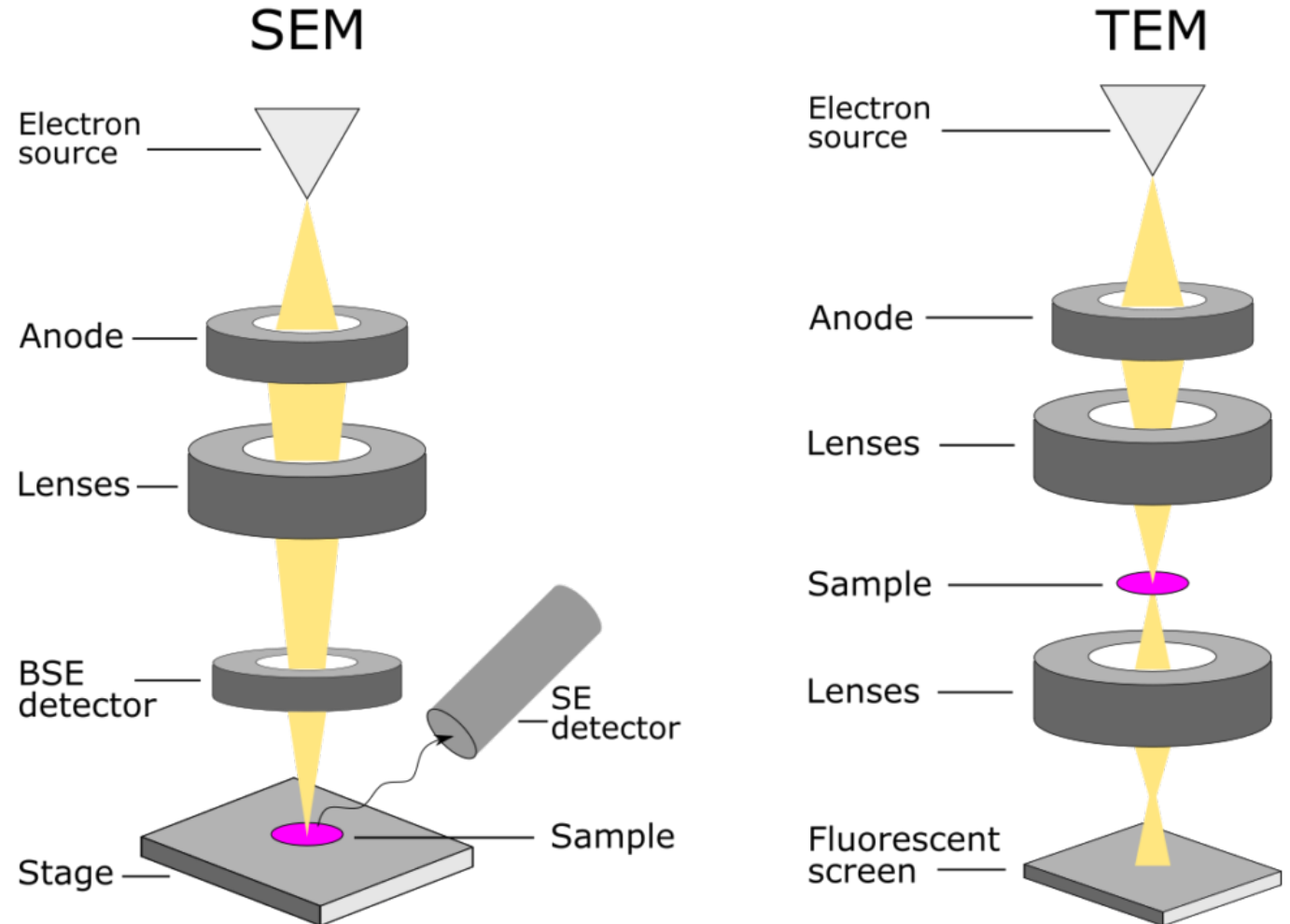


# Nanofabrication

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AFM,  
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electrical measurement,  
X-ray,  
Photoluminescence,  
Raman spectrum,  
ARPES,

SEM/TEM

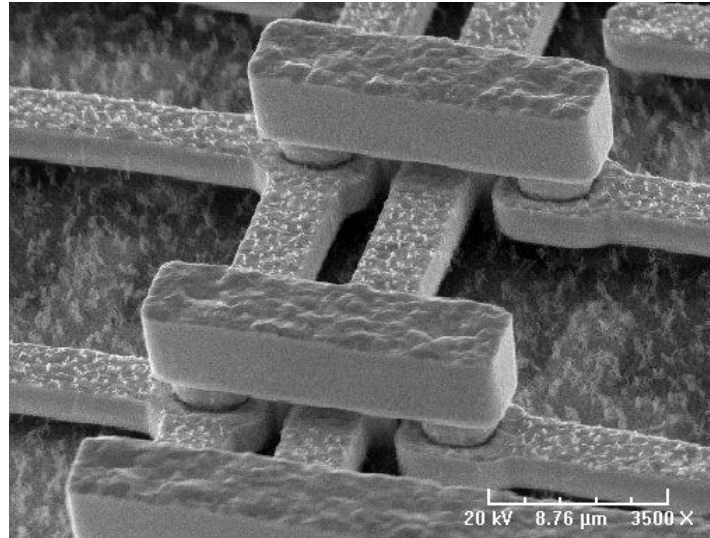


# Nanofabrication

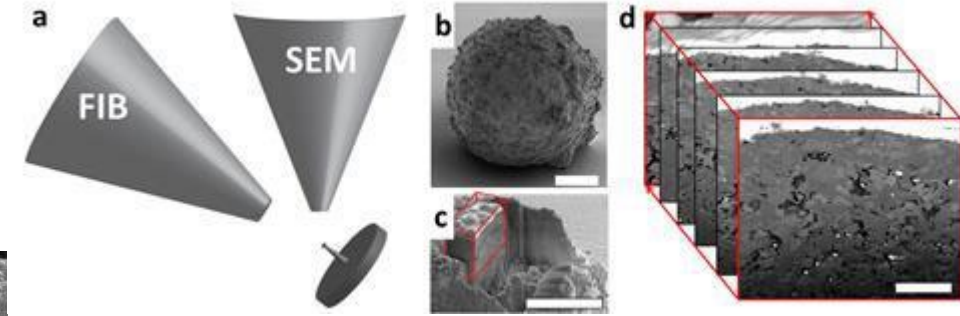
## Characterizations:

AFM,  
profilometer,  
electrical measurement,  
X-ray,  
Photoluminescence,  
Raman spectrum,  
ARPES,

SEM/TEM



<https://orlabs.com/services/material-analysis/sem/>



Bert Weckhuysen / Utrecht University



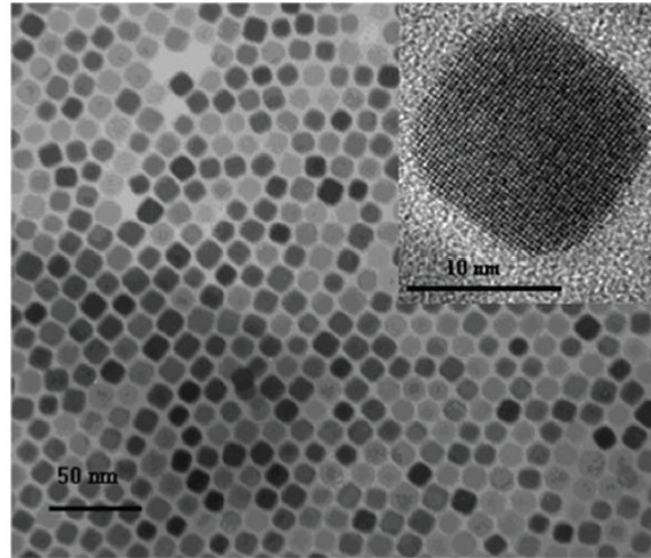
<https://www.huttonltd.com/services/scanning-electron-microscopy-sem>

# Nanofabrication

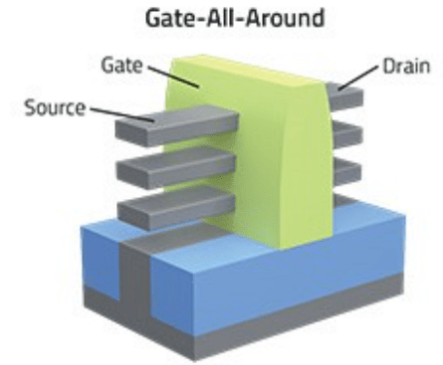
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profilometer,  
electrical measurement,  
X-ray,  
Photoluminescence,  
Raman spectrum,  
ARPES,

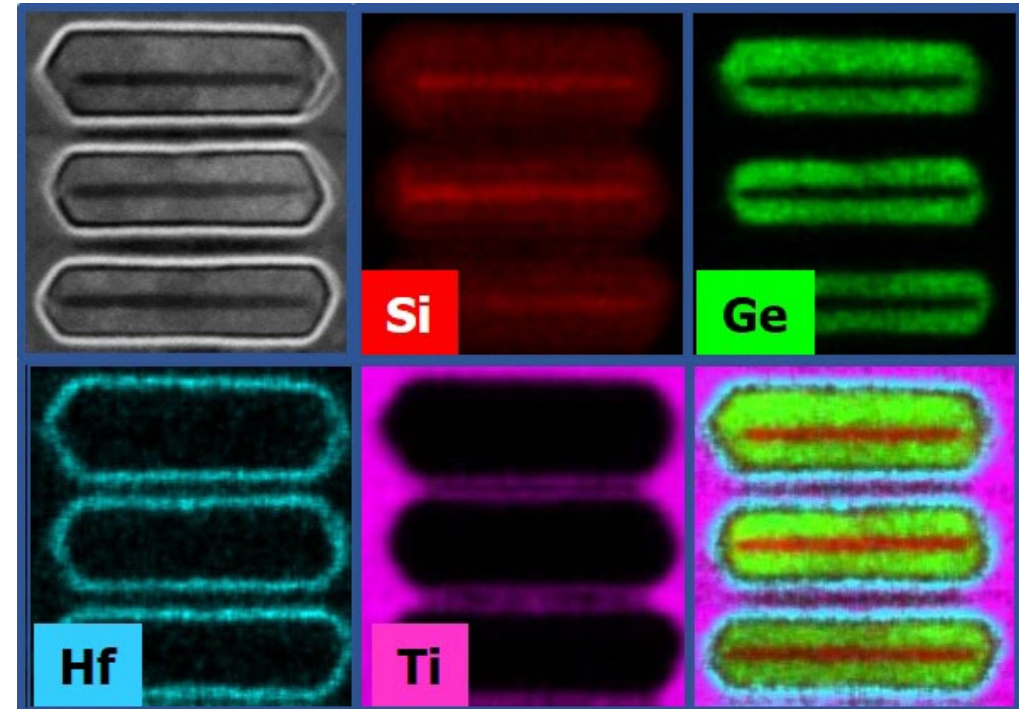
SEM/TEM/STM



PbS nanocrystals as imaged via TEM



IBM STEM EDX image

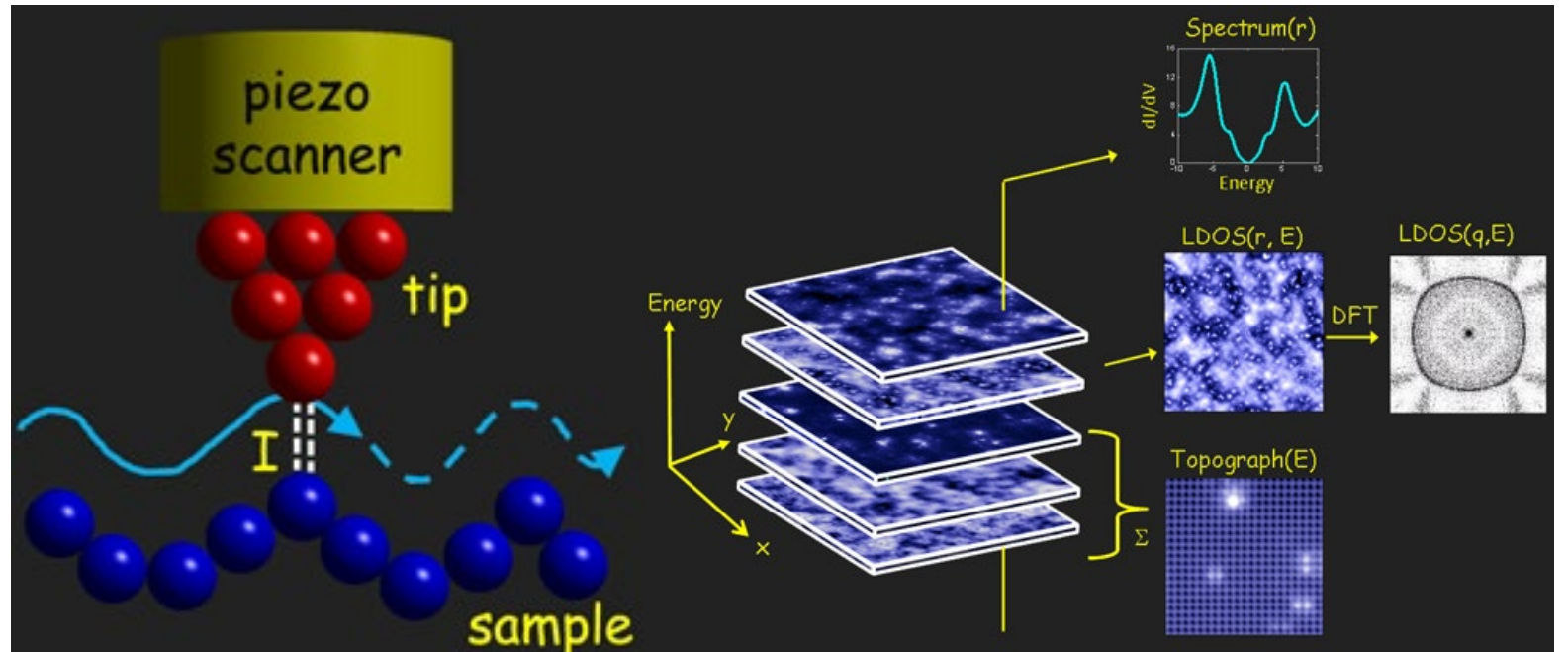


# Nanofabrication

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