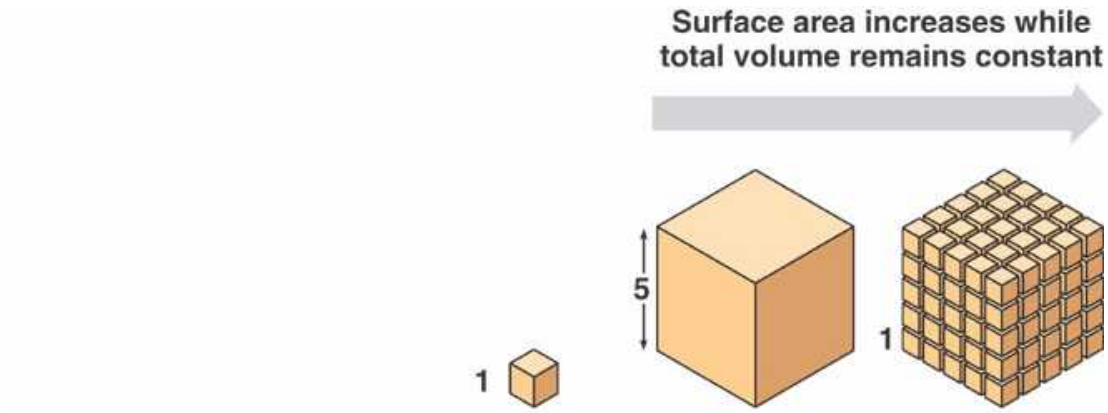
Nanomaterials

- Metals and Alloys
  - Fe, Al, Au
- Semiconductors
  - Band gap, CdS, TiO_2, ZnO
- Ceramic
  - Al_2O_3, Si_3N_4, MgO, , SiO_2, ZrO_2
- Carbon based
  - Diamond, graphite, nanotube, C60, graphene
- Polymers
  - Soft mater, block co-polymer
- Biological
  - Photonic, hydrophobic, adhesive,
- Composites

Surface to Volume Ratio



Total surface area (height × width × number of sides × number of boxes)	6	150	750
Total volume (height × width × length × number of boxes)	1	125	125
Surface-to-volume ratio (surface area / volume)	6	1.2	6

Surface Energy

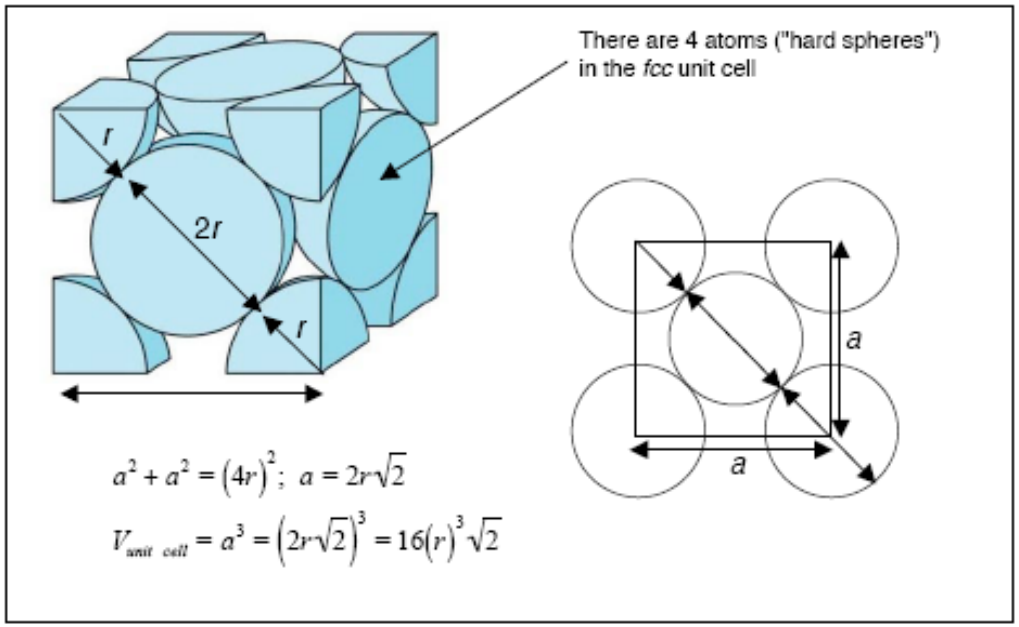
One face surface energy: γ
27 cube: 27 x 6 γ
3 x 9 cube line: 114 γ
3 x (3x3) square: 90 γ
3 x 3 x 3 cube: 54 γ

Surface to Volume Ratio

Au: AAA
Atomic mass: 196.967
Density 19.31
Radii =0.144 nm

Number of Au atoms in 1 m	$3.4\ 10^{9}$
Volume of Au atom	$4.19\ 10^{28}$
Surface area Au atom	$7.22\ 10^{19}$
Surface/volume ratio	$1.72\ 10^{-9}$

fcc



$$V_{unit\ cell} = a^3 = \left(2r\sqrt{2}\right)^3 = 16(0.5\text{nm})^3\sqrt{2} = \mathbf{2.828\ nm^3}$$

$$\frac{10^{27}\ \text{nm}^3}{2.828\ \text{nm}^3} = \mathbf{3.536x10^{26}\ nano\ \ unit\ cells}$$

$$\text{Collective Area} = 3.536x10^{26}\ \text{nano unit cells}\left(\frac{4\ \text{spheres}}{\text{unit cell}}\right)\left(\frac{4\pi r^2}{\text{sphere}}\right) = \mathbf{4.44x10^{27}\ nm^2}$$

$$\frac{S_{spheres}}{S_{unit\ cell}} = \frac{4.44x10^9\ \text{m}^2}{6.0x10^9\ \text{m}^2} = \mathbf{0.74}$$

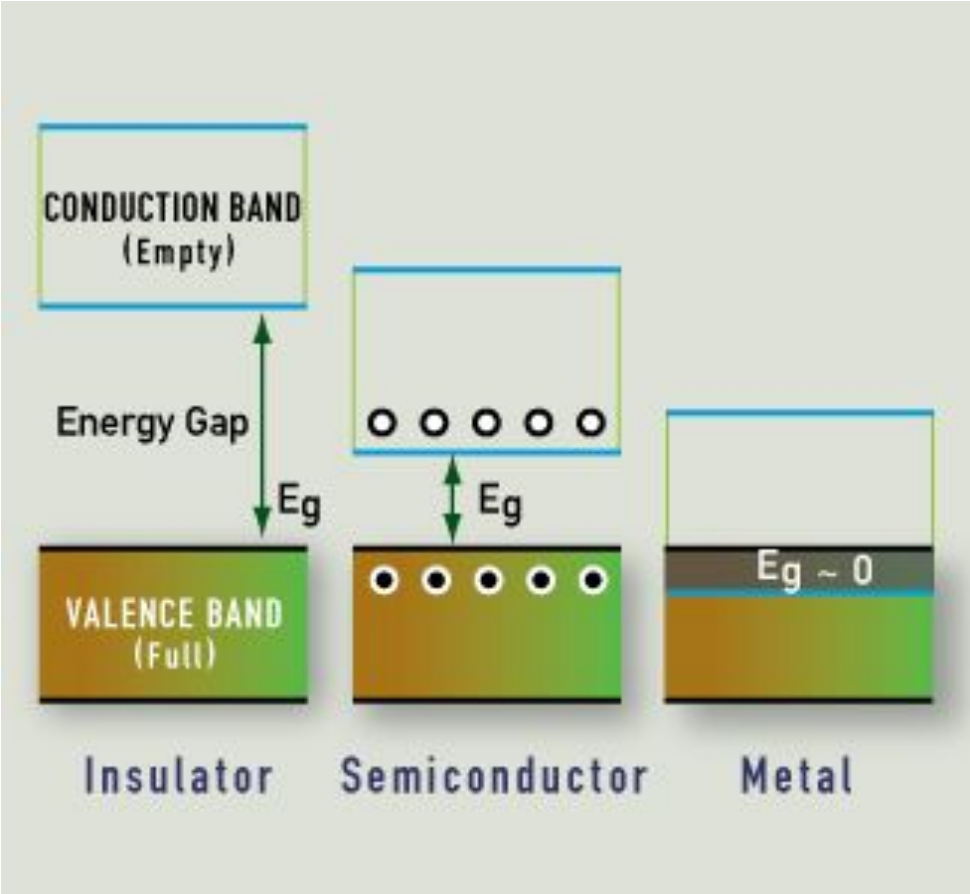
Packing Fraction

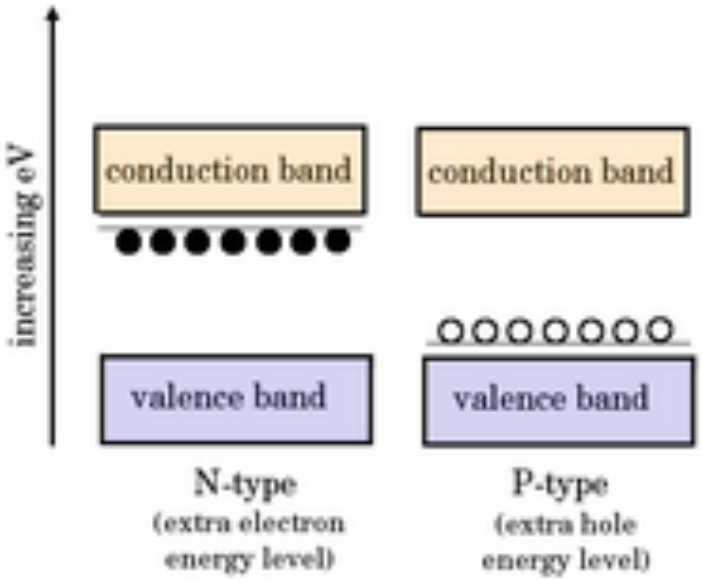
$$\mathrm{APF} = \frac{N_{\mathbf{atoms}} V_{\mathbf{atom}}}{V_{\mathbf{crystal}}}$$

Surfaces

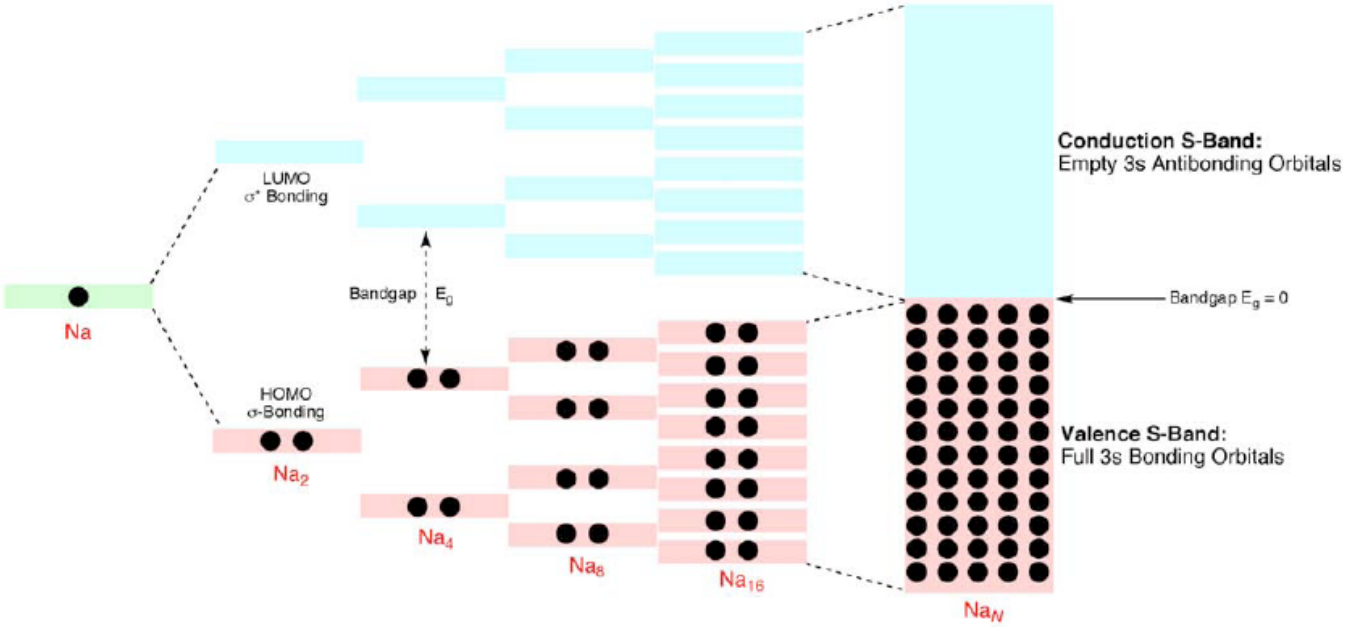
- Collective surface area of nanocube 1 nm
- Porous materials
  - Micropore (<2 nm)
  - Mesopore (2 nm ~ 50 nm)
  - Marcopore (> 50nm)
- Void volume
  - $V_{pore}/V_{material}$

Bandgap

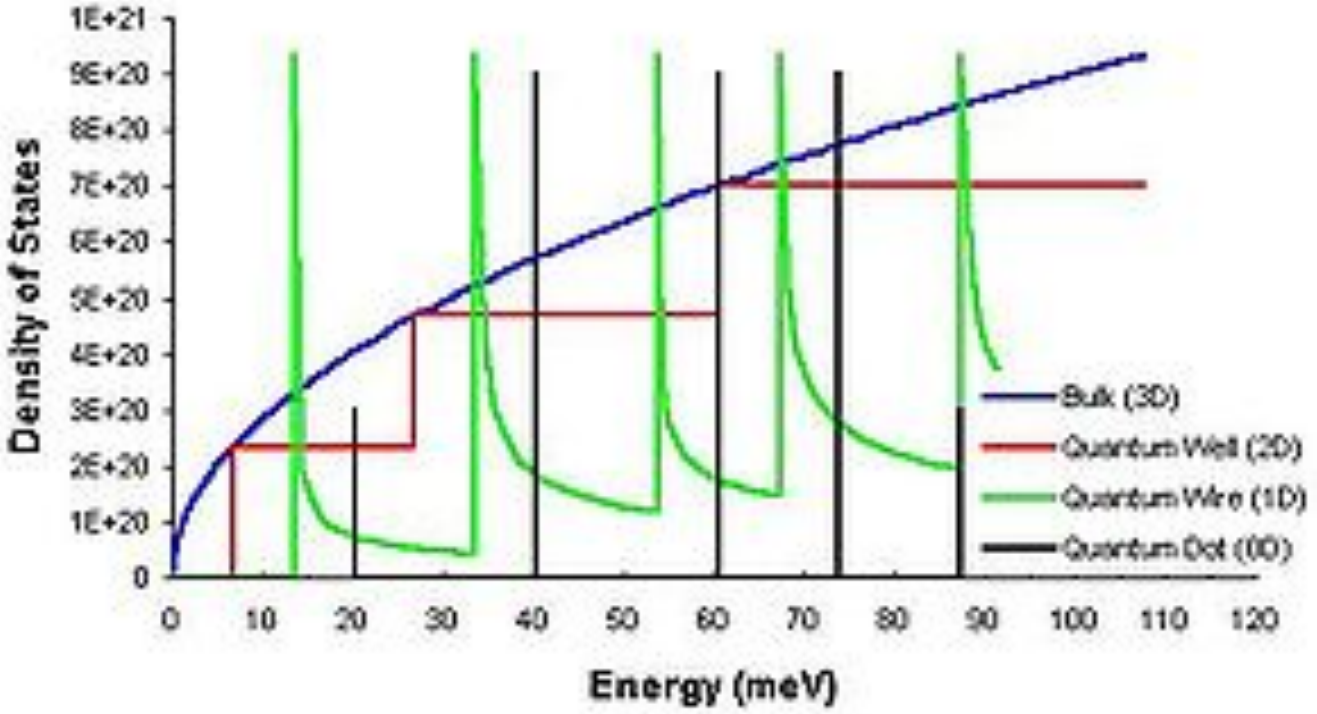

CONDUCTION BAND
(Empty)
Energy Gap
Eg
VALENCE BAND
(Full)
Eg
Eg ~ 0
Insulator
Semiconductor
Metal


increasing eV
conduction band
conduction band
valence band
valence band
N-type
(extra electron
energy level)
P-type
(extra hole
energy level)

Bandgap


LUMO
σ* Bonding
Bandgap E_0
Na
HOMO
σ-Bonding
Na_2
Na_4
Na_8
Na_{16}
Na_N
Conduction S-Band:
Empty 3s Antibonding Orbitals
Bandgap $E_g = 0$
Valence S-Band:
Full 3s Bonding Orbitals

Density of State

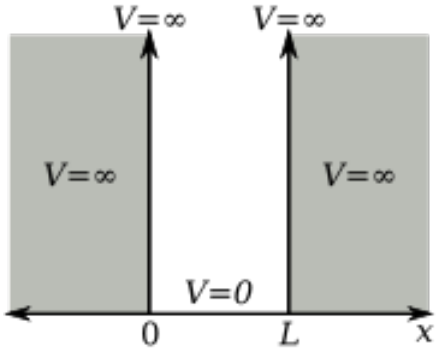


Particle in a Box

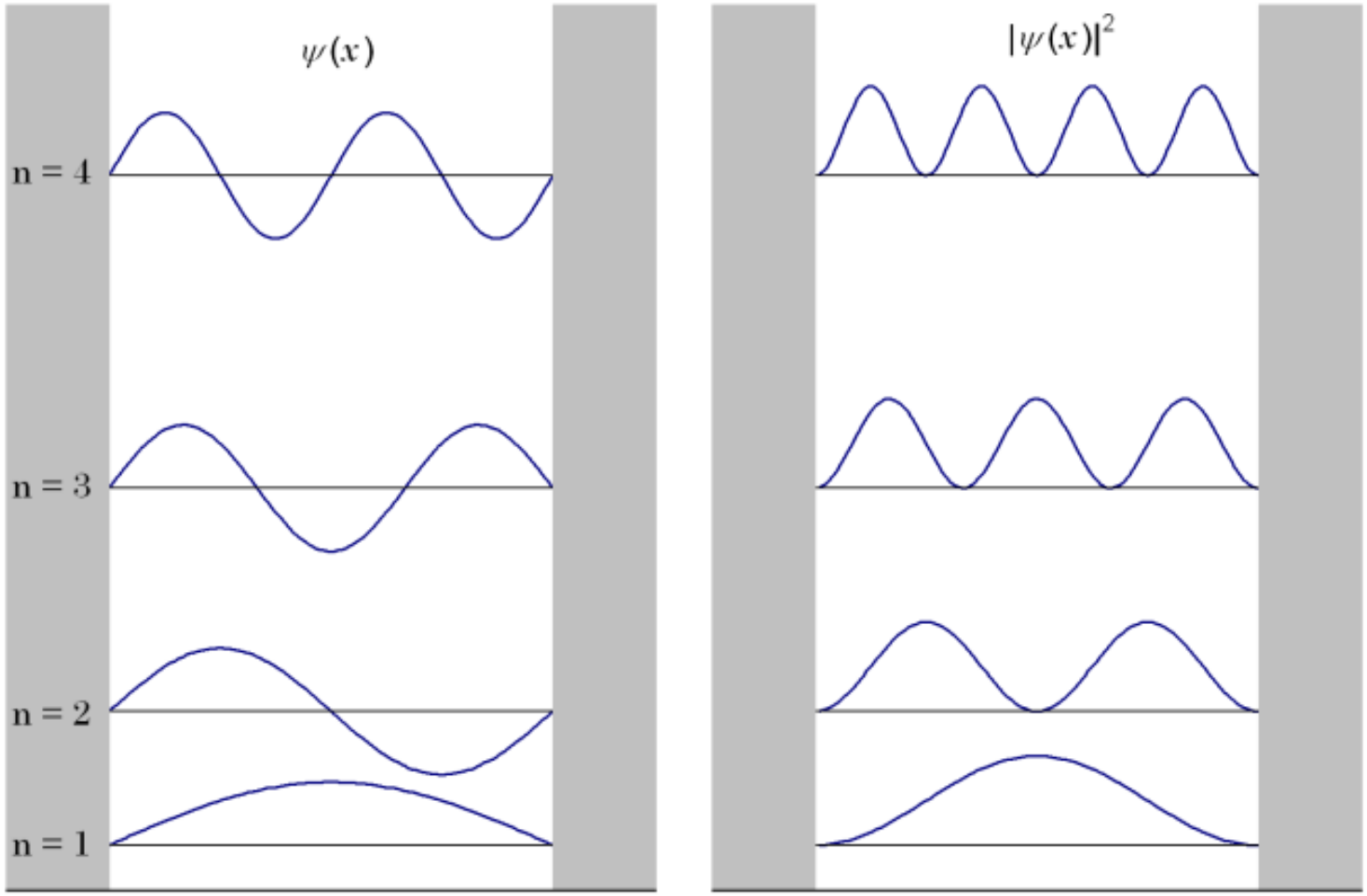
$$-\frac{\hbar^2}{2m}\frac{\mathrm{d}^2\psi(x)}{\mathrm{d}x^2} + V(x)\psi(x) = E\psi(x) \quad (1)$$

$$\psi_n = \sqrt{\frac{2}{L}}\sin\left(\frac{n\pi x}{L}\right)$$

$$E_n = \frac{\hbar^2\pi^2}{2mL^2}n^2$$



Particle in a Box



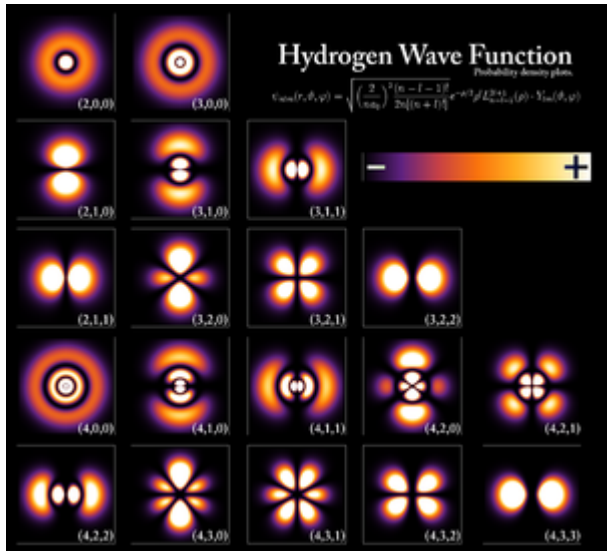
$$\psi_{n_x,n_y} = \sqrt{\frac{4}{L_x L_y}} \sin\left(\frac{n_x \pi x}{L_x}\right) \sin\left(\frac{n_y \pi y}{L_y}\right)$$

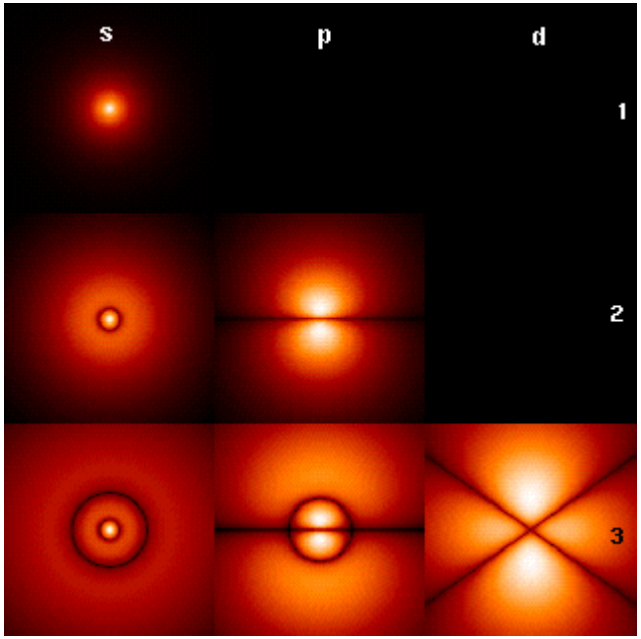
$$E_{n_x,n_y} = \frac{\hbar^2 \pi^2}{2m} \left[\left(\frac{n_x}{L_x}\right)^2 + \left(\frac{n_y}{L_y}\right)^2 \right]$$

$$\psi_{n_x,n_y,n_z} = \sqrt{\frac{8}{L_x L_y L_z}} \sin\left(\frac{n_x \pi x}{L_x}\right) \sin\left(\frac{n_y \pi y}{L_y}\right) \sin\left(\frac{n_z \pi z}{L_z}\right) \quad (22)$$

$$E_{n_x,n_y,n_z} = \frac{\hbar^2 \pi^2}{2m} \left[\left(\frac{n_x}{L_x}\right)^2 + \left(\frac{n_y}{L_y}\right)^2 + \left(\frac{n_z}{L_z}\right)^2 \right] \quad (23)$$

Wave Functions





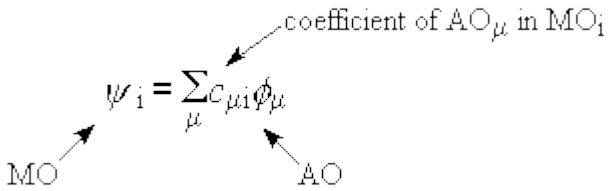
$$i\hbar\frac{\partial}{\partial t}\Psi(\mathbf{r},\,t) = \hat{H}\Psi = \left(-\frac{\hbar^2}{2m}\nabla^2 + V(\mathbf{r})\right)\Psi(\mathbf{r},\,t) = -\frac{\hbar^2}{2m}\nabla^2\Psi(\mathbf{r},\,t) + V(\mathbf{r})\Psi(\mathbf{r},\,t)$$

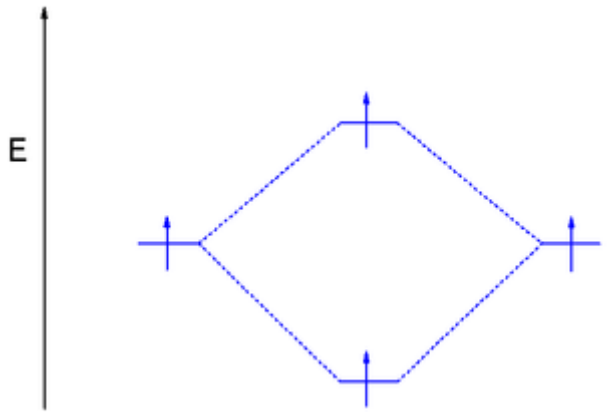
$$V(r) = -\frac{1}{4\pi\epsilon_0}\frac{Ze^2}{r}$$

$$\psi_{n\ell m}(r,\vartheta,\varphi) = \sqrt{\left(\frac{2}{na_0}\right)^3\frac{(n-\ell-1)!}{2n(n+\ell)!}}e^{-\rho/2}\rho^\ell L_{n-\ell-1}^{2\ell+1}(\rho)\cdot Y_\ell^m(\vartheta,\varphi)$$

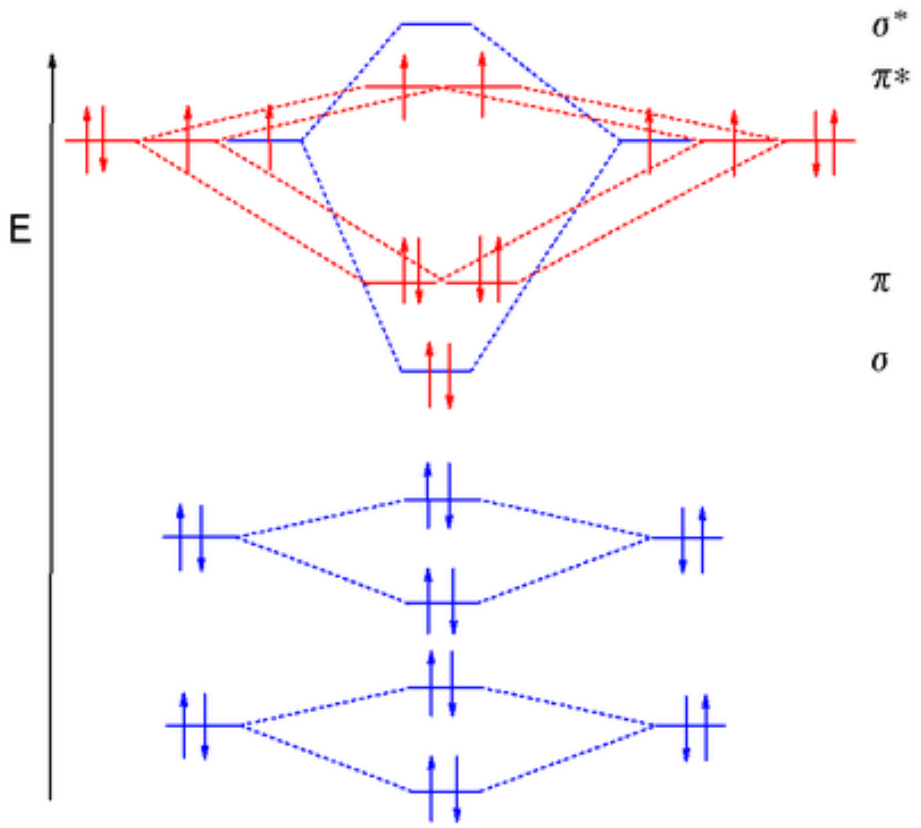
Linear combination of atomic orbitals molecular orbital method

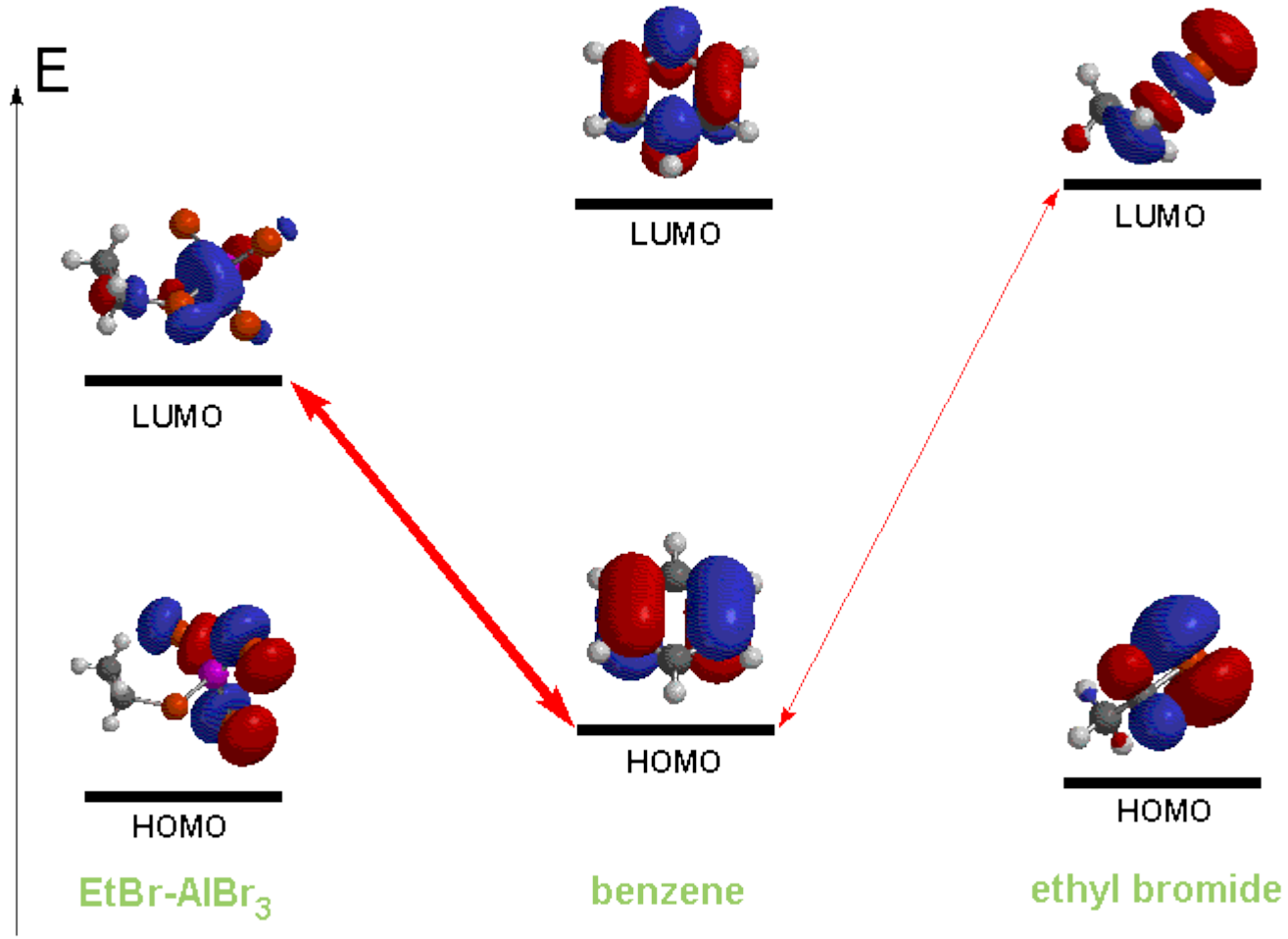
$$\phi_i = c_{1i}\chi_1 + c_{2i}\chi_2 + c_{3i}\chi_3 + \cdots + c_{ni}\chi_n$$

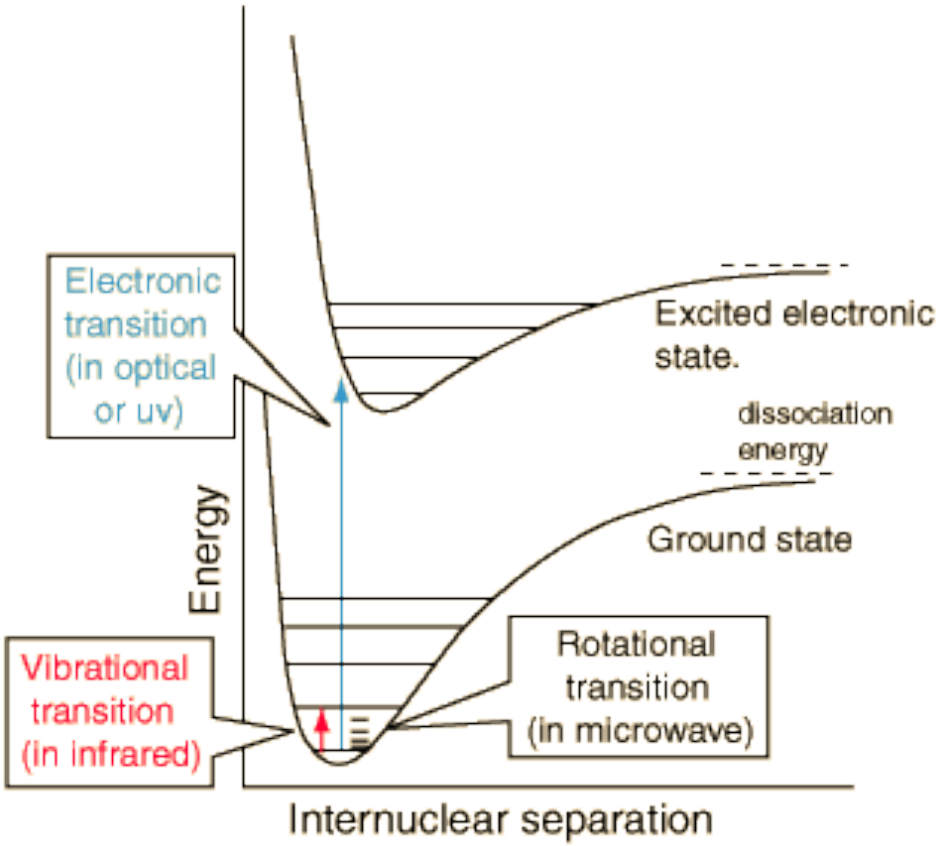




Oxygen




E
LUMO
LUMO
LUMO
HOMO
HOMO
HOMO
EtBr-AlBr3
benzene
ethyl bromide


Electronic transition (in optical or uv)
Excited electronic state.
dissociation energy
Ground state
Energy
Vibrational transition (in infrared)
Rotational transition (in microwave)
Internuclear separation

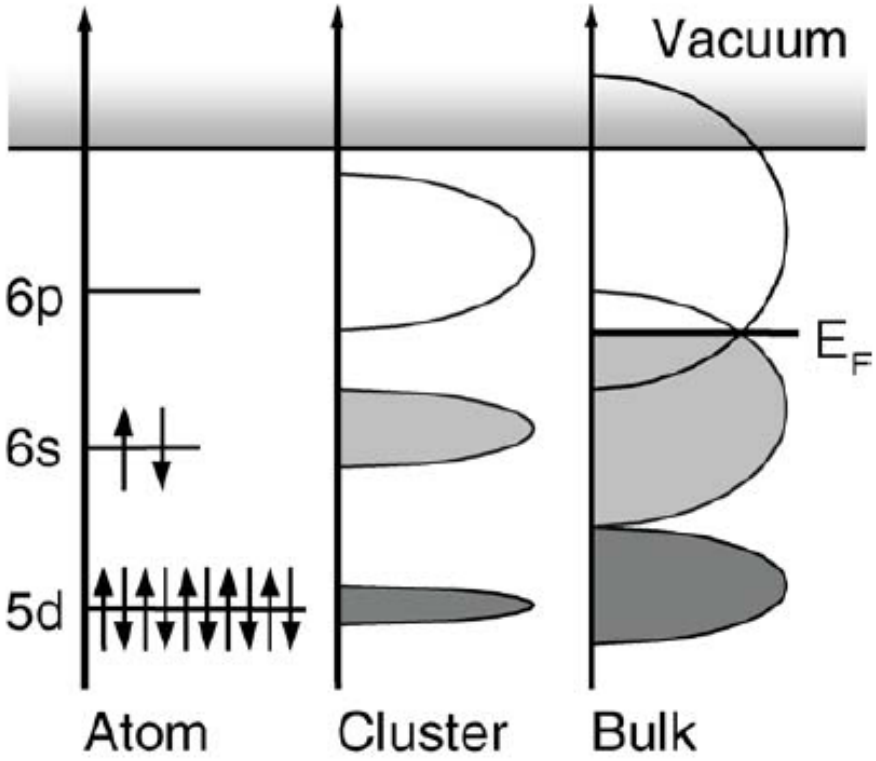


Figure 5 Energy diagram describing a generic Bloch-Wilson MIT in clusters (with specific reference to the energy levels of mercury). For sufficiently large clusters, the *s-p* band gap closes with increasing cluster size (shaded areas represent energy range with occupied electron levels). Overlap leads to a "continuous" DOS at E_F and to an Insulator to Metal transition.

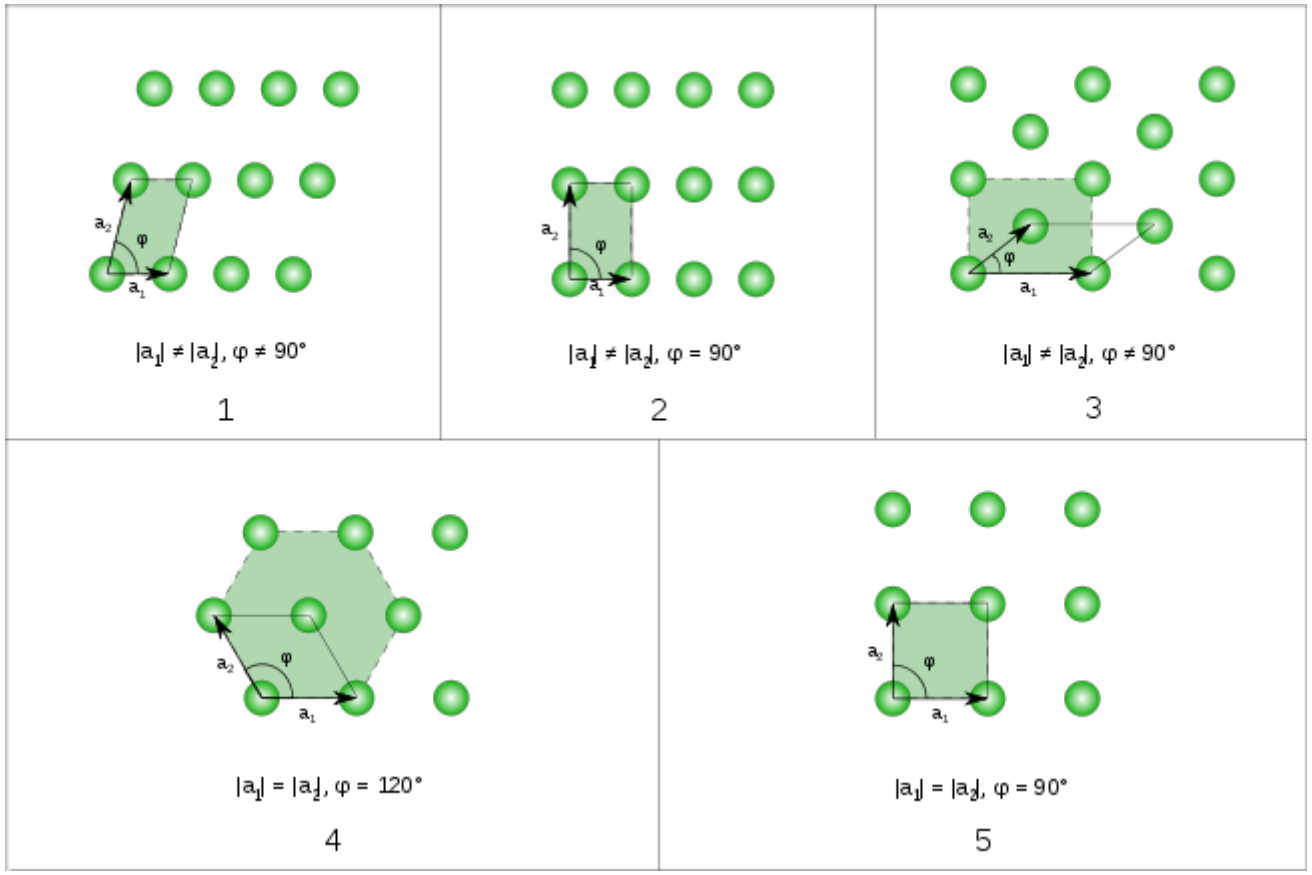
Bloch wave

$$\psi_{n\mathbf{k}}(\mathbf{r}) = e^{i\mathbf{k}\cdot\mathbf{r}} u_{n\mathbf{k}}(\mathbf{r})$$

A **Bloch wave** or **Bloch state**, named after Felix Bloch, is the wavefunction of a particle (usually, an electron) placed in a periodic potential.

$\epsilon n(\mathbf{k}) = \epsilon n(\mathbf{k} + \mathbf{K})$,

The five fundamental two-dimensional Bravais lattices



Unit Cell

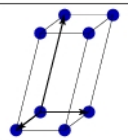
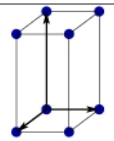
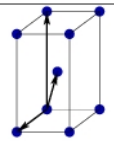
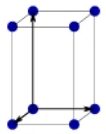
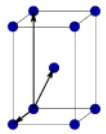
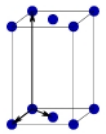
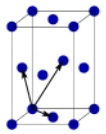
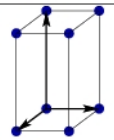
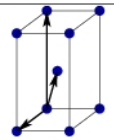
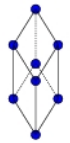
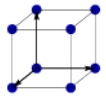
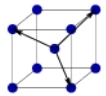
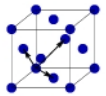
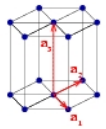
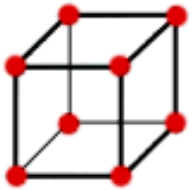
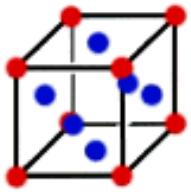
Bravais lattice	Parameters	Simple (P)	Volume centered (I)	Base centered (C)	Face centered (F)
Triclinic	$a_1 \neq a_2 \neq a_3$ $\alpha_{12} \neq \alpha_{23} \neq \alpha_{31}$				
Monoclinic	$a_1 \neq a_2 \neq a_3$ $\alpha_{23} = \alpha_{31} = 90°$ $\alpha_{12} \neq 90°$				
Orthorhombic	$a_1 \neq a_2 \neq a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90°$				
Tetragonal	$a_1 = a_2 \neq a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90°$				
Trigonal	$a_1 = a_2 = a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} < 120°$				
Cubic	$a_1 = a_2 = a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90°$				
Hexagonal	$a_1 = a_2 \neq a_3$ $\alpha_{12} = 120°$ $\alpha_{23} = \alpha_{31} = 90°$				

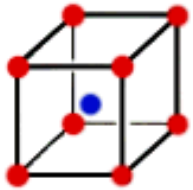
Table 1.1: Bravais lattices in three-dimensions.



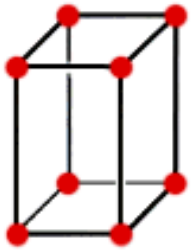
Simple cubic



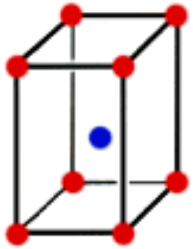
Face-centered cubic



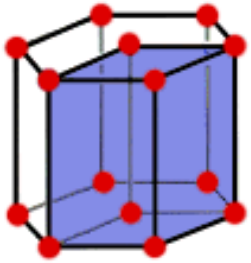
Body-centered cubic



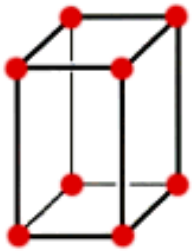
Simple tetragonal



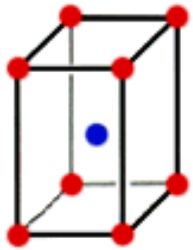
Body-centered tetragonal



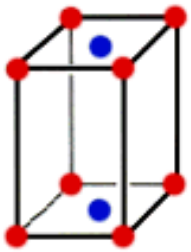
Hexagonal



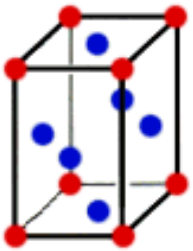
Simple orthorhombic



Body-centered orthorhombic

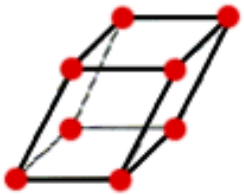


Base-centered orthorhombic

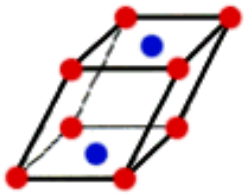


Face-centered orthorhombic

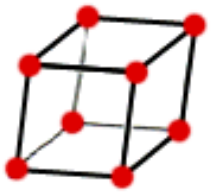
Rhombohedral



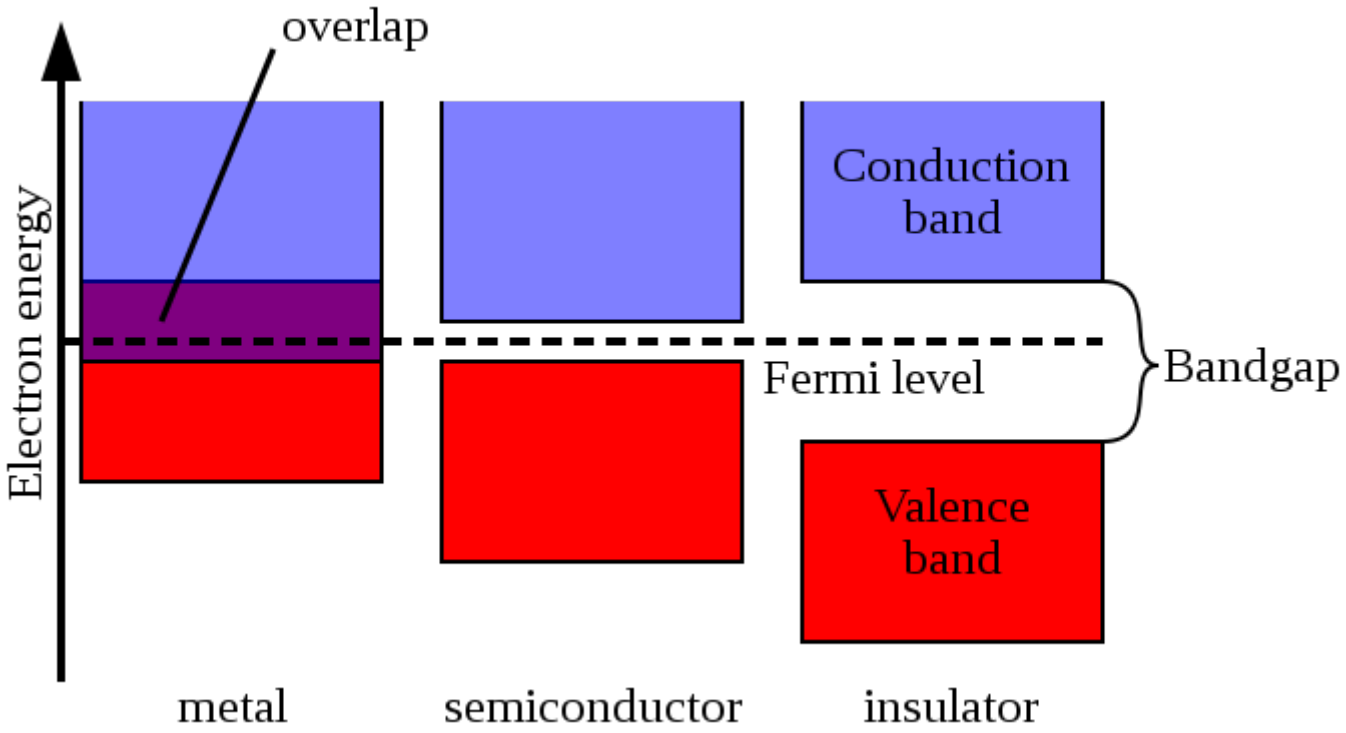
Simple Monoclinic



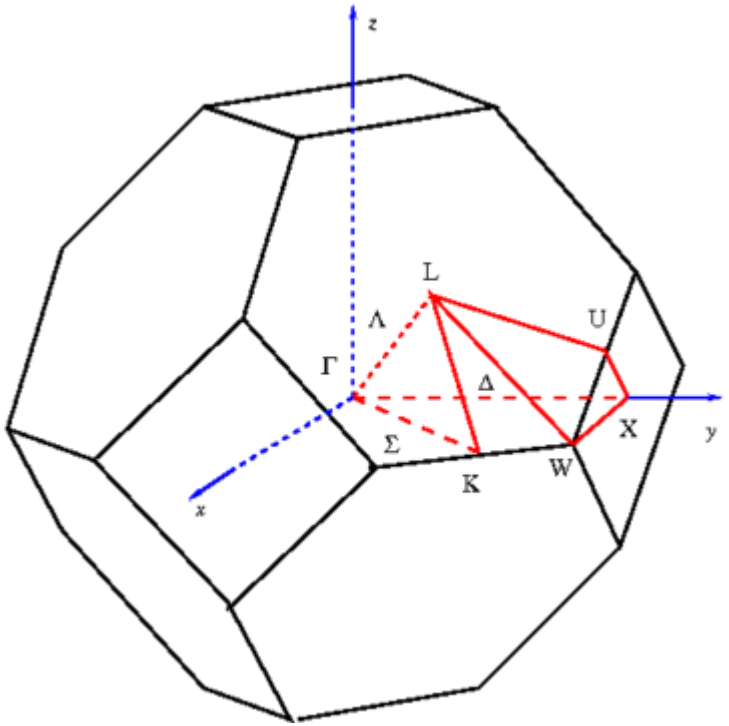
Base-centered monoclinic



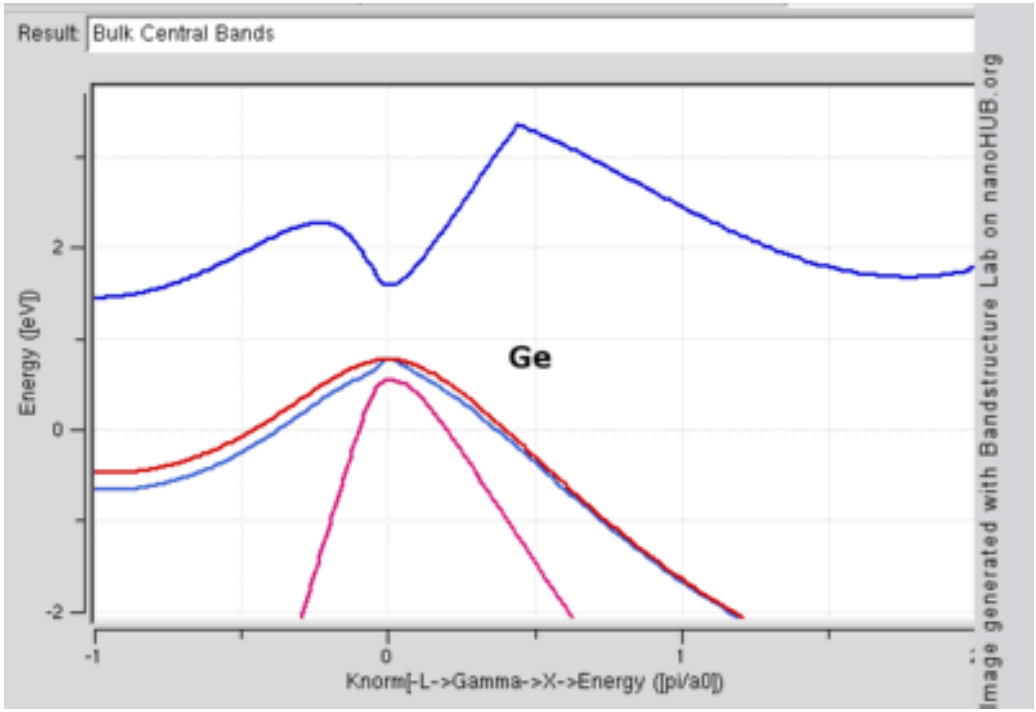
Triclinic


overlap
Electron energy
Conduction band
Fermi level
Bandgap
Valence band
metal
semiconductor
insulator

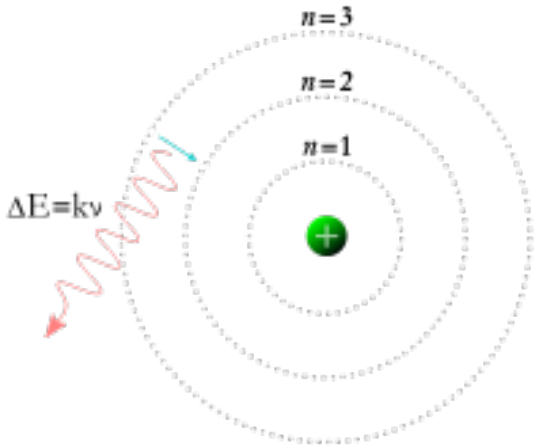
First Brillouin zone of FCC lattice showing symmetry labels

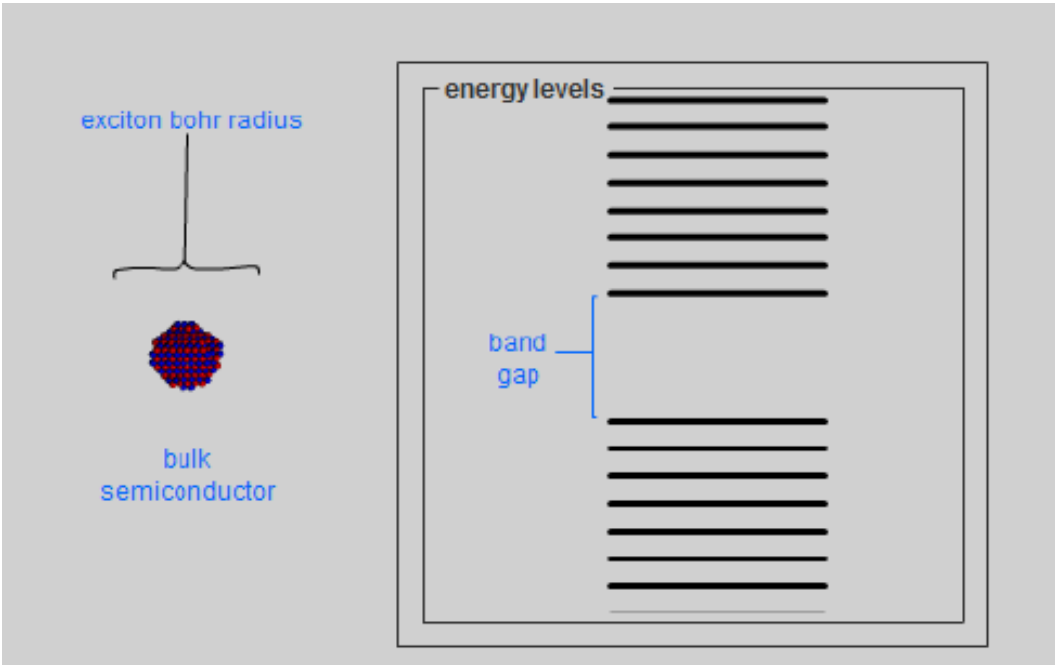


Band Structures

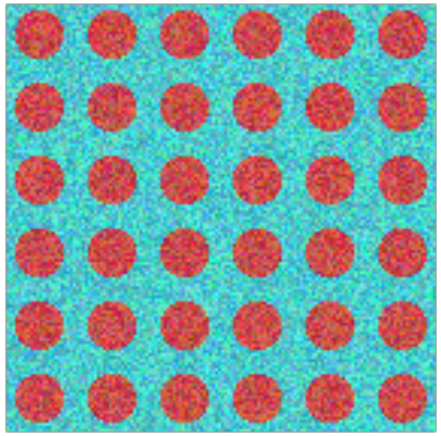


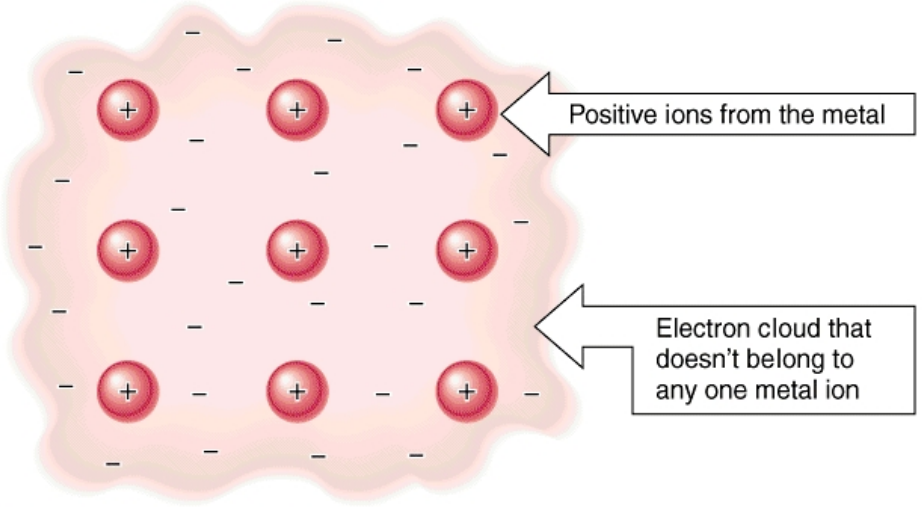
Bohr Exciton Radius





Electron Sea

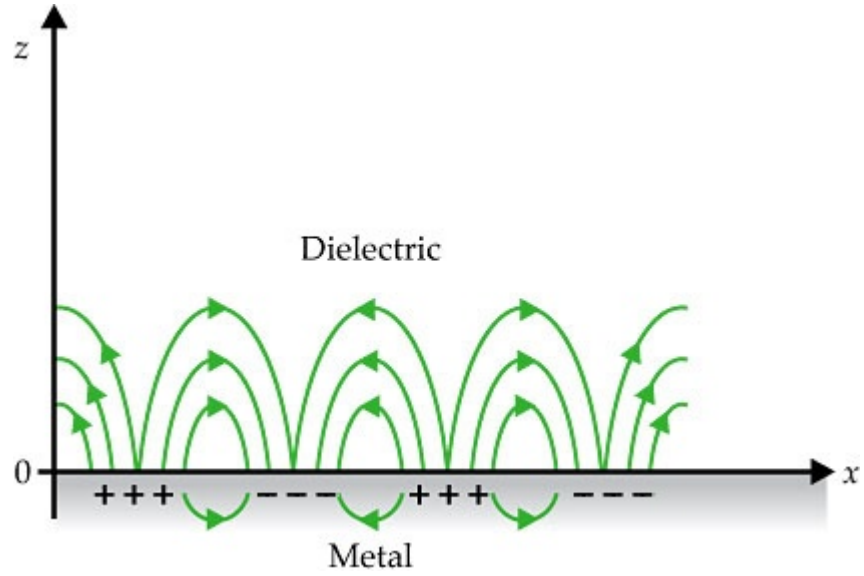




$$m\frac{d^2\delta x}{dt^2} = e\,E_x = -m\,{\omega_p}^2\,\delta x,$$

$${\omega_p}^2 = \frac{n\,e^2}{\epsilon_0\,m},$$

Surface Plasmonon



$$\varepsilon_m = 1 - \frac{\omega_p^2}{\omega^2}$$

TiO_2

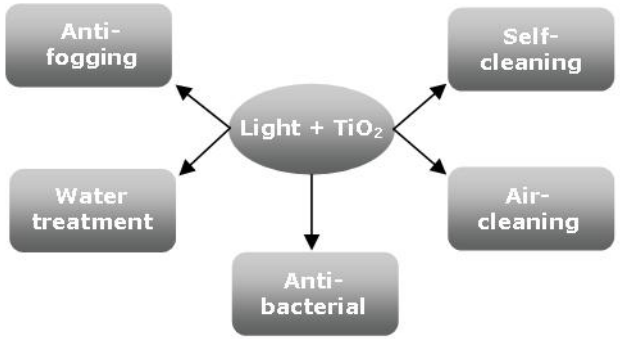
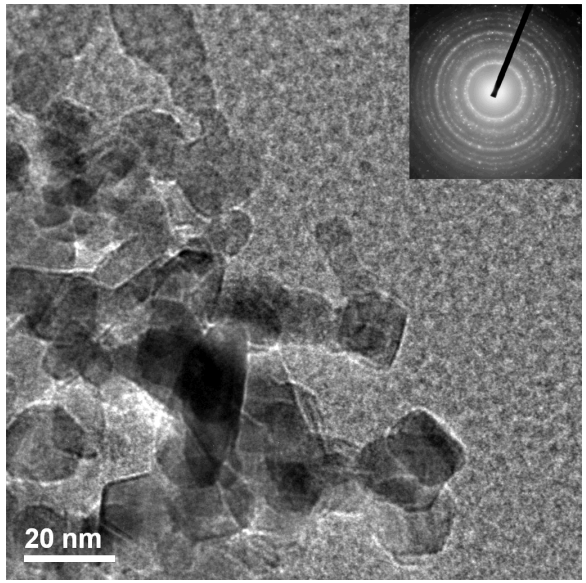
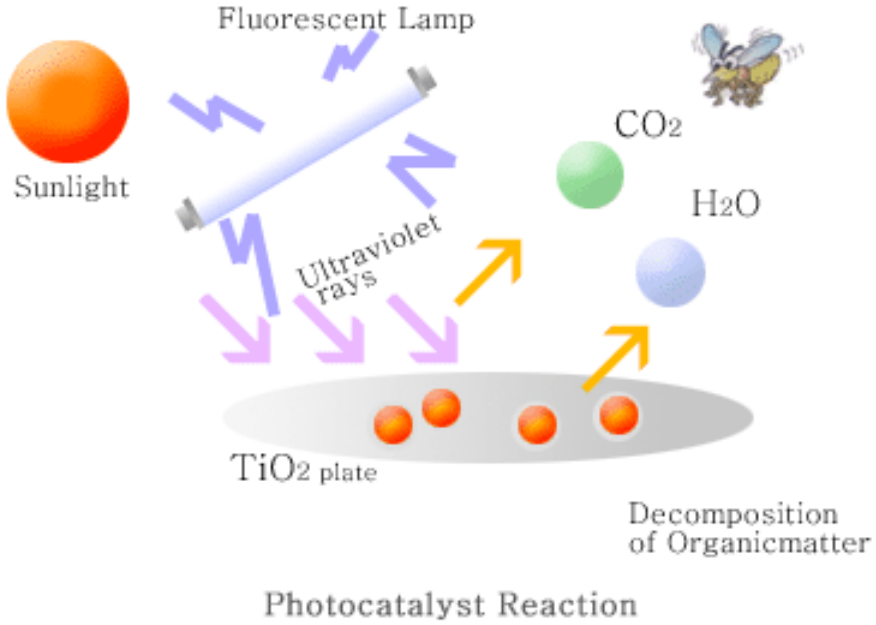
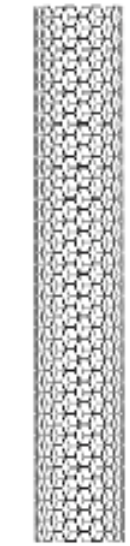


Figure 1. Major areas of activity in titanium dioxide photocatalysis

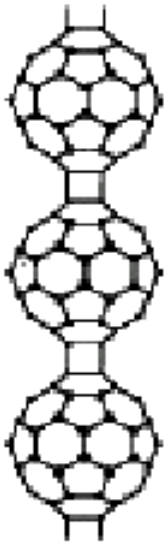




Carbon



SWNT

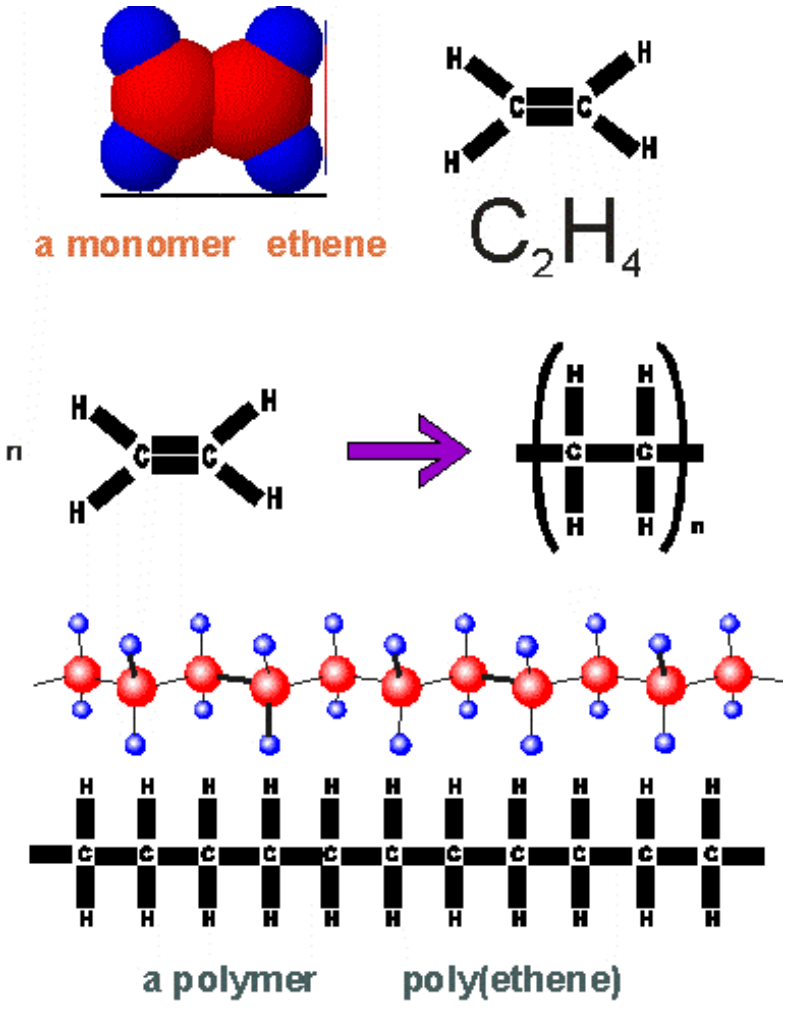


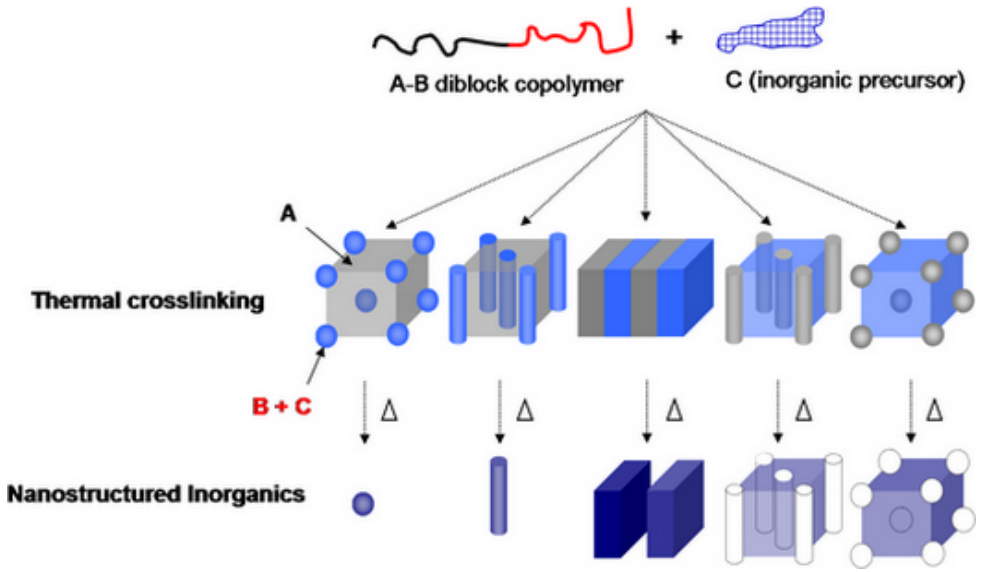
Poly-C_{60}

C_{60}

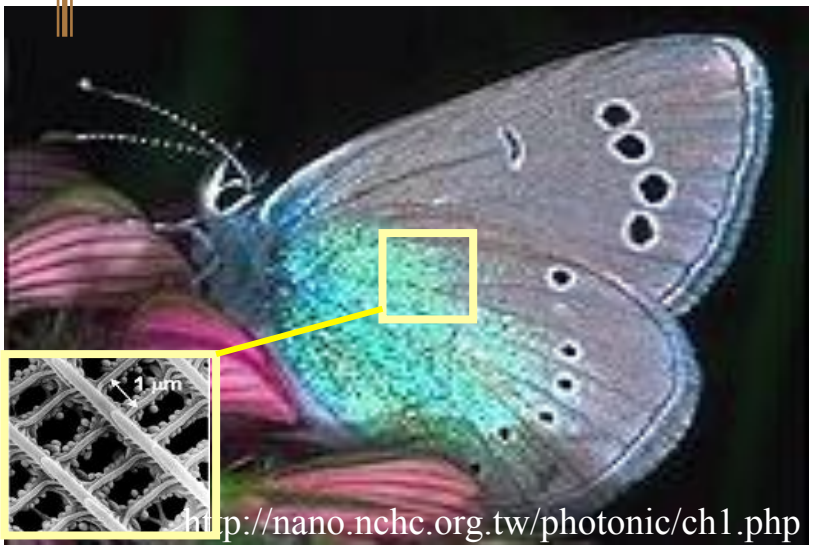
Nanodiamond
~ 2-10 nm

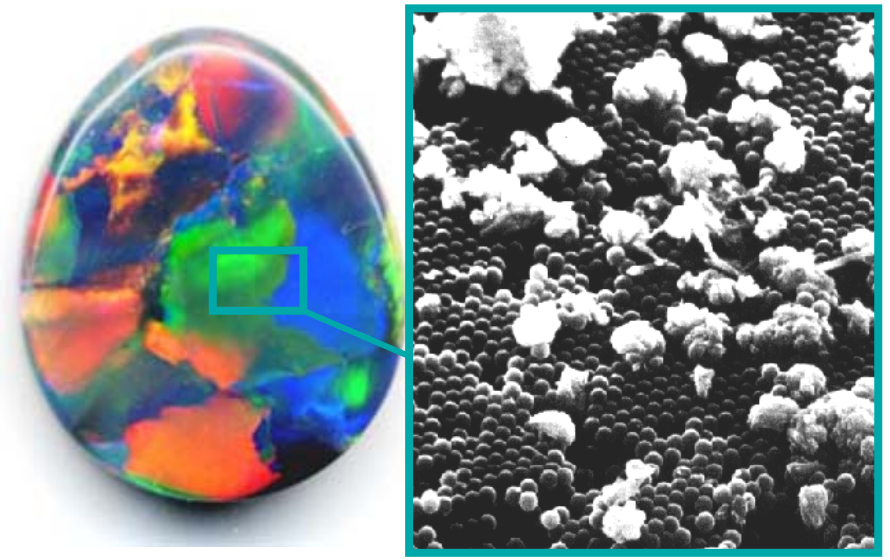
Polymer

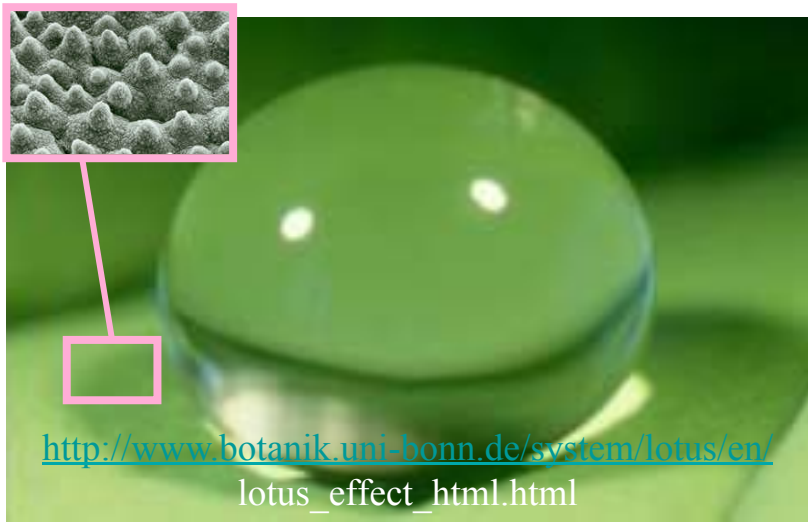

a monomer ethene
C_2H_4
n
a polymer poly(ethene)

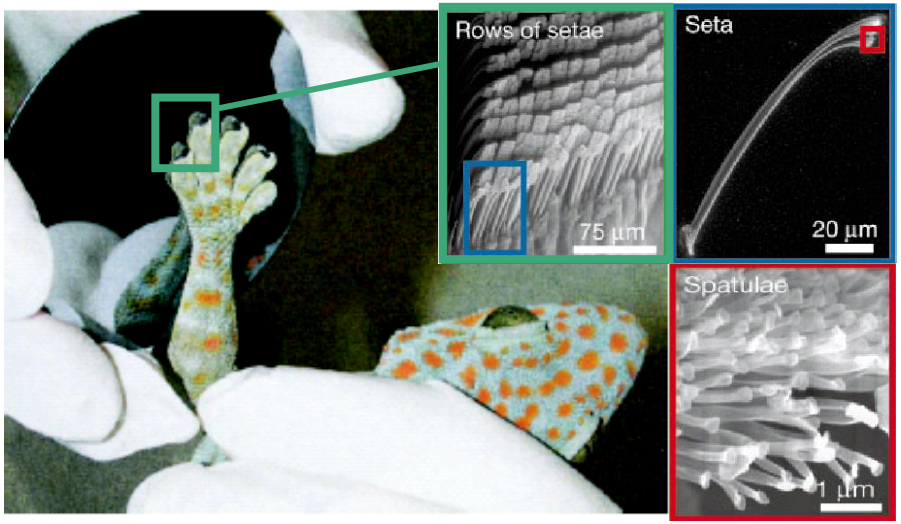

A-B diblock copolymer
C (inorganic precursor)
A
Thermal crosslinking
B + C
Δ
Nanostructured Inorganics

Nature Materials

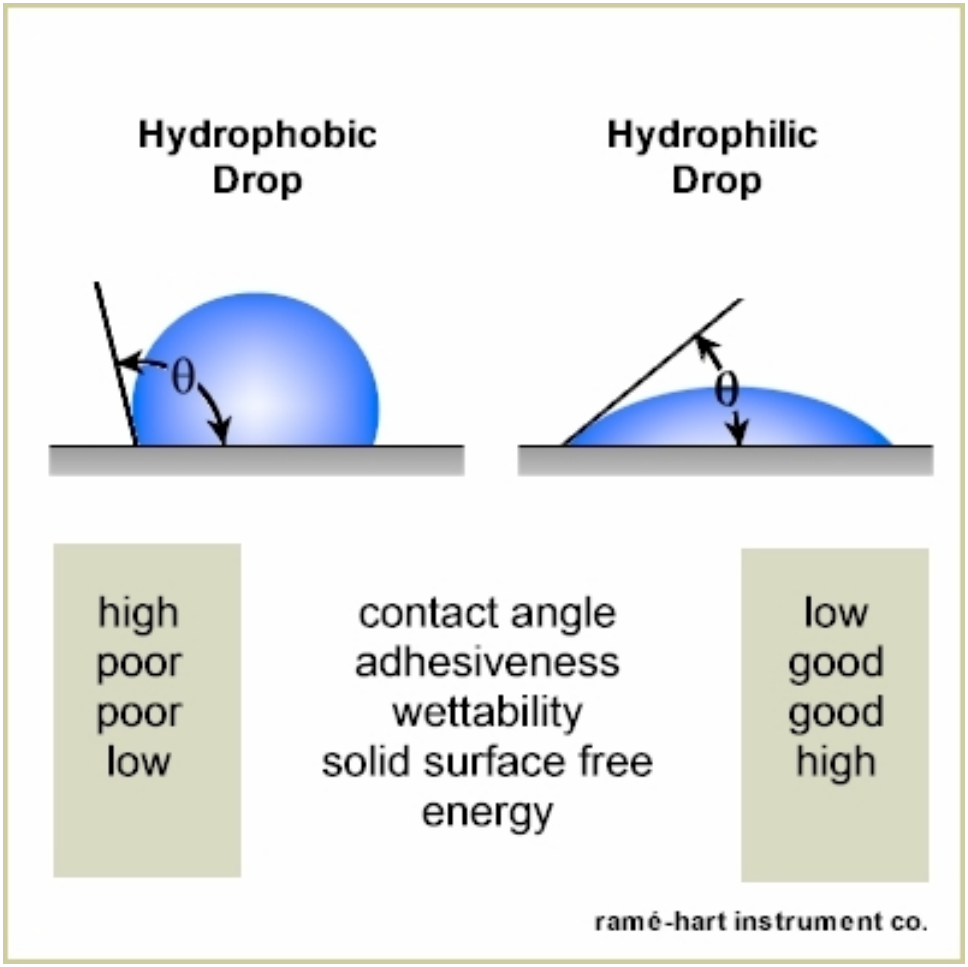






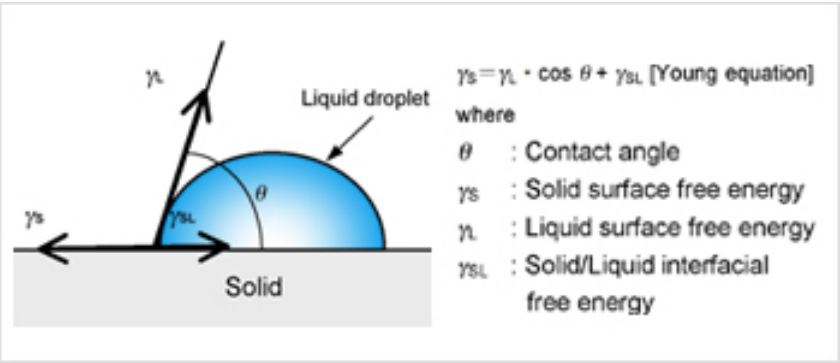


Contact Angle



Young's Equation

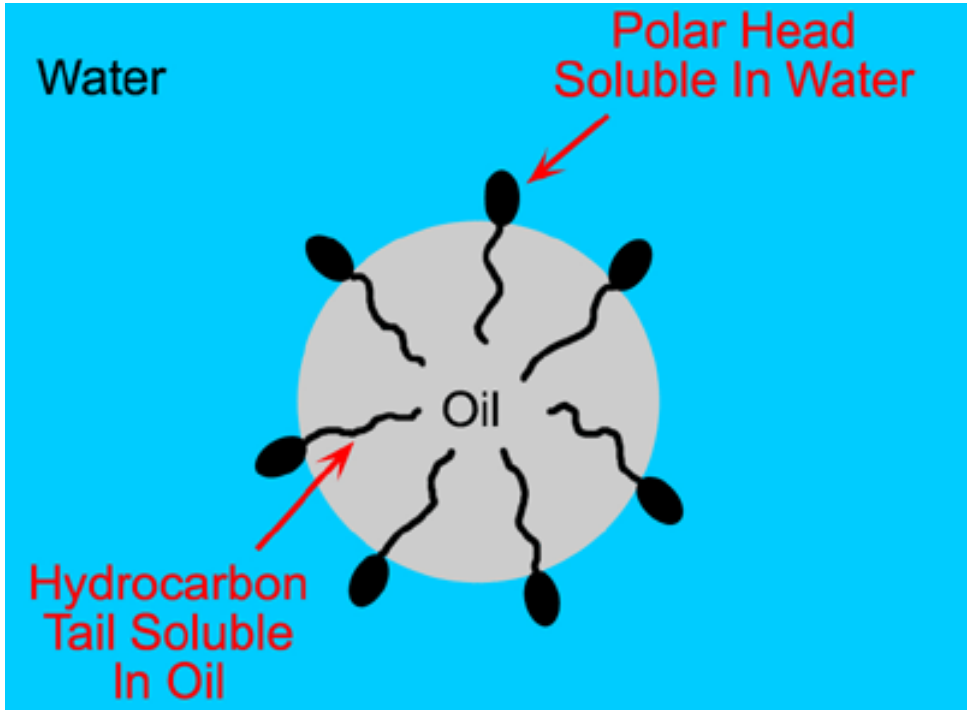
$$\gamma_{SL} + \gamma_{LV} \cos\theta_c = \gamma_{SV}$$



Surface Energy Minimization

- Surfactants
- DLVO
- Polymeric
- Nucleation
- Ostwald Ripening
- Sintering
- Restructure

Surfactant


Water
Polar Head
Soluble In Water
Oil
Hydrocarbon
Tail Soluble
In Oil

DLVO Theory

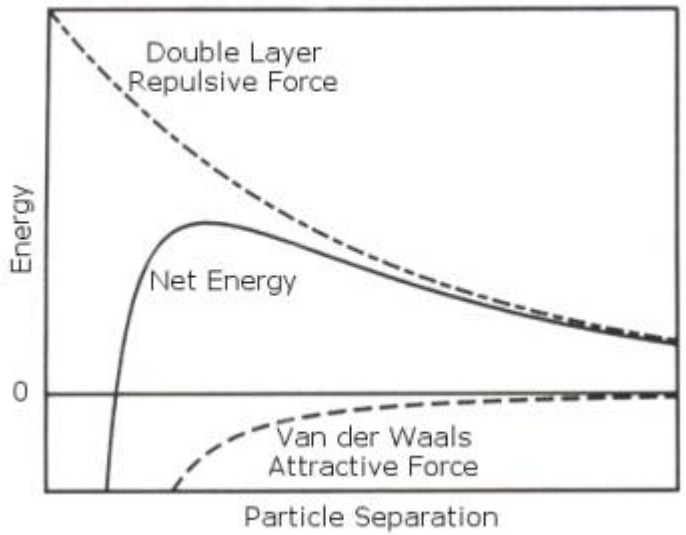
$$V_T = V_A + V_R + V_S$$

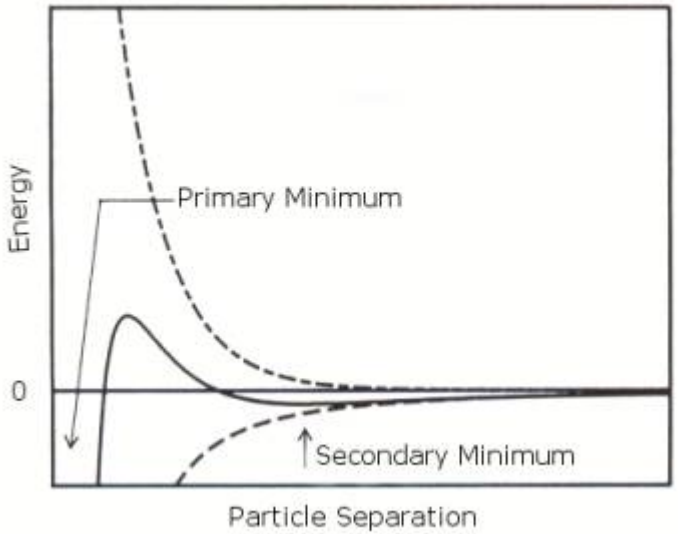
$$V_A = -A/(12 \pi D^2)$$

A is the Hamaker constant and D is the particle separation

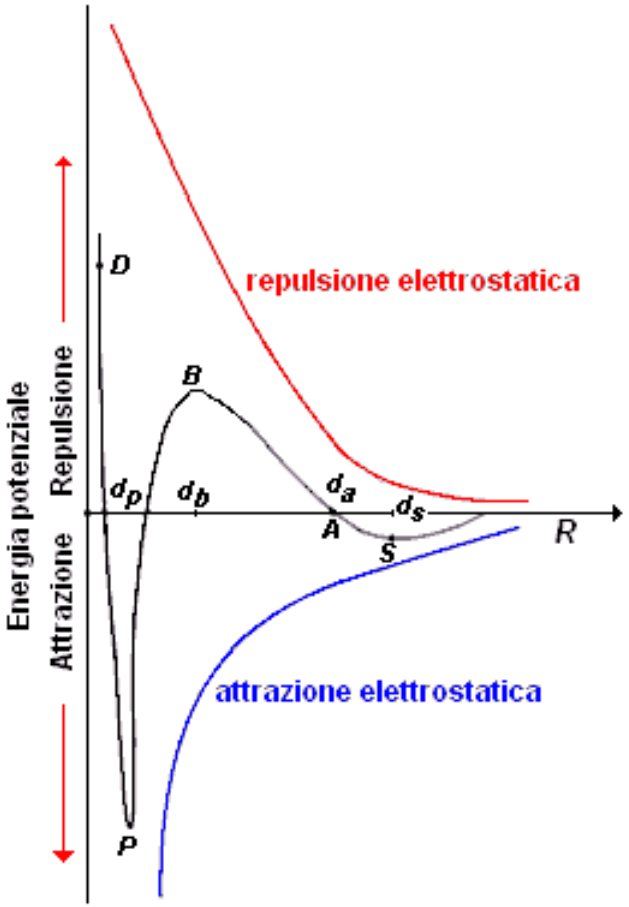
$$V_R = 2 \pi \varepsilon a \xi^2 \exp(- \kappa D)$$

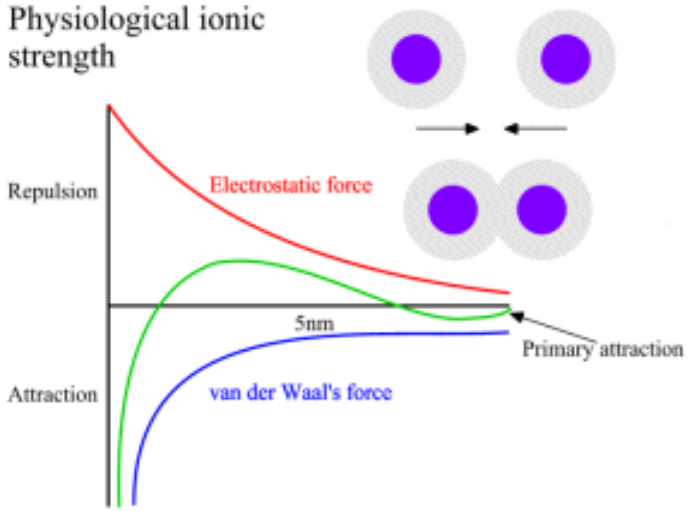
a is the particle radius, π is the solvent permeability,
κ is a function of the ionic composition and ξ is the zeta potential

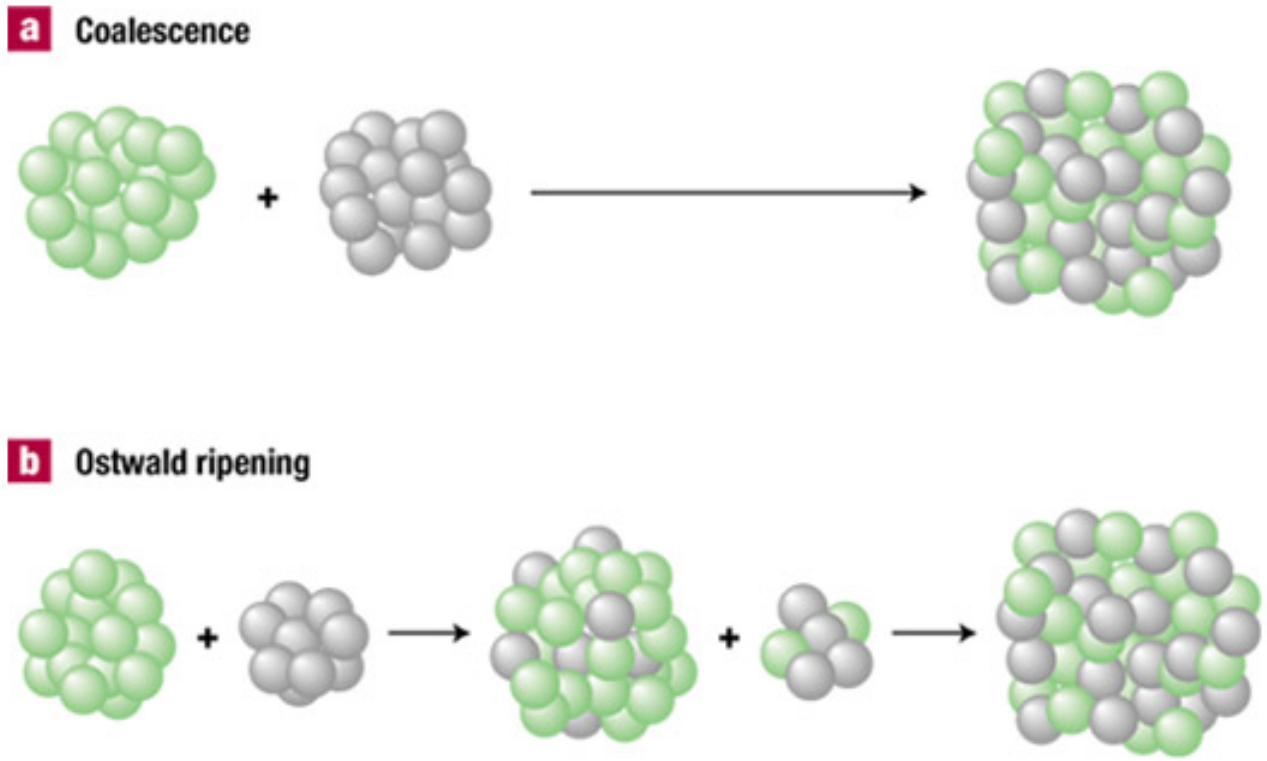

Double Layer
Repulsive Force
Energy
Net Energy
0
Van der Waals
Attractive Force
Particle Separation


Energy
Primary Minimum
0
Secondary Minimum
Particle Separation

DLVO Theory


Energia potenziale
Repulsione
Attrazione
D
B
A
S
P
R
d_p
d_b
d_a
d_s
repulsione elettrostatica
attrazione elettrostatica


Physiological ionic strength
Repulsion
Attraction
Electrostatic force
van der Waal's force
5nm
Primary attraction



Two main mechanisms are shown here: **a**, coalescence sintering, and **b**, Ostwald ripening sintering. Coalescence sintering occurs when two clusters touch or collide and merge to form one bigger cluster. In contrast, Ostwald ripening sintering occurs by evaporation of atoms from one cluster, which then transfer to another. This is a dynamic process — both clusters exchange atoms, but the rate of loss from the smaller cluster is higher, because of the lower average coordination of atoms at the surface and their relative ease of removal. Thus big clusters get bigger at the expense of smaller clusters, which shrink and eventually disappear. The latter process is the usual form of sintering for metal clusters on a supported surface that are well spaced apart, although coalescence can occur for a high density of clusters. In general, the presence of the surface results in SMORS (surface-mediated Ostwald ripening sintering) in which material is transferred from one cluster to another by diffusion across the surface, and not through the gas phase.