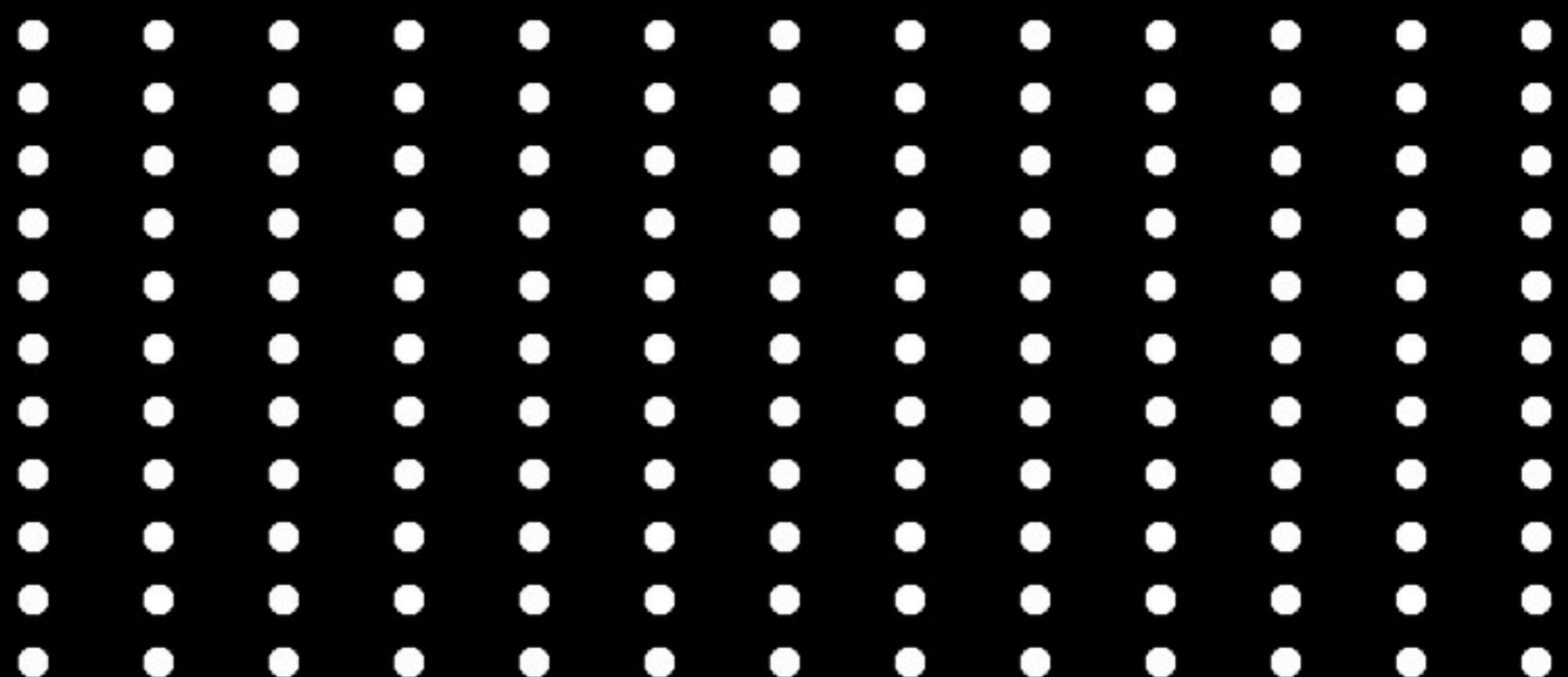


# Chapter 3

## Imaging Modes

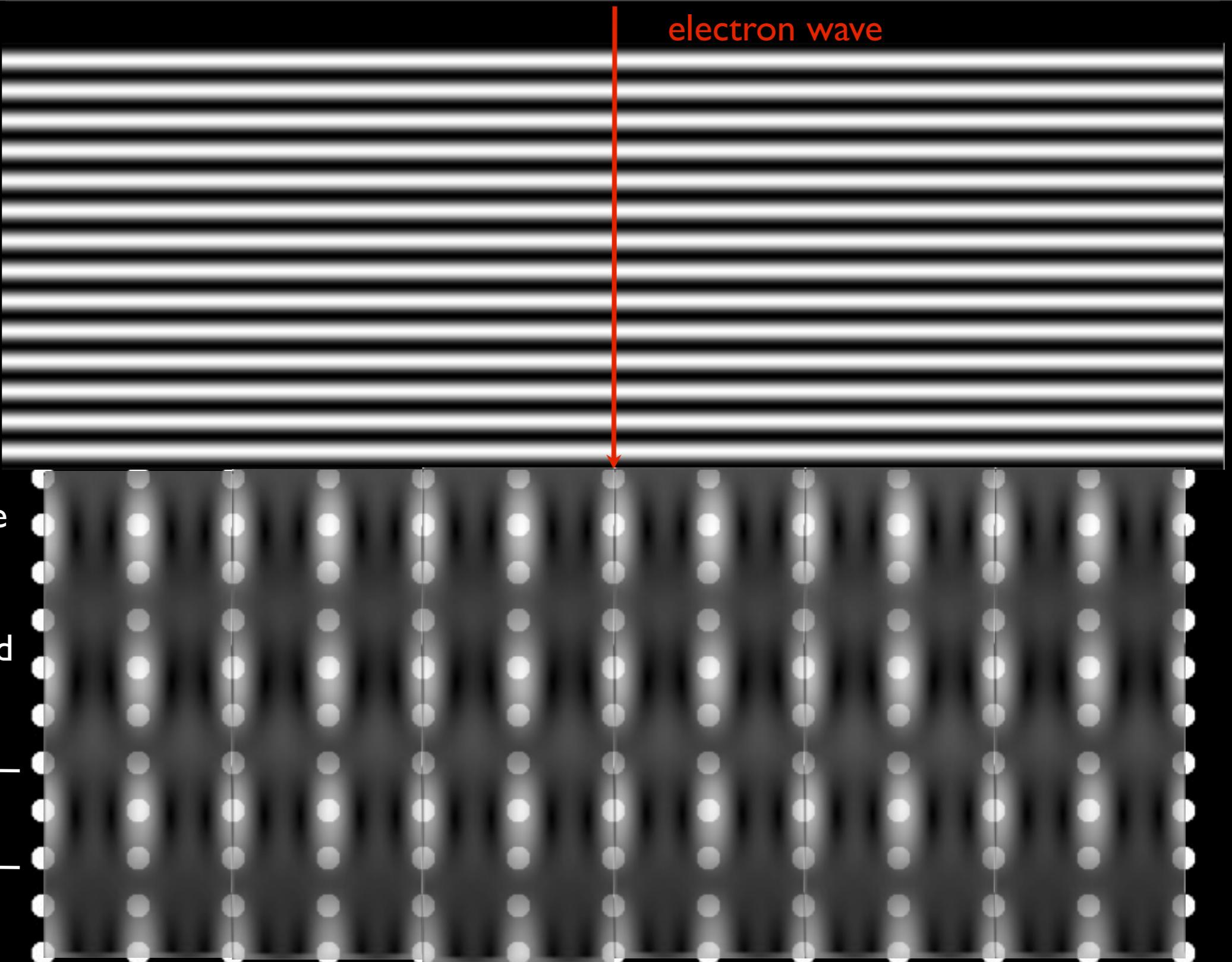


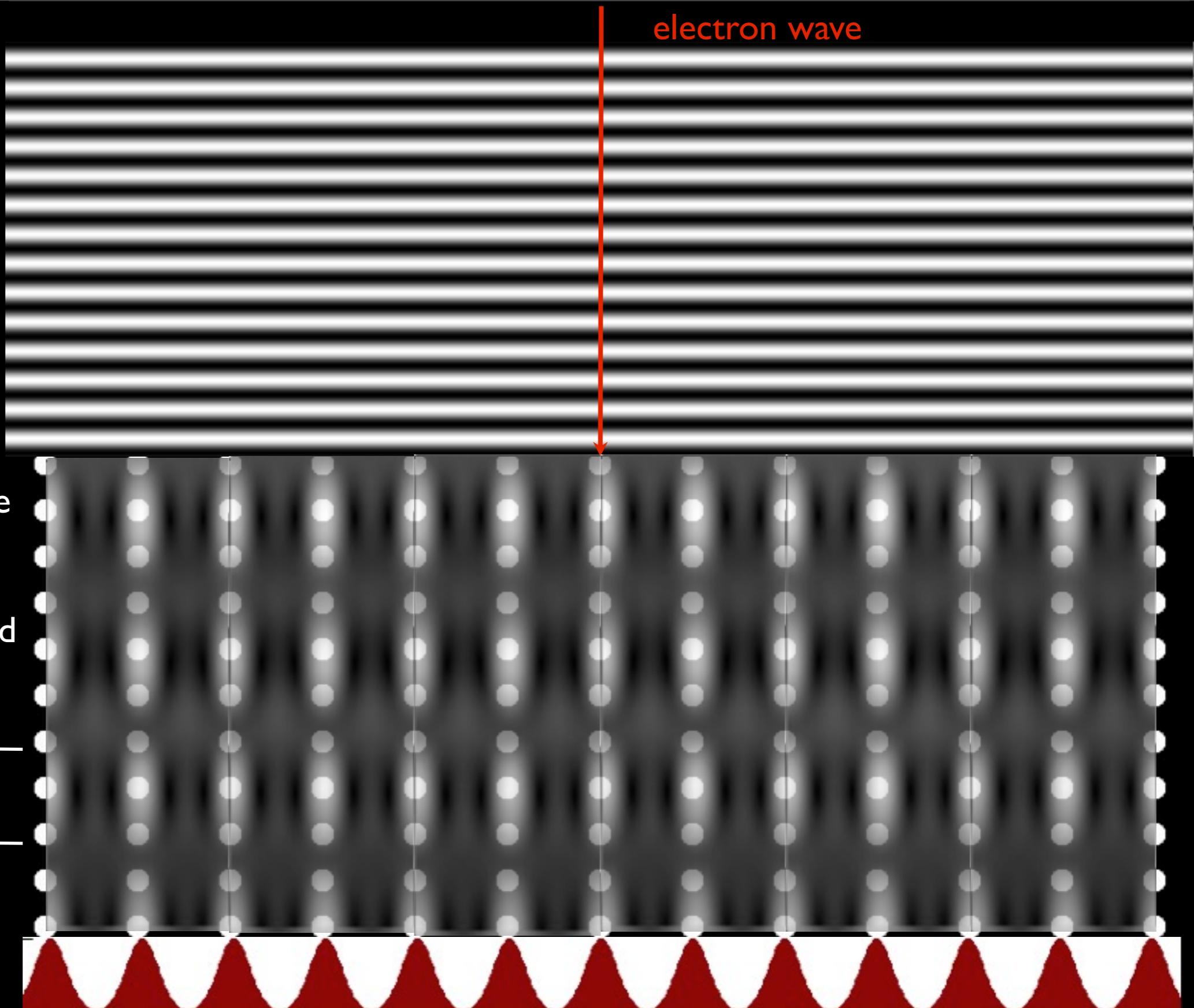
Electron Channeling

wave propagates inside  
crystal

~ electrons are trapped  
along the atomic  
columns

depends on z





Electron Channeling

wave propagates inside  
crystal

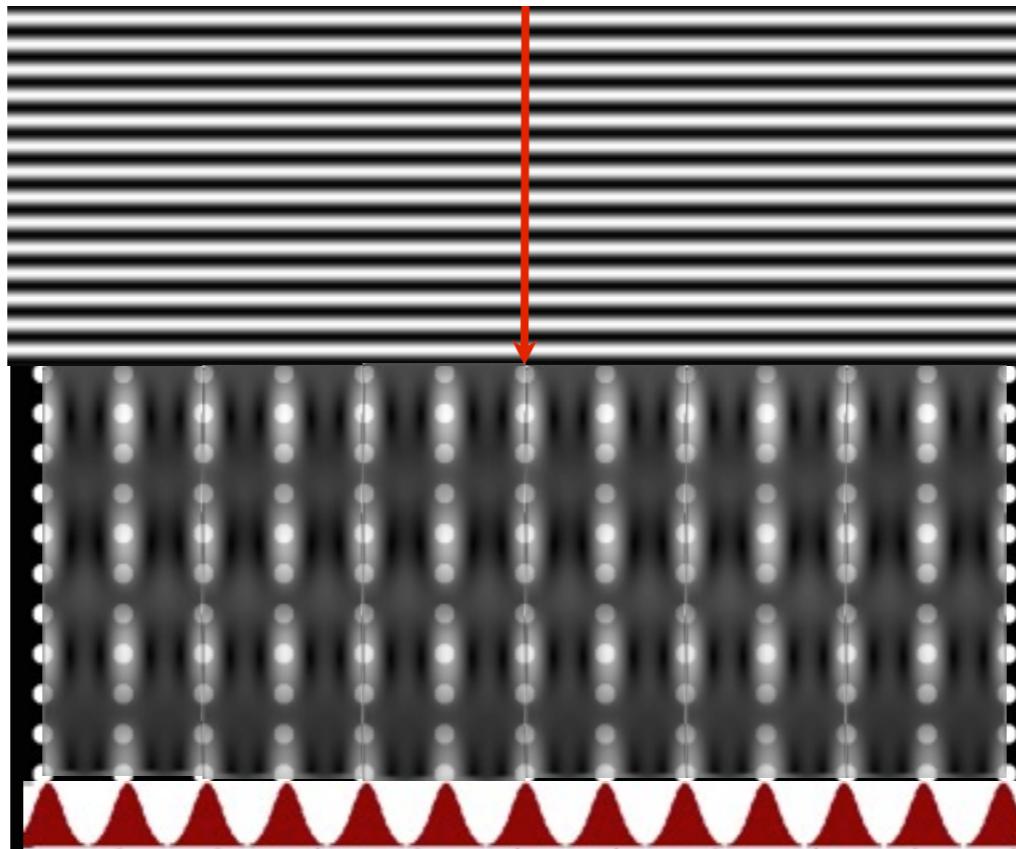
~ electrons are trapped  
along the atomic  
columns

depends on z

electron wave

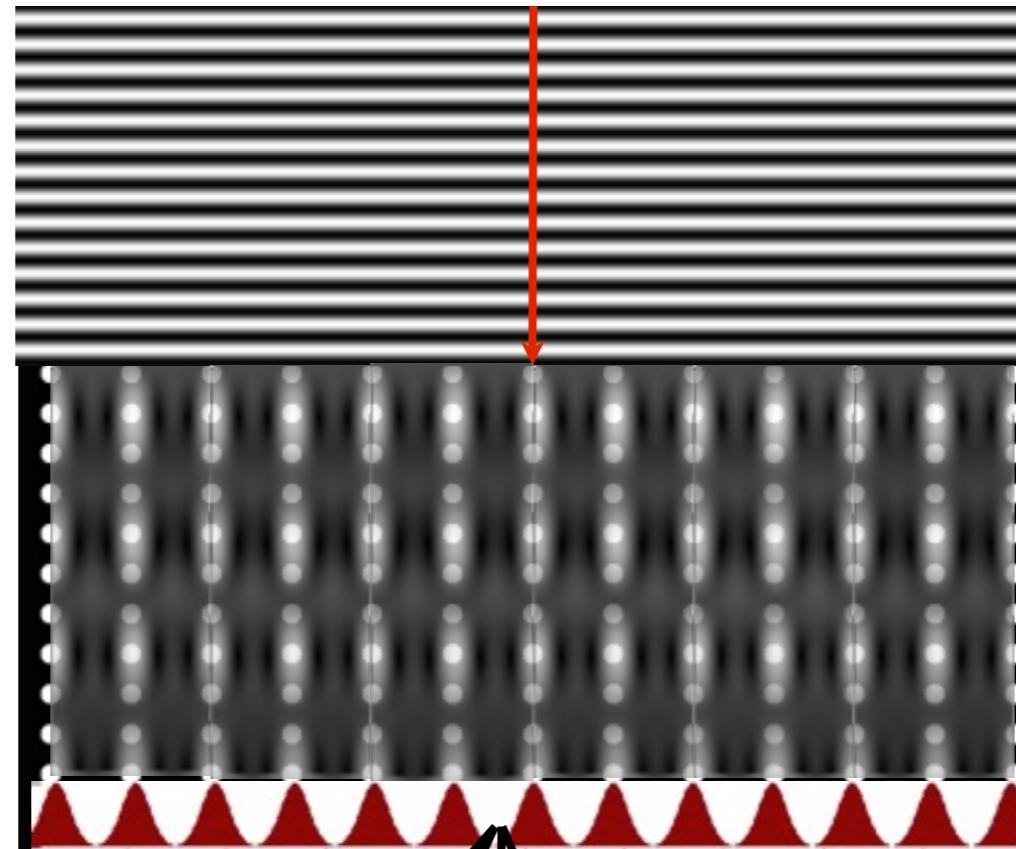
Exit Wave

**exit wave**  
 $\Psi_e(r) = A(r) \exp(i\varphi(r))$



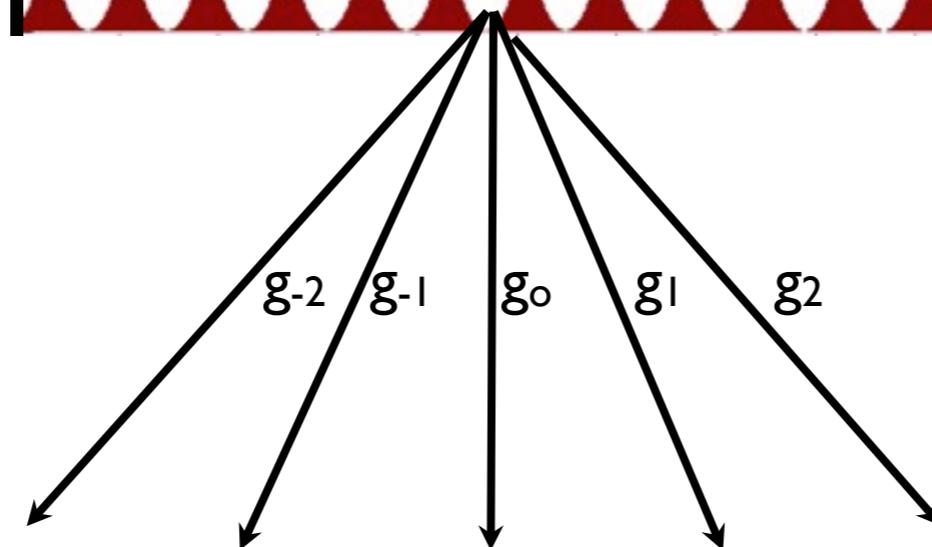
electron wave

exit wave  
 $\Psi_e(r) = A(r) \exp(i\varphi(r))$



electron wave

Fourier Theory  
 $\Psi_e(x, y) = \sum F(g) \exp(2\pi g r)$



exit wave

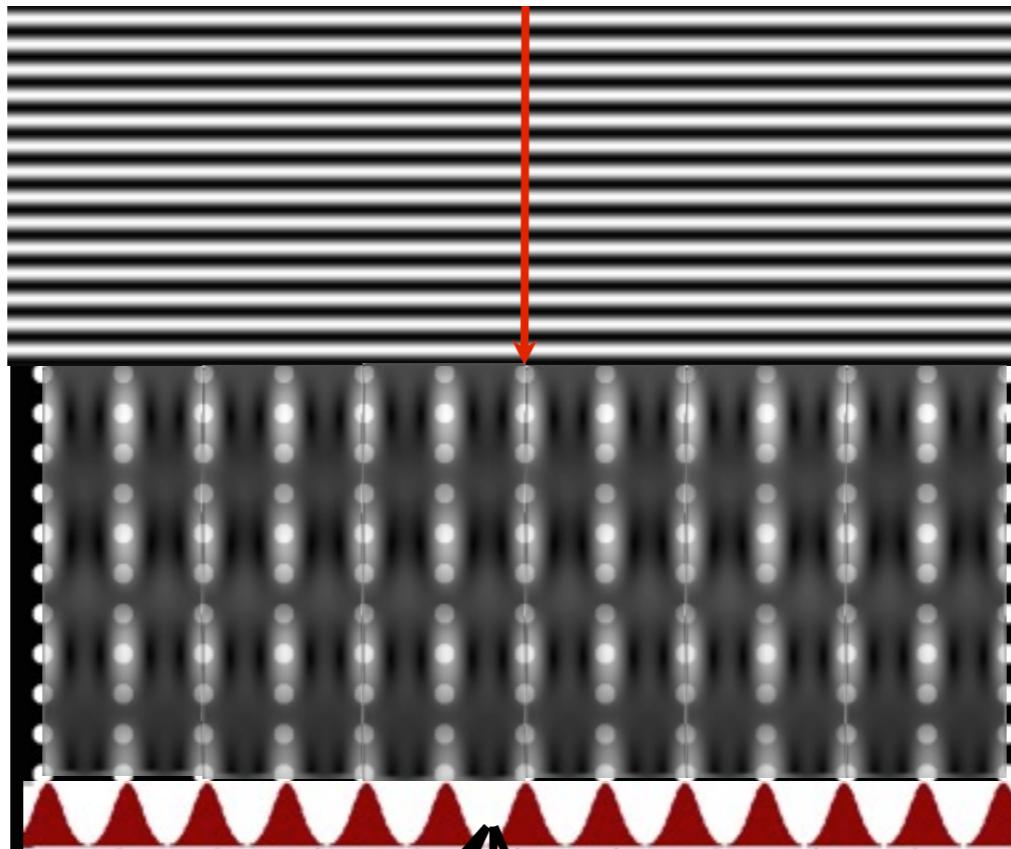
$$\Psi_e(r) = A(r) \exp(i\varphi(r))$$

Fourier Theory

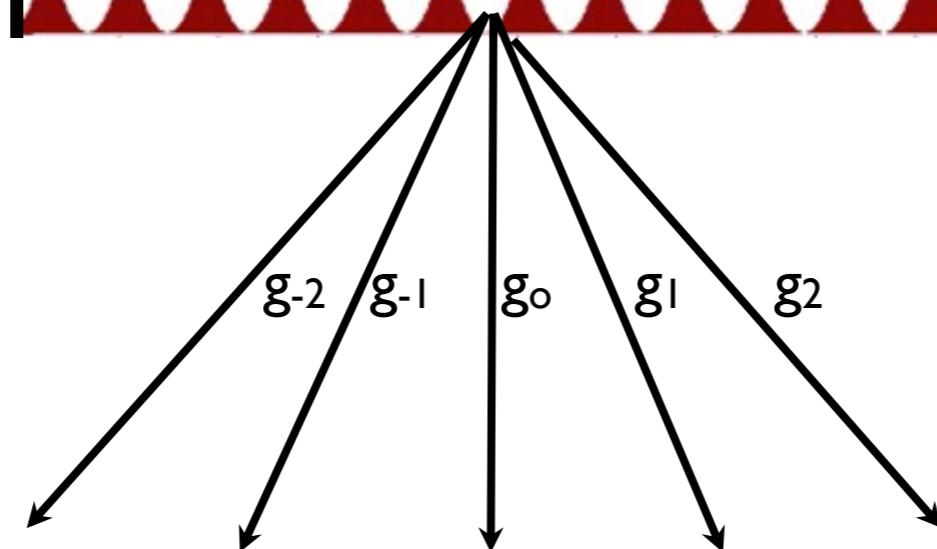
$$\Psi_e(x, y) = \sum F(g) \exp(2\pi g r)$$

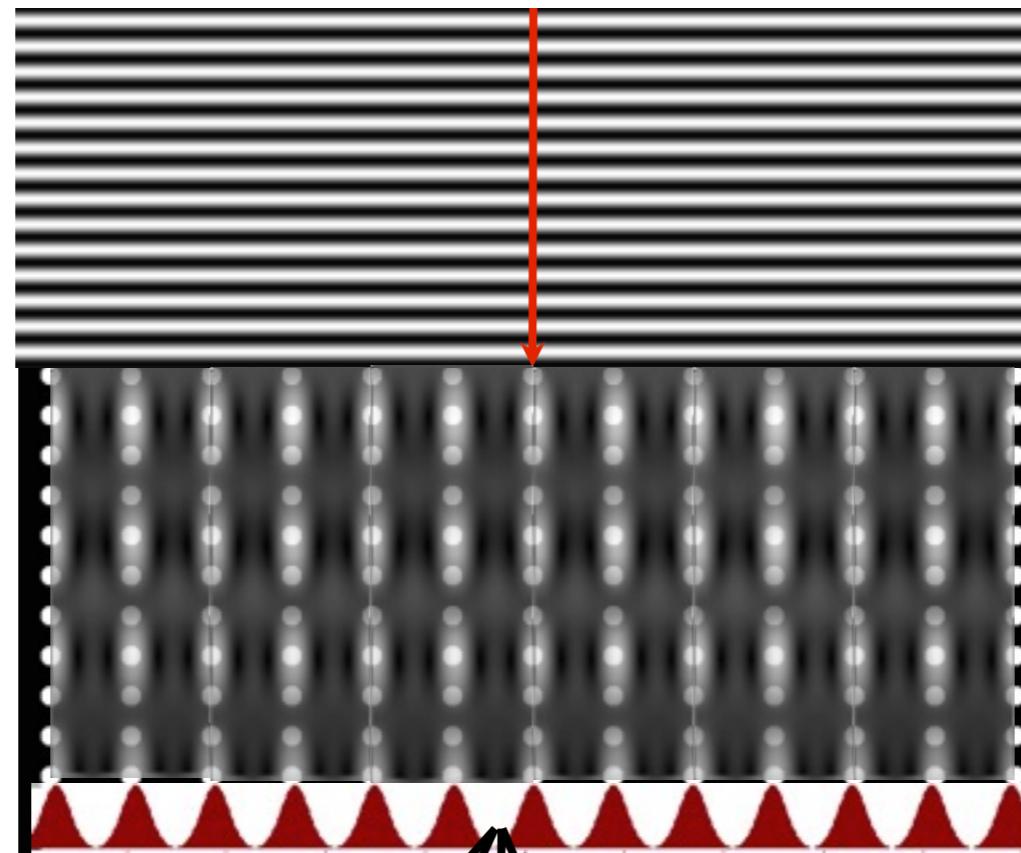
Physics

each Fourier component is  
called diffracted wave



electron wave





exit wave

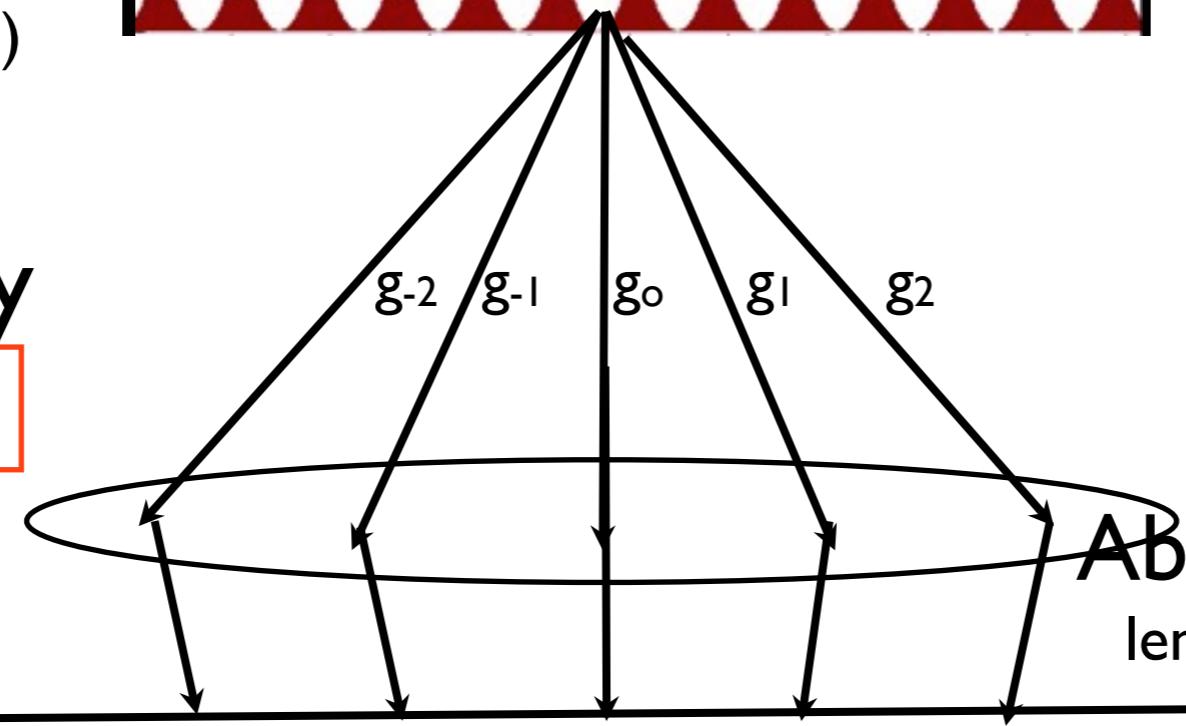
$$\Psi_e(r) = A(r) \exp(i\varphi(r))$$

Fourier Theory

$$\Psi_e(x, y) = \sum F(g) \exp(2\pi g r)$$

Physics

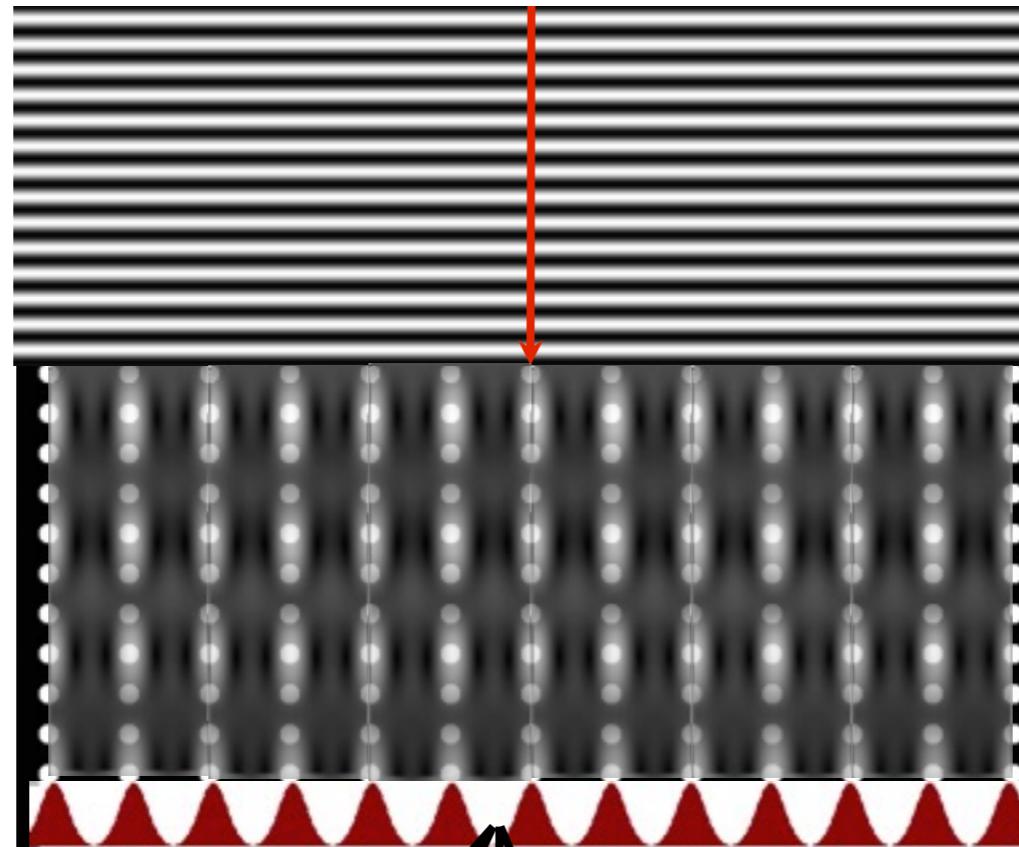
each Fourier component is  
called diffracted wave



Abbe Microscopy Theory  
lens does two Fourier transforms

exit wave

$$\Psi_e(r) = A(r) \exp(i\varphi(r))$$



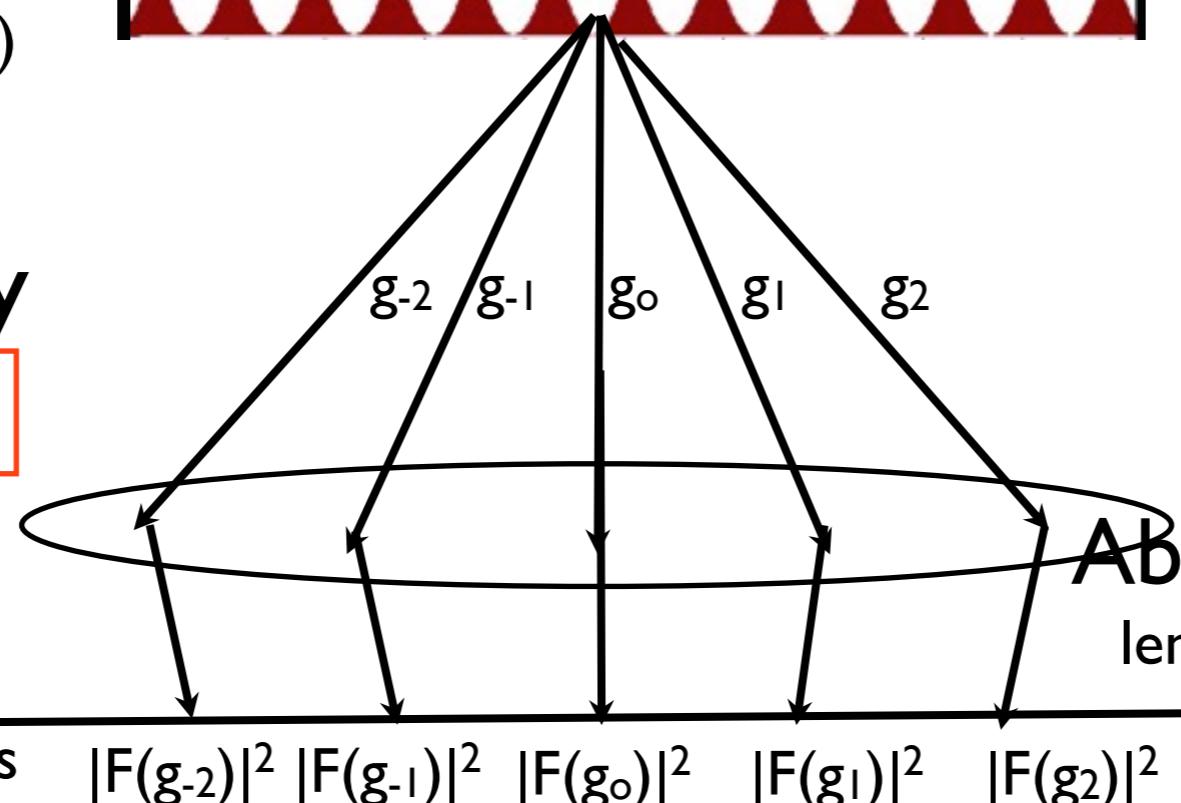
electron wave

Fourier Theory

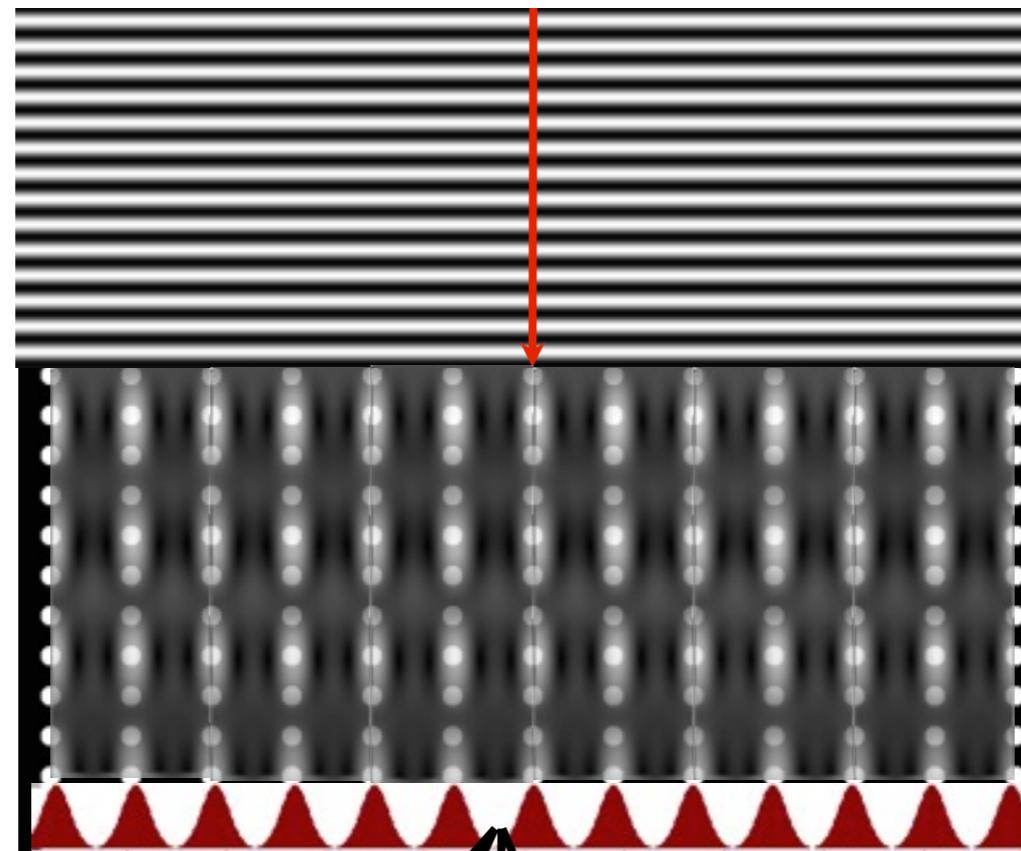
$$\Psi_e(x, y) = \sum F(g) \exp(2\pi g r)$$

Physics

each Fourier component is  
called diffracted wave



Abbe Microscopy Theory  
lens does two Fourier transforms  
Focal plane



electron wave

exit wave

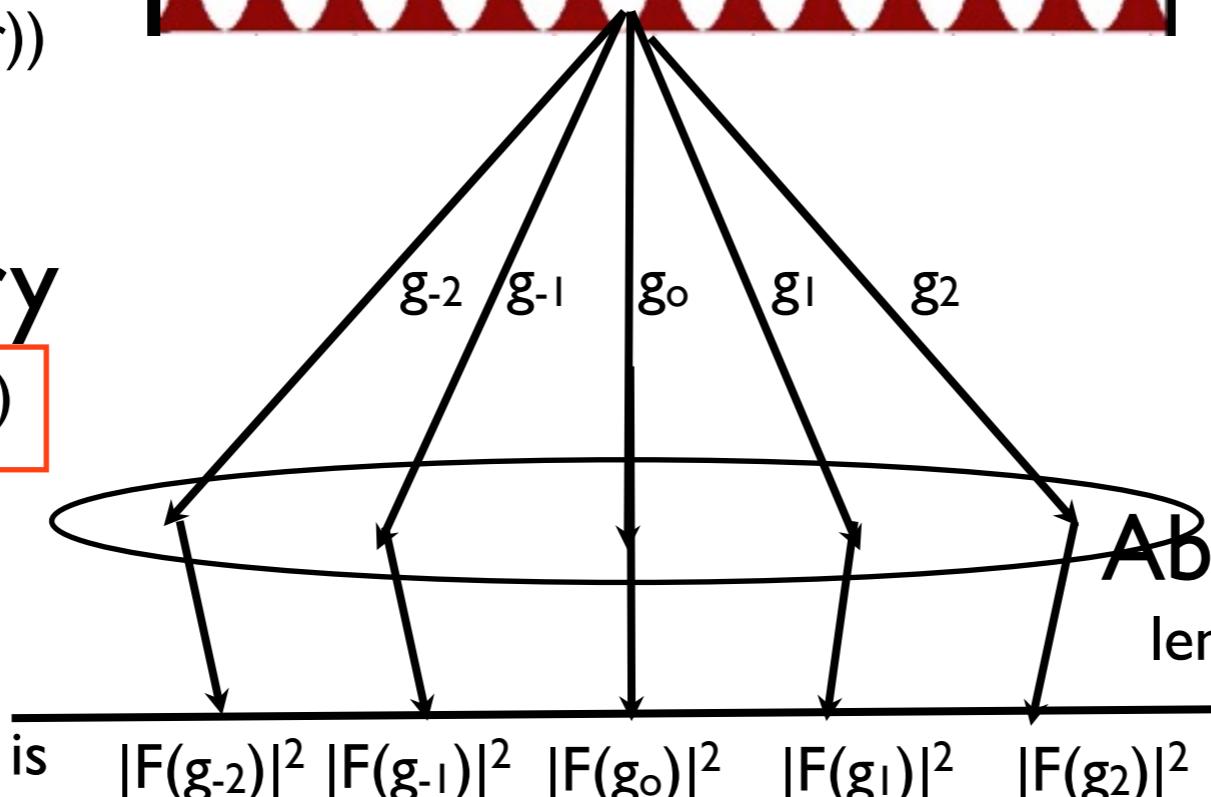
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Fourier Theory

$$\Psi_e(x, y) = \sum F(g) \exp(2\pi g r)$$

Physics

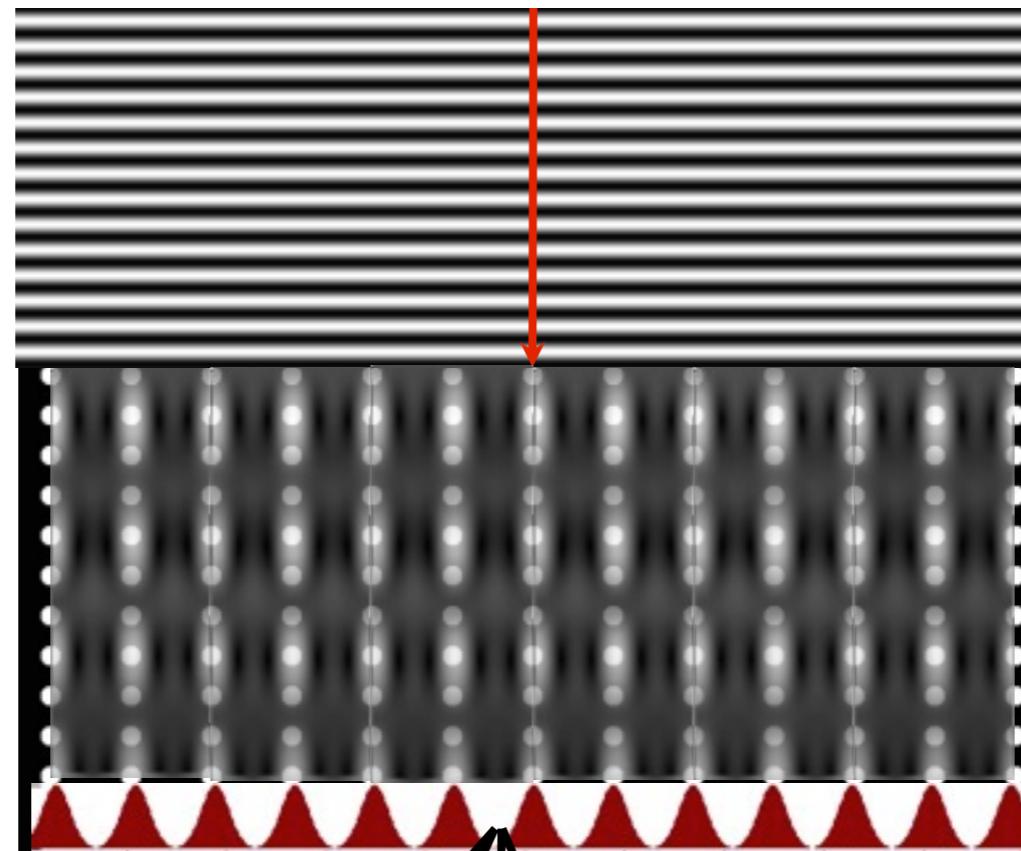
each Fourier component is  
called diffracted wave



Abbe Microscopy Theory  
lens does two Fourier transforms  
Focal plane



image plane



**exit wave**

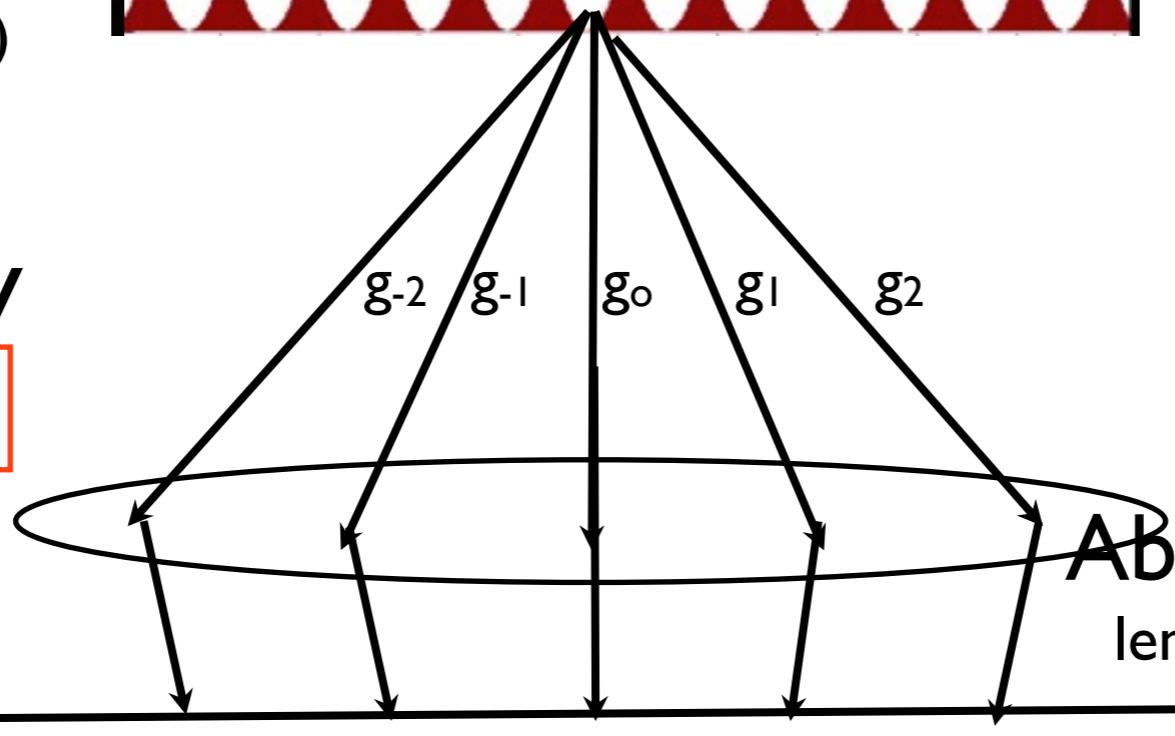
$$\Psi_e(r) = A(r) \exp(i\varphi(r))$$

**Fourier Theory**

$$\Psi_e(x, y) = \sum F(g) \exp(2\pi gr)$$

**Physics**

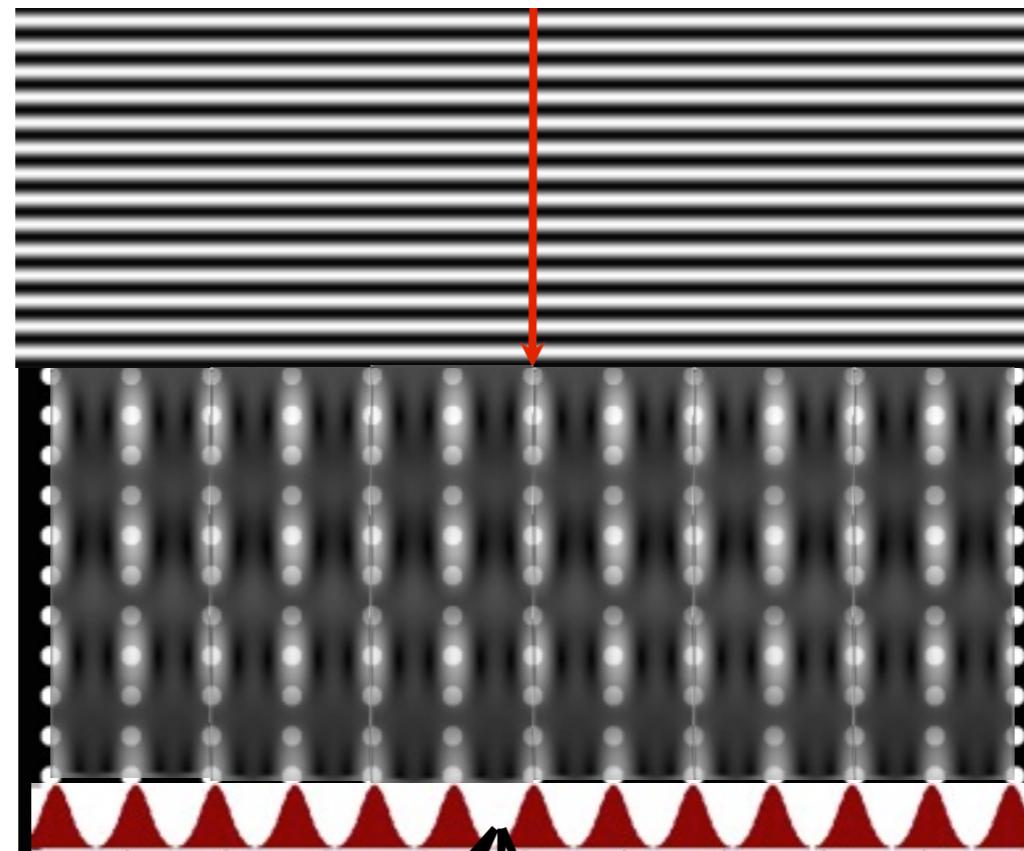
each Fourier component is called diffracted wave



**lens aberrations modify the Fourier Components**

**electron wave**

**image plane**



exit wave

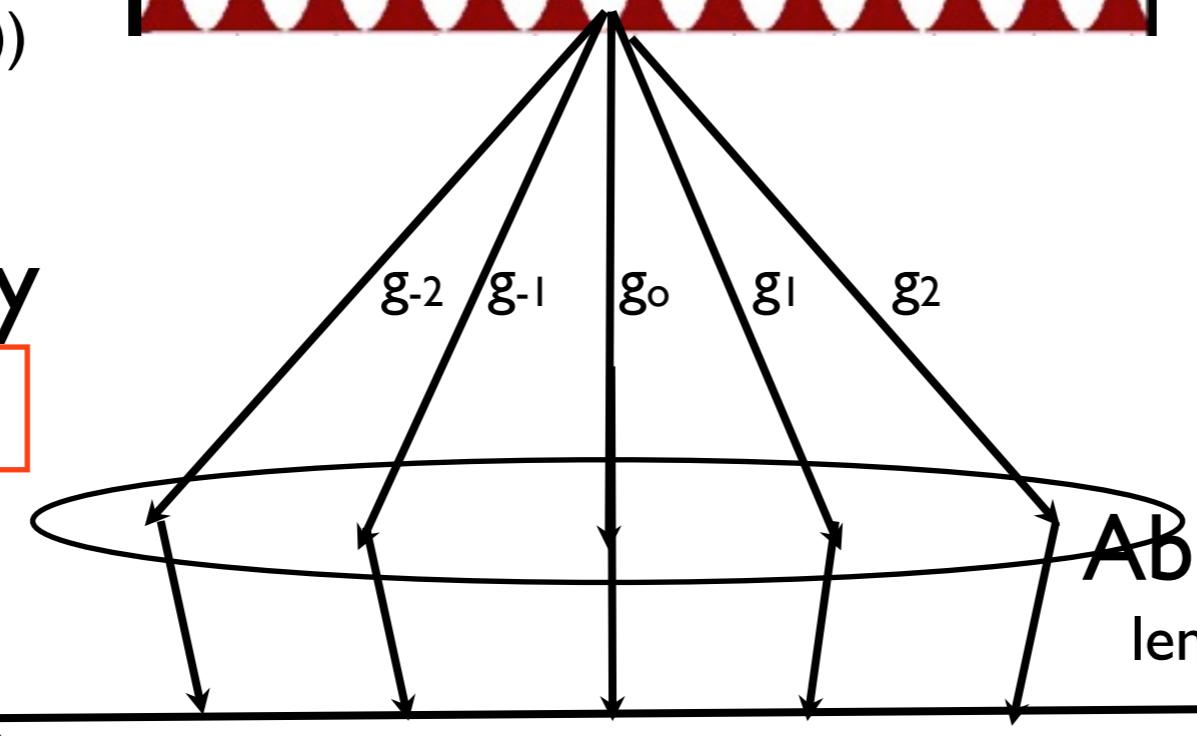
$$\Psi_e(r) = A(r) \exp(i\varphi(r))$$

Fourier Theory

$$\Psi_e(x, y) = \sum F(g) \exp(2\pi g r)$$

Physics

each Fourier component is called diffracted wave



lens aberrations modify the Fourier Components

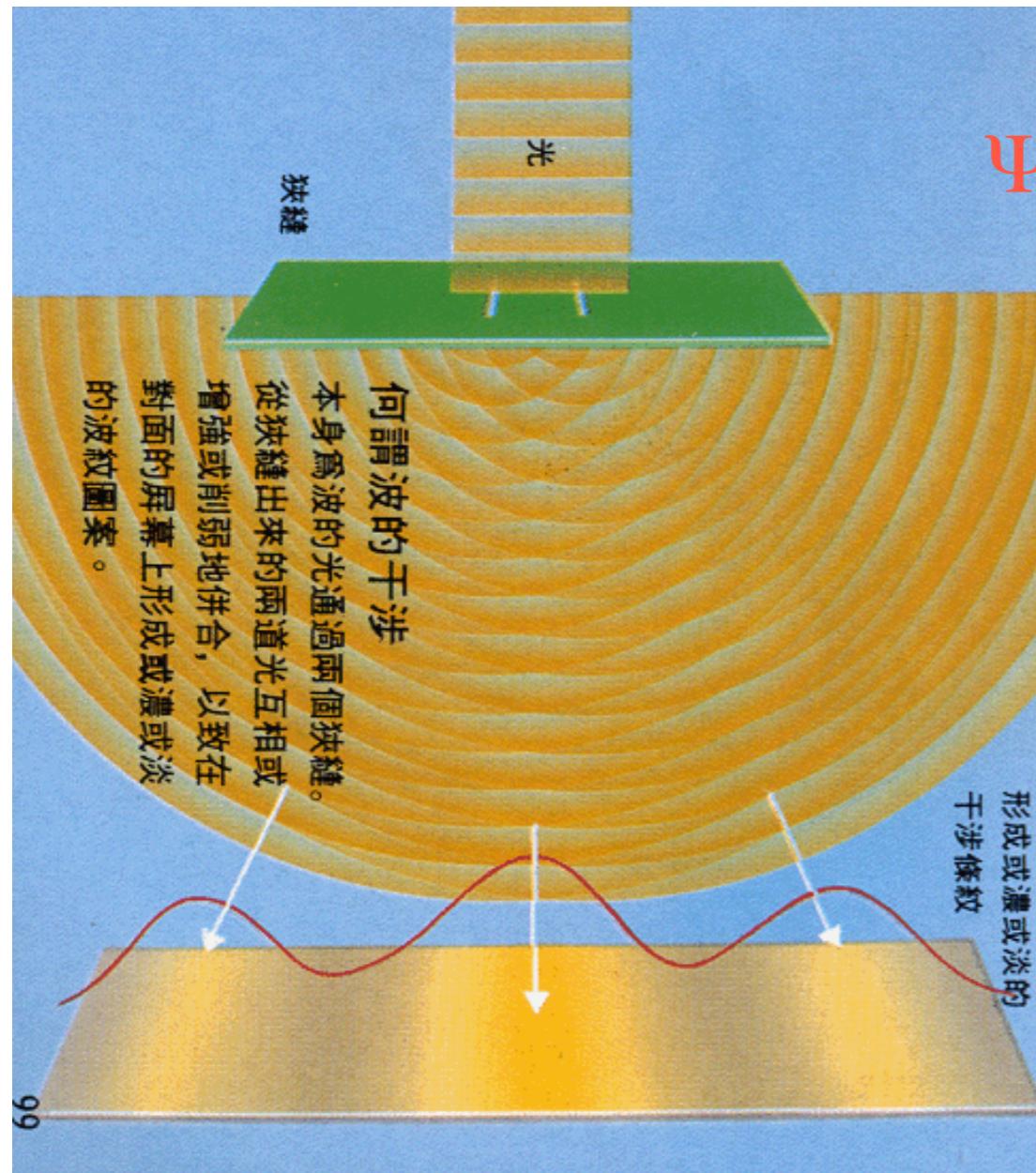
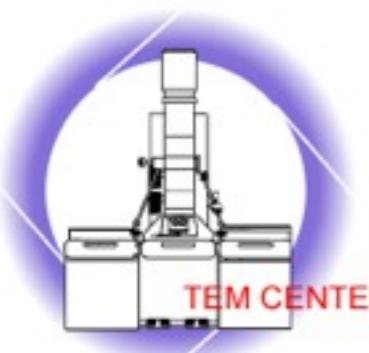


$$I = |A(r)|^2, \text{ Phase lost}$$

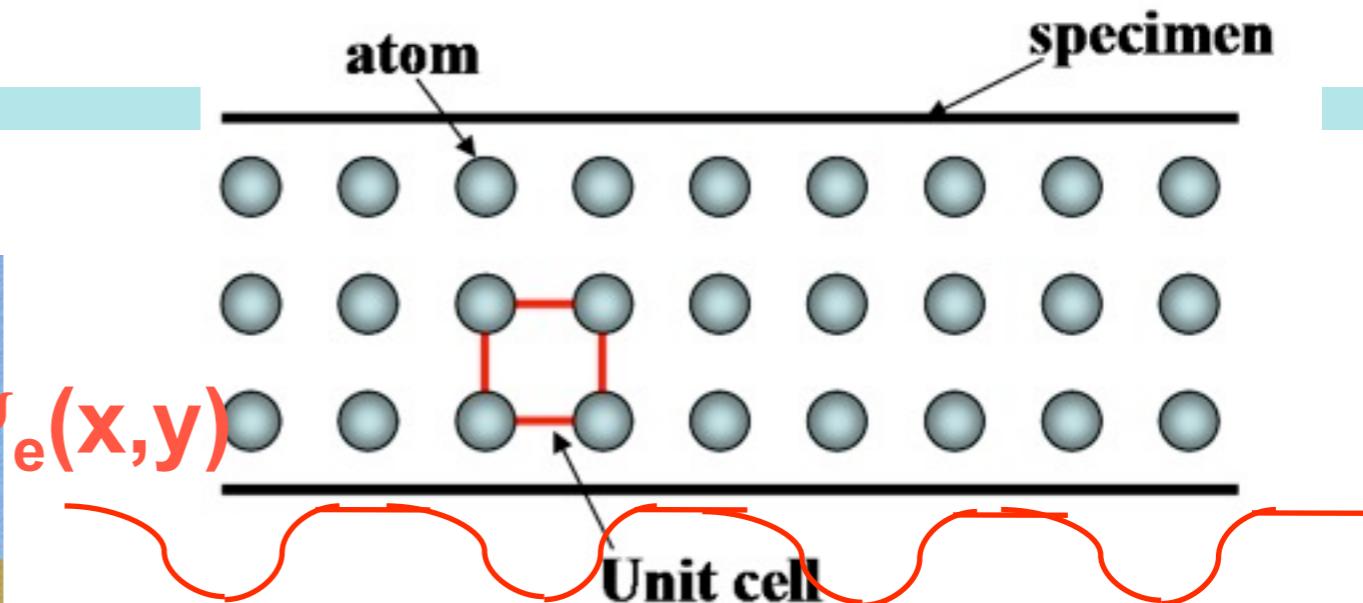
electron wave

image plane

# Interaction of Electron Wave with Crystal



亮線位置不一定與原子柱位置重疊

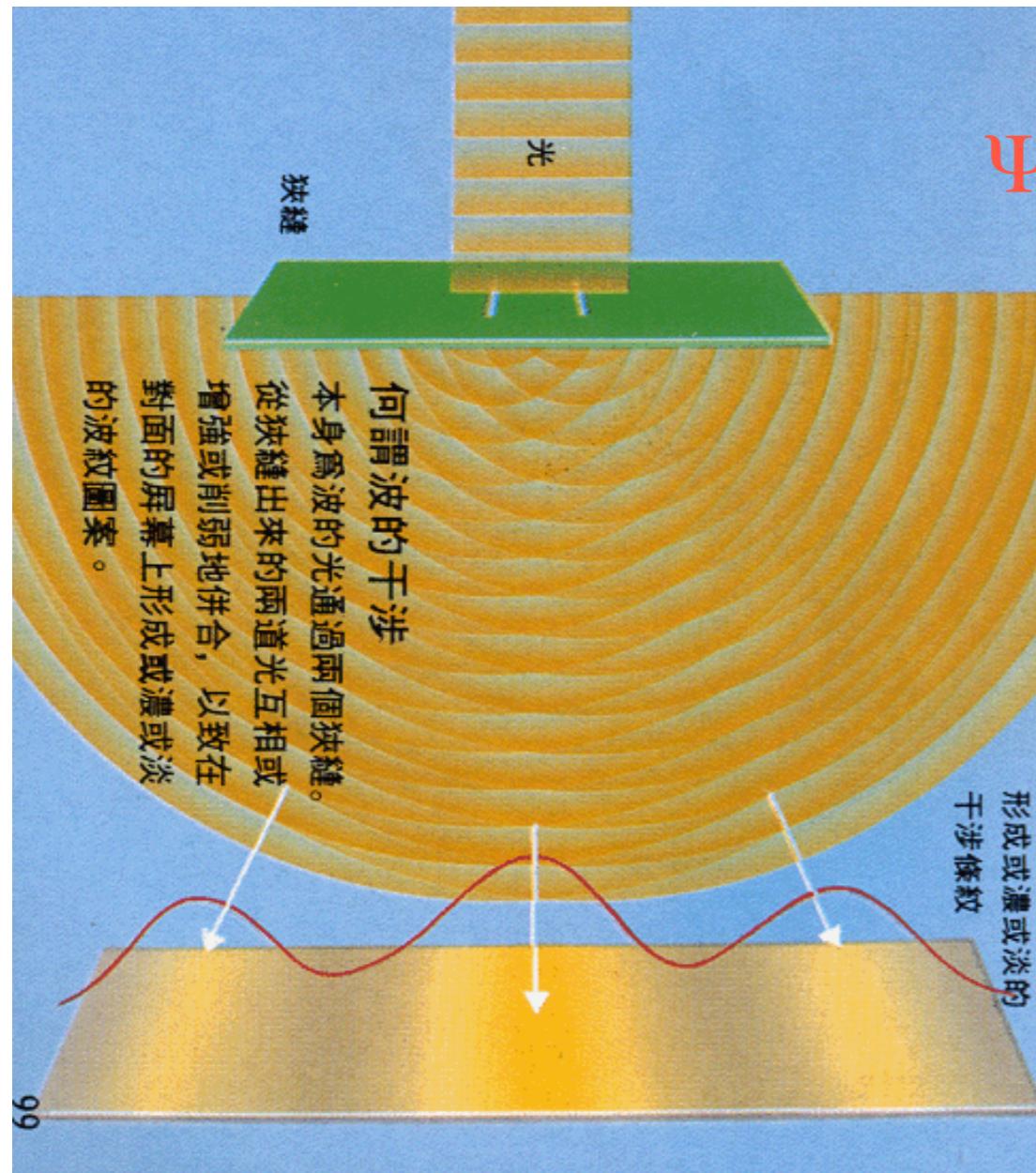
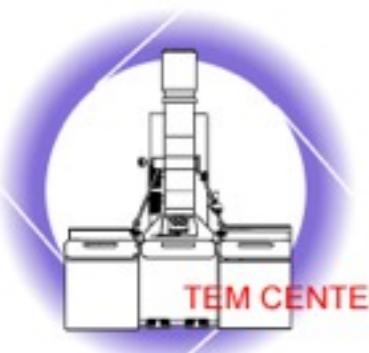


$\mathbf{g}_{-1}$   $\mathbf{g}_0$   $\mathbf{g}_1$

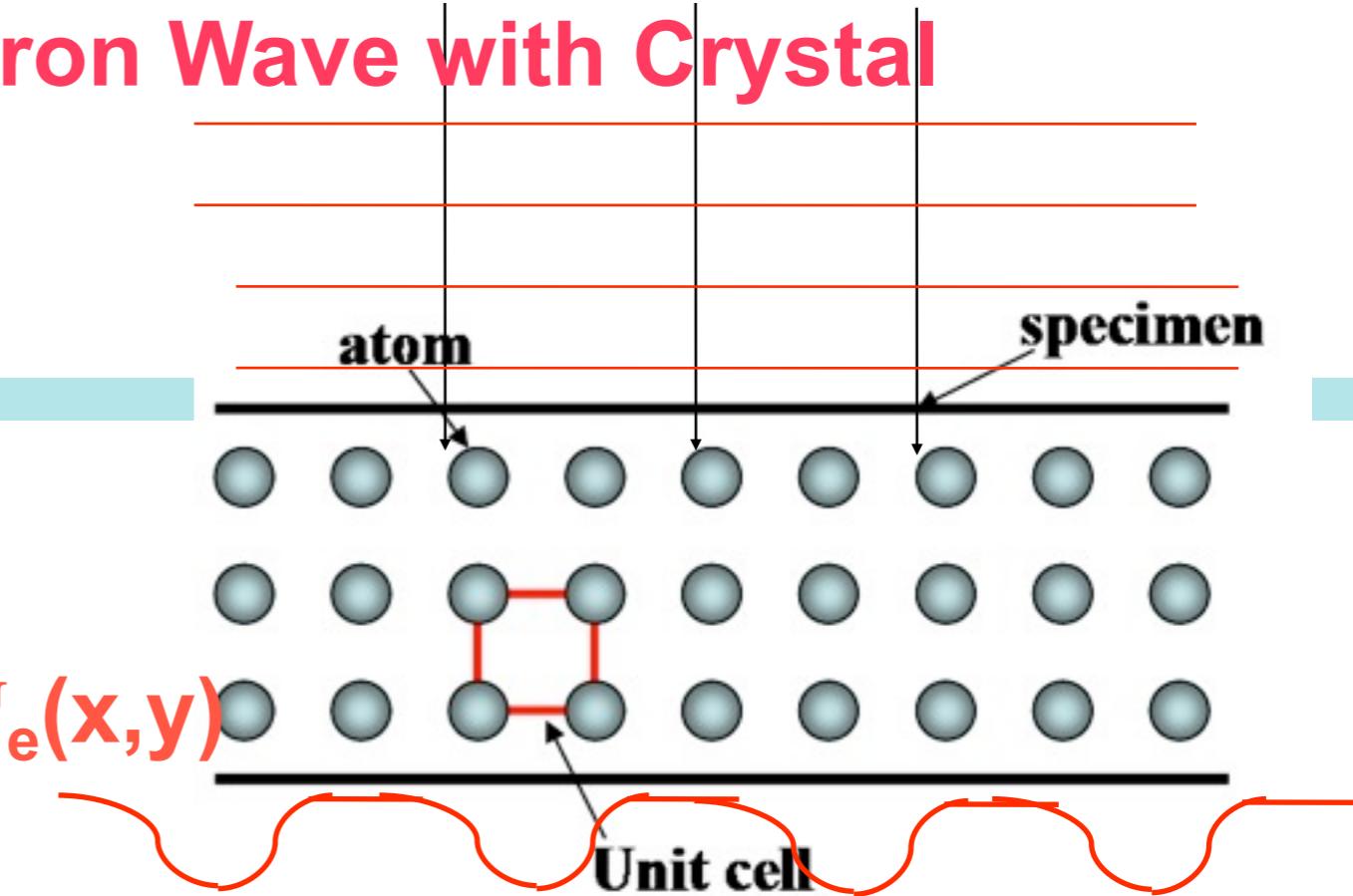
$\Psi_e$  is composed of many Fourier components

$$\Psi_e(x, y) = \sum_{H=-g}^g F(H) \exp(-2\pi H \cdot r)$$

# Interaction of Electron Wave with Crystal



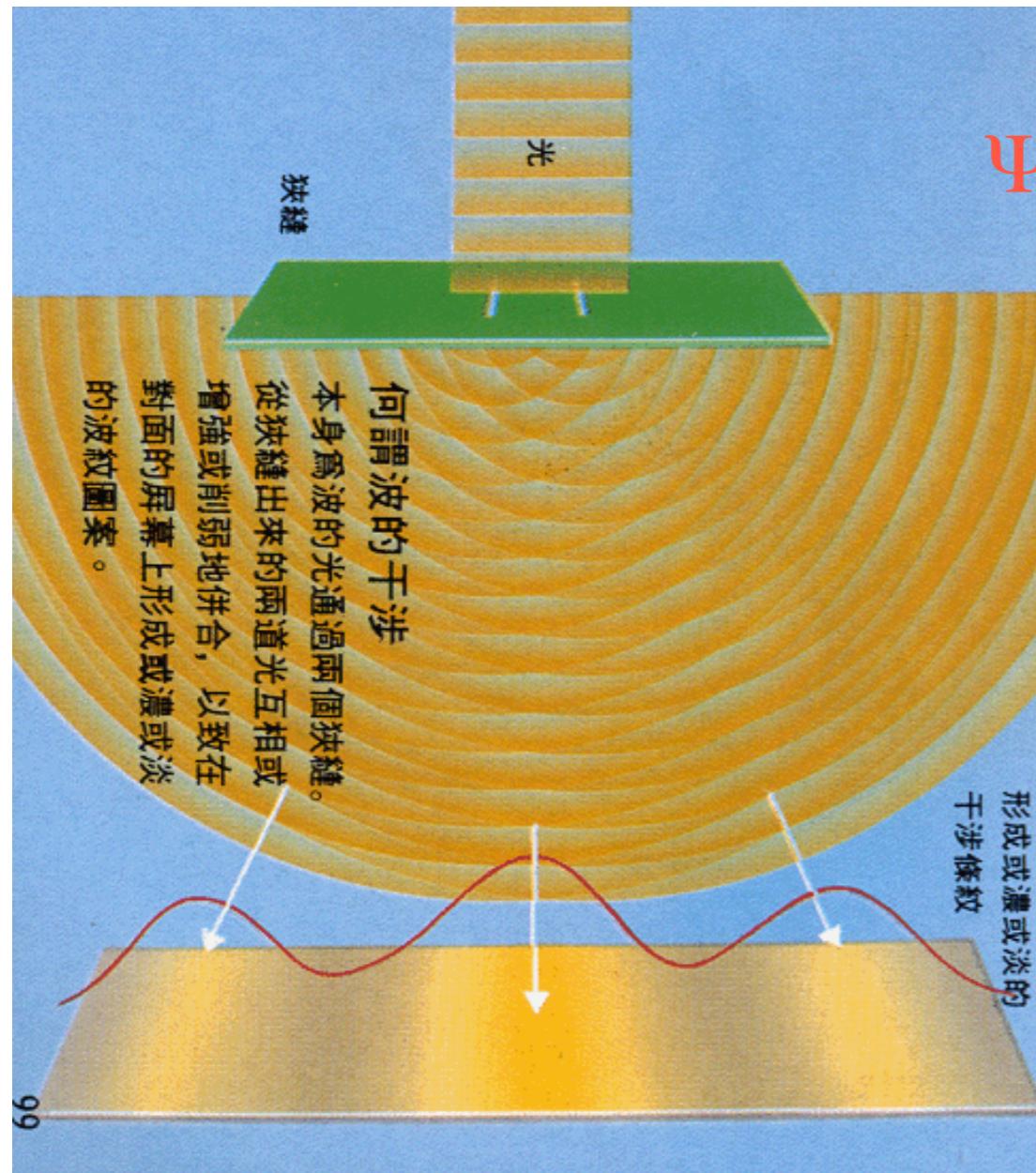
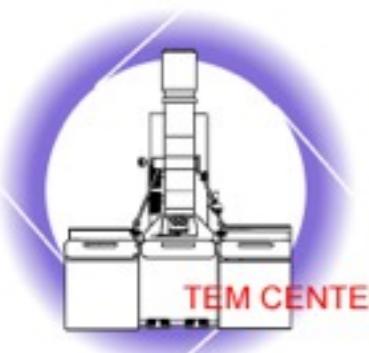
亮線位置不一定與原子柱位置重疊



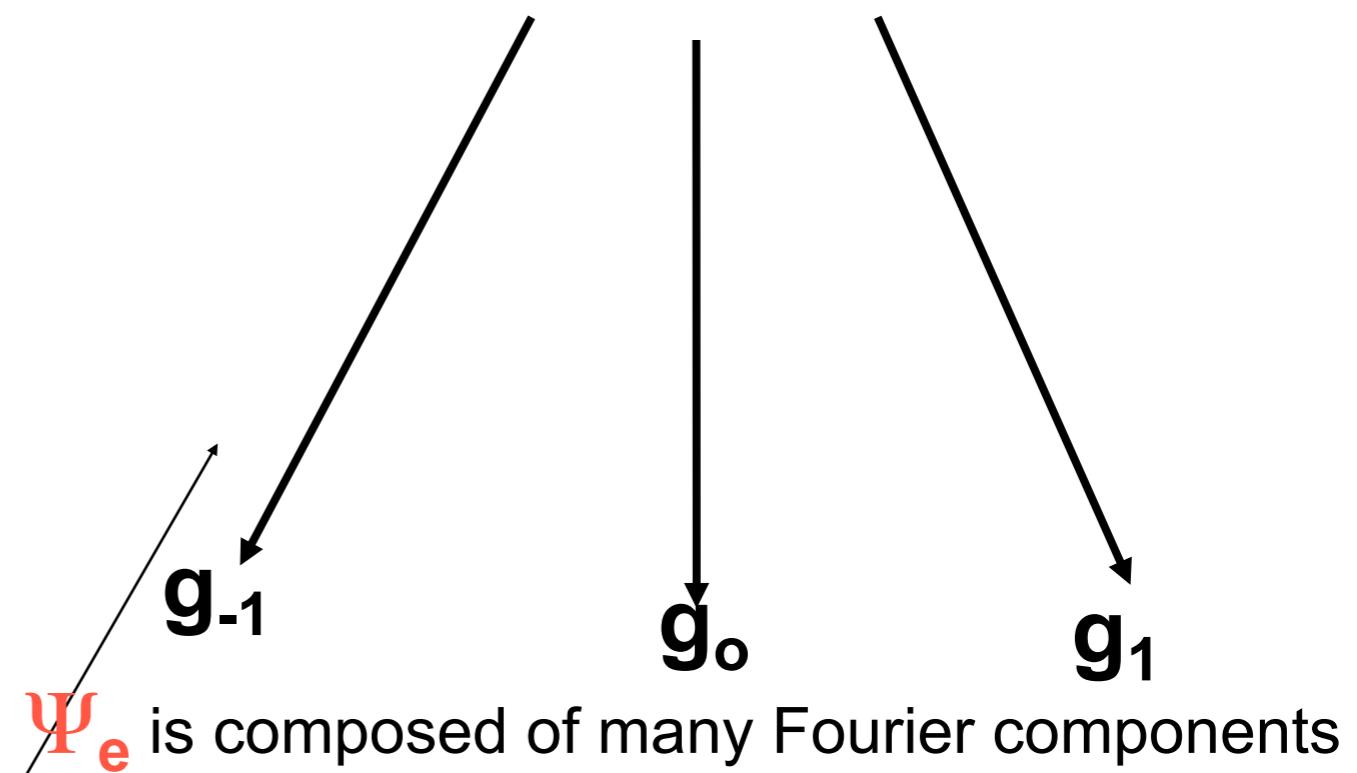
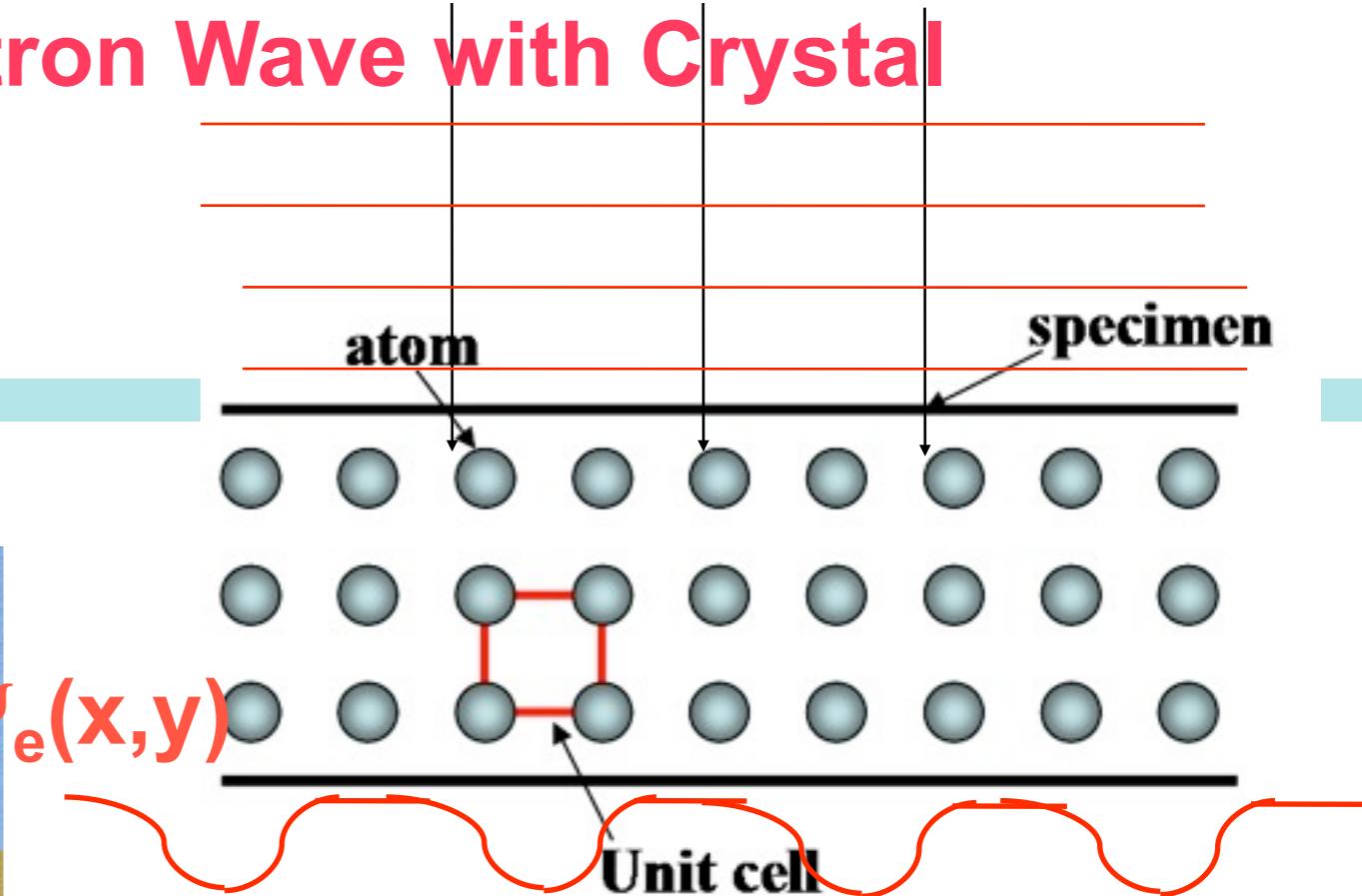
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# Interaction of Electron Wave with Crystal

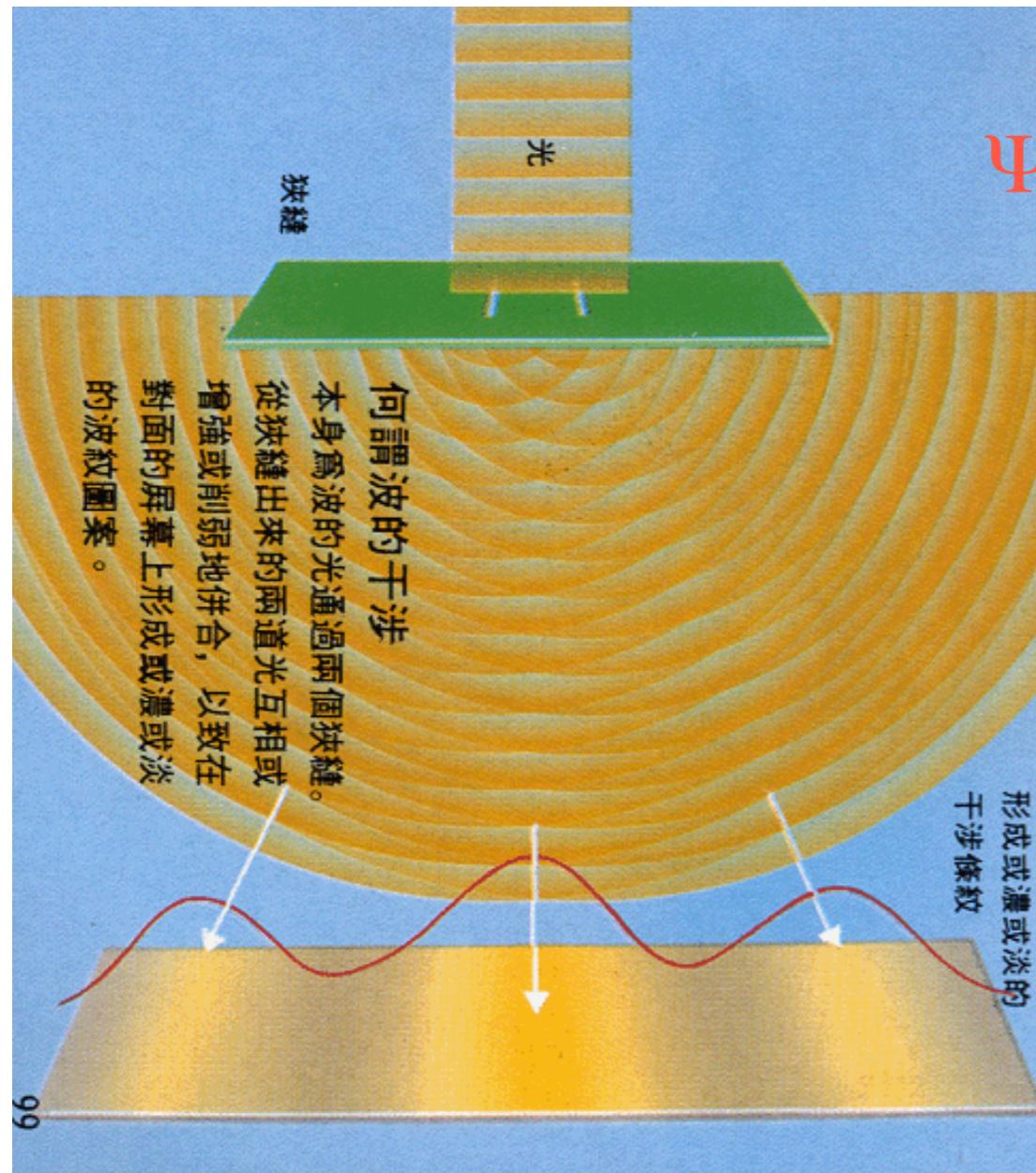
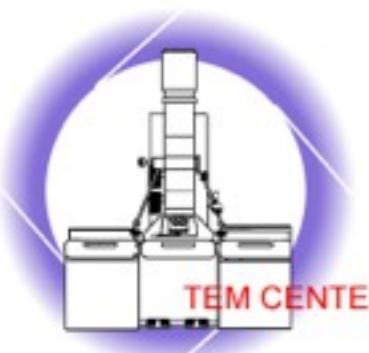


亮線位置不一定與原子柱位置重疊

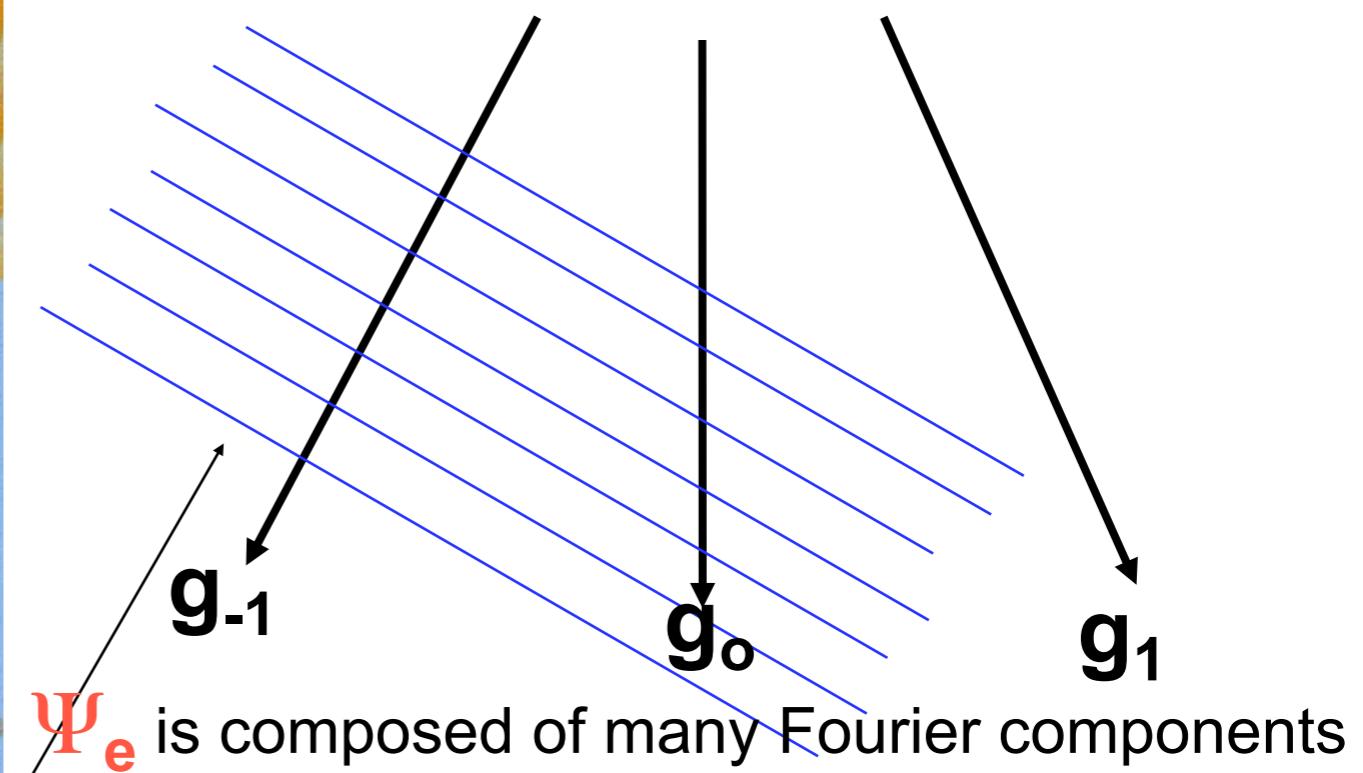
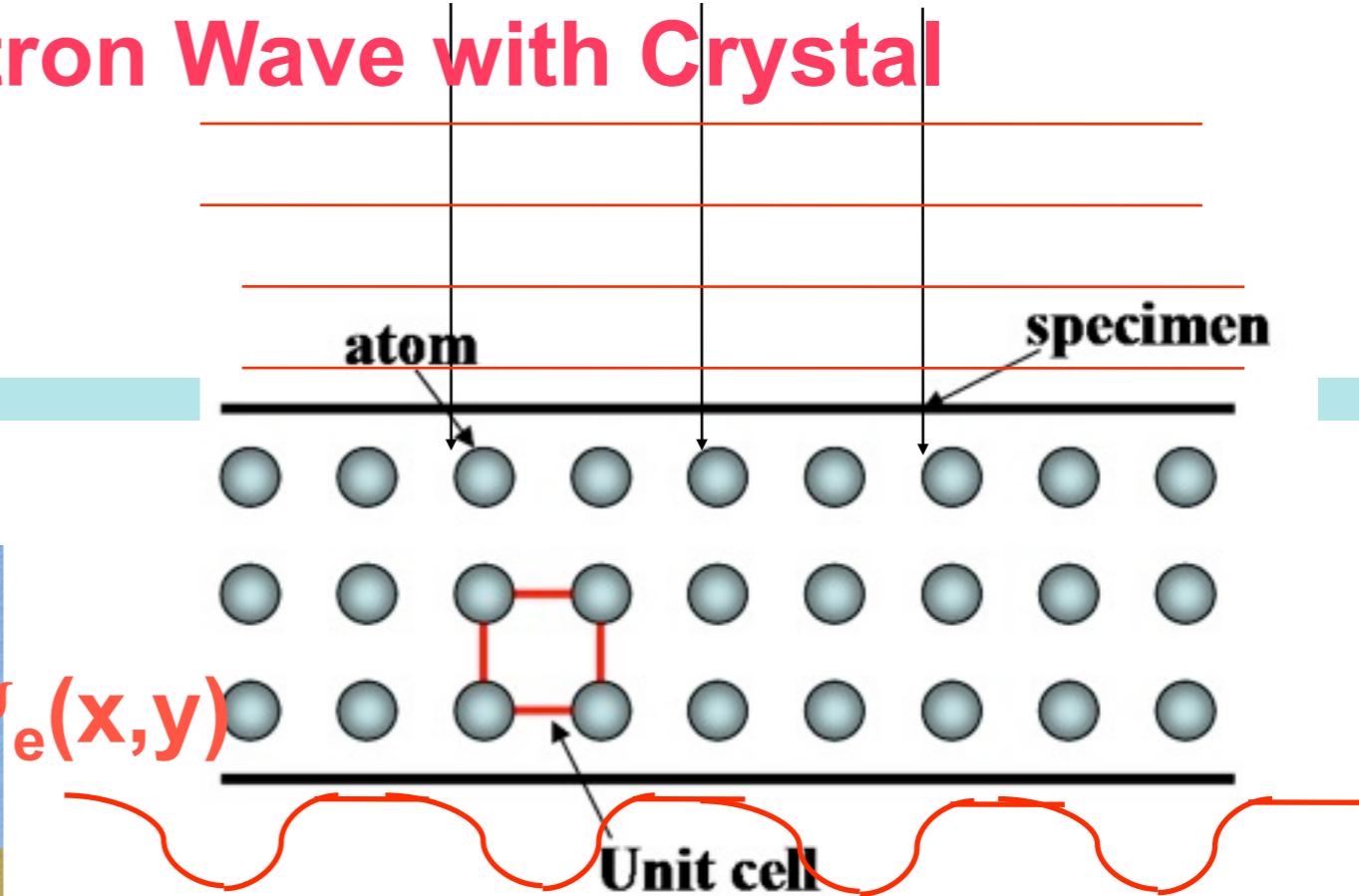


$$\Psi_e(x, y) = \sum_{H=-g}^g F(H) \exp(-2\pi H \cdot r)$$

# Interaction of Electron Wave with Crystal

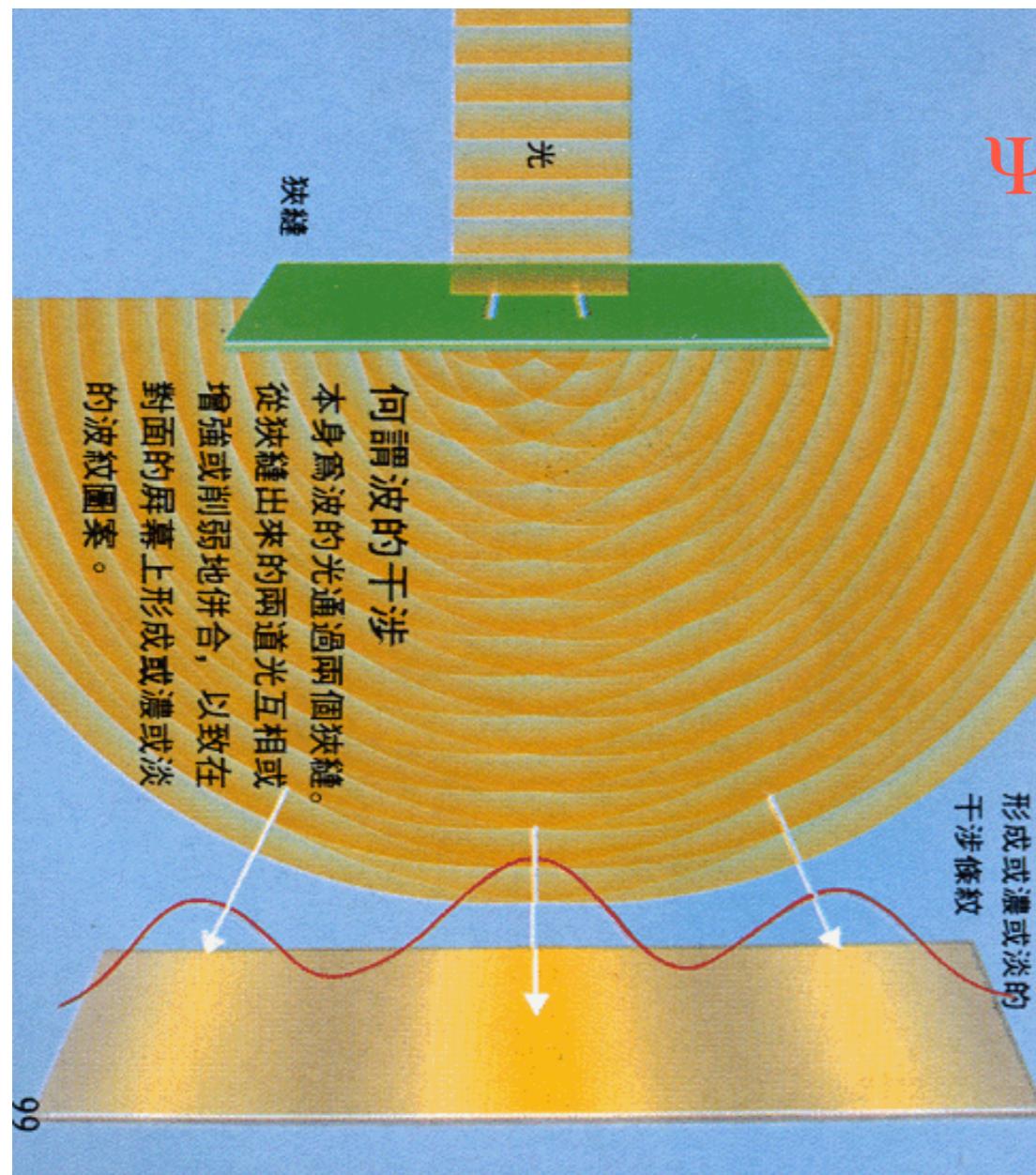
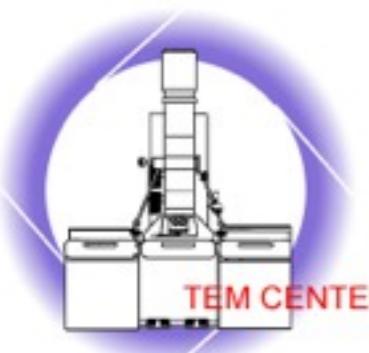


亮線位置不一定與原子柱位置重疊

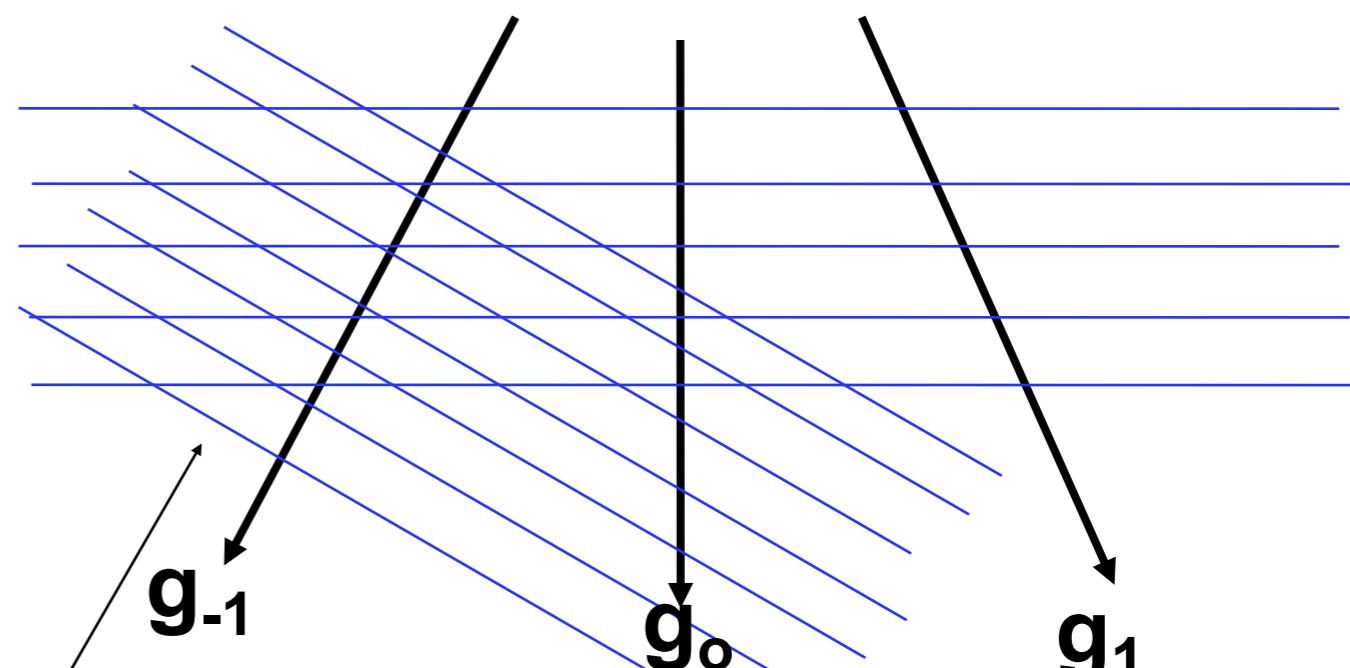
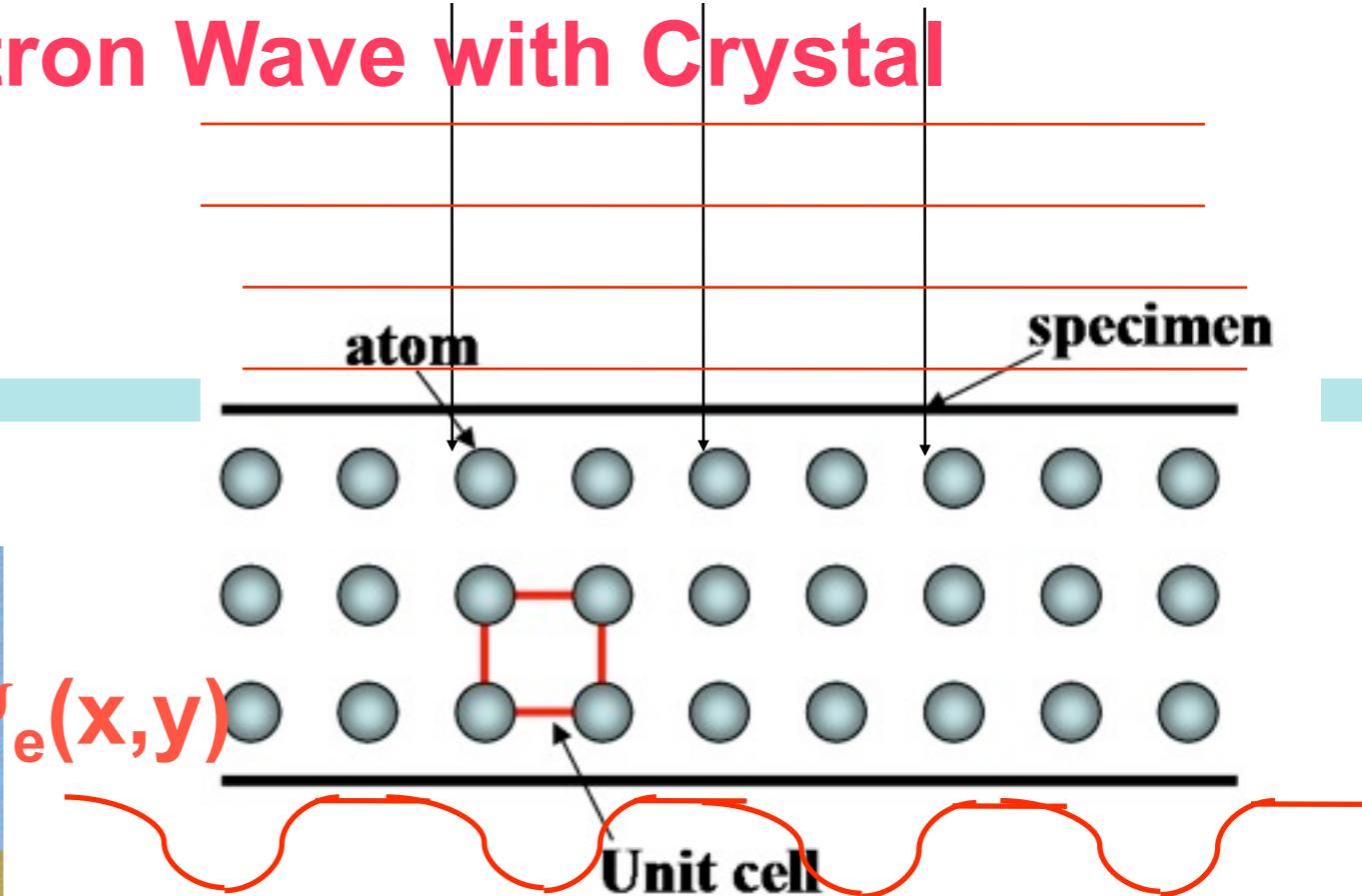


$$\Psi_e(x, y) = \sum_{H=-g}^g F(H) \exp(-2\pi H \cdot r)$$

# Interaction of Electron Wave with Crystal



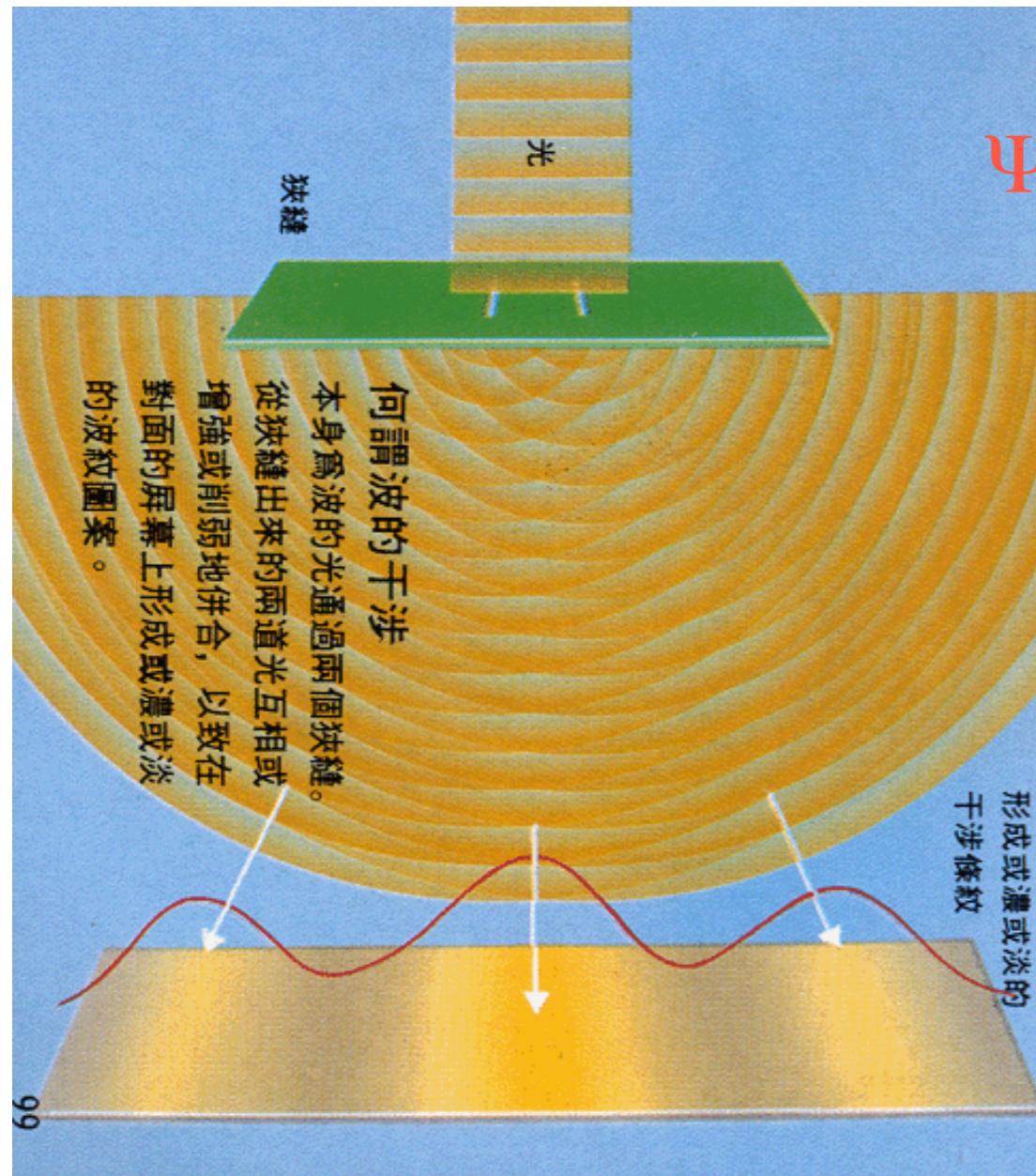
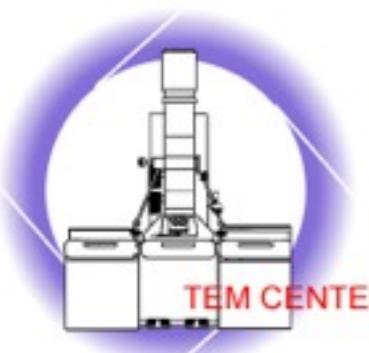
亮線位置不一定與原子柱位置重疊



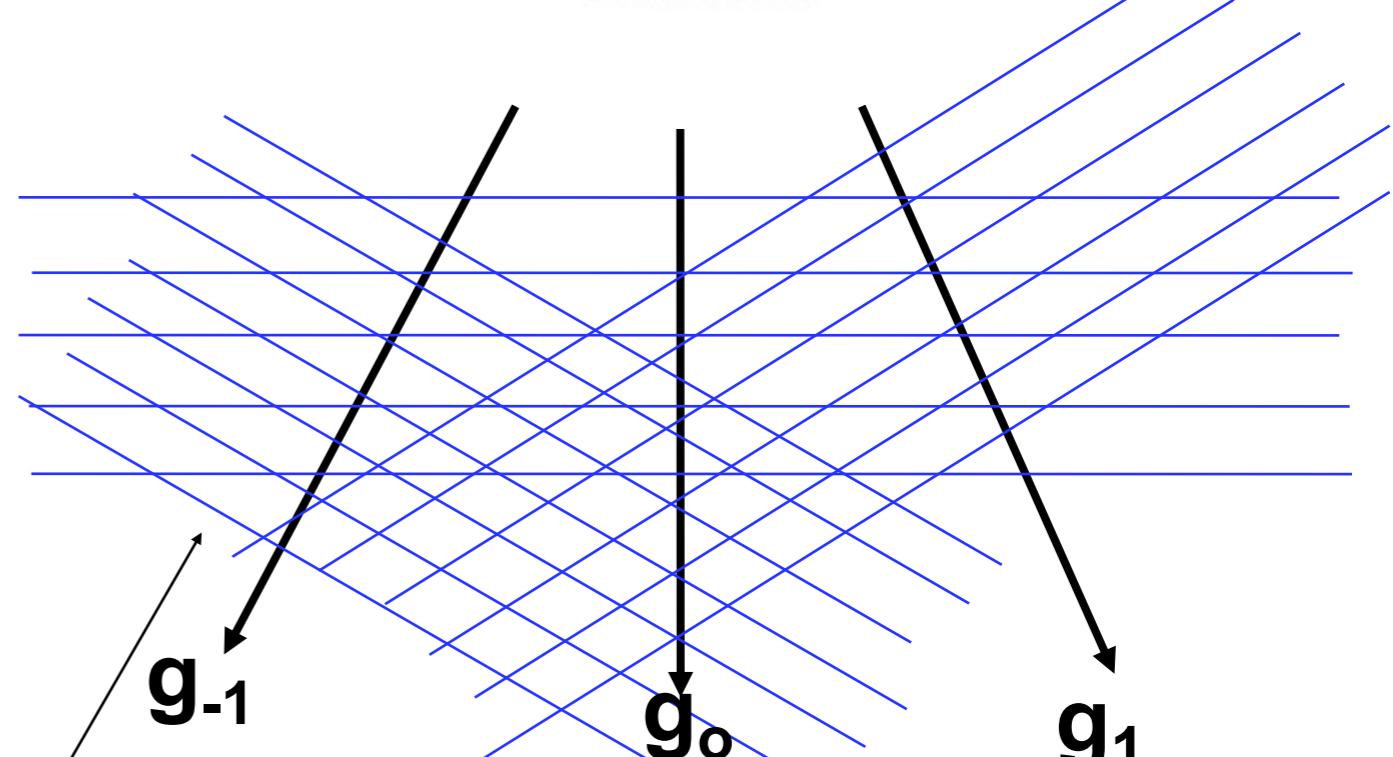
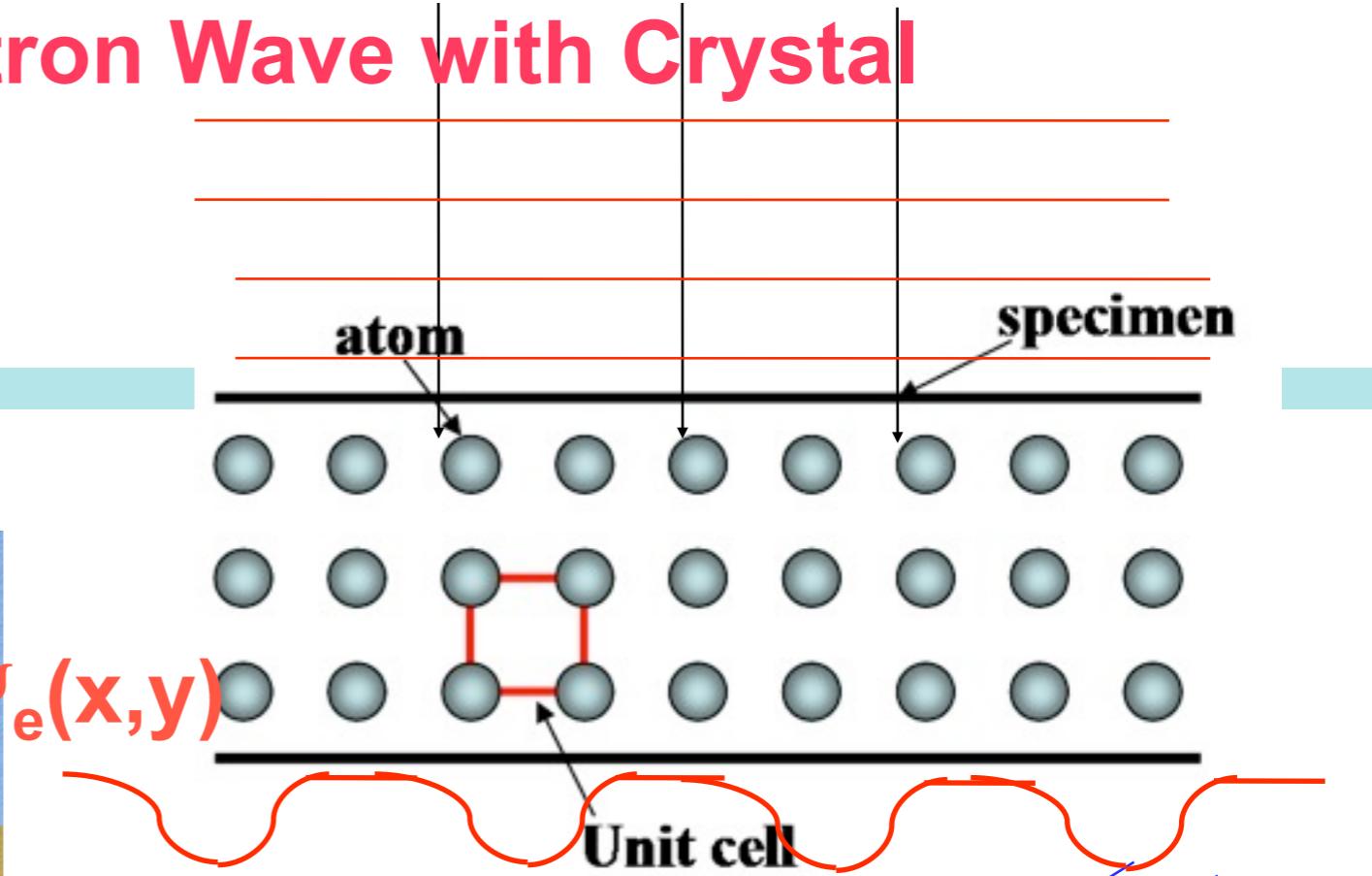
$\Psi_e$  is composed of many Fourier components

$$\Psi_e(x, y) = \sum_{H=-g}^g F(H) \exp(-2\pi H \cdot r)$$

# Interaction of Electron Wave with Crystal



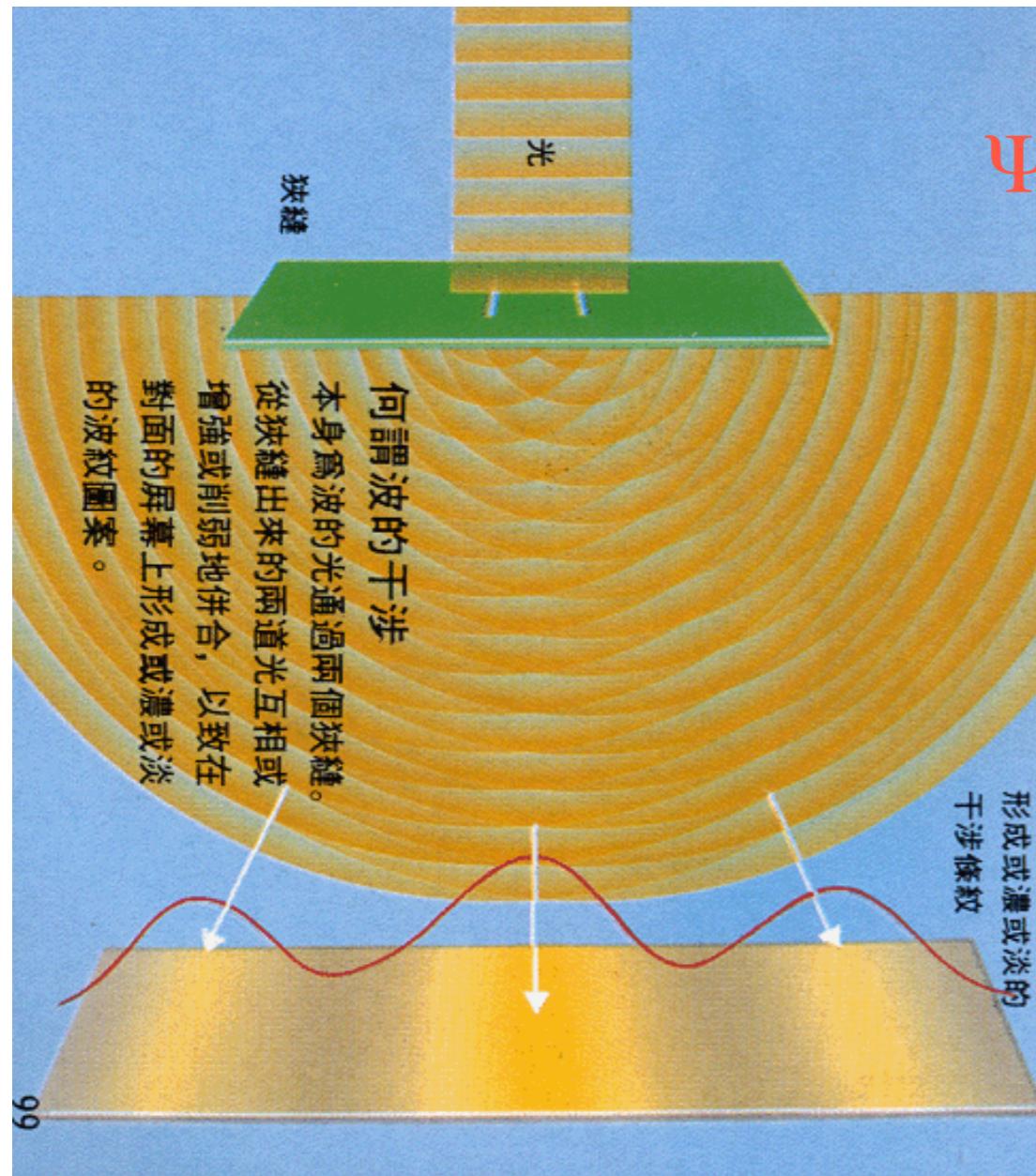
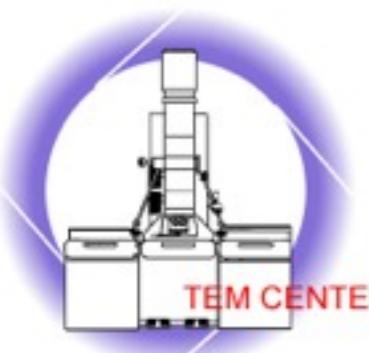
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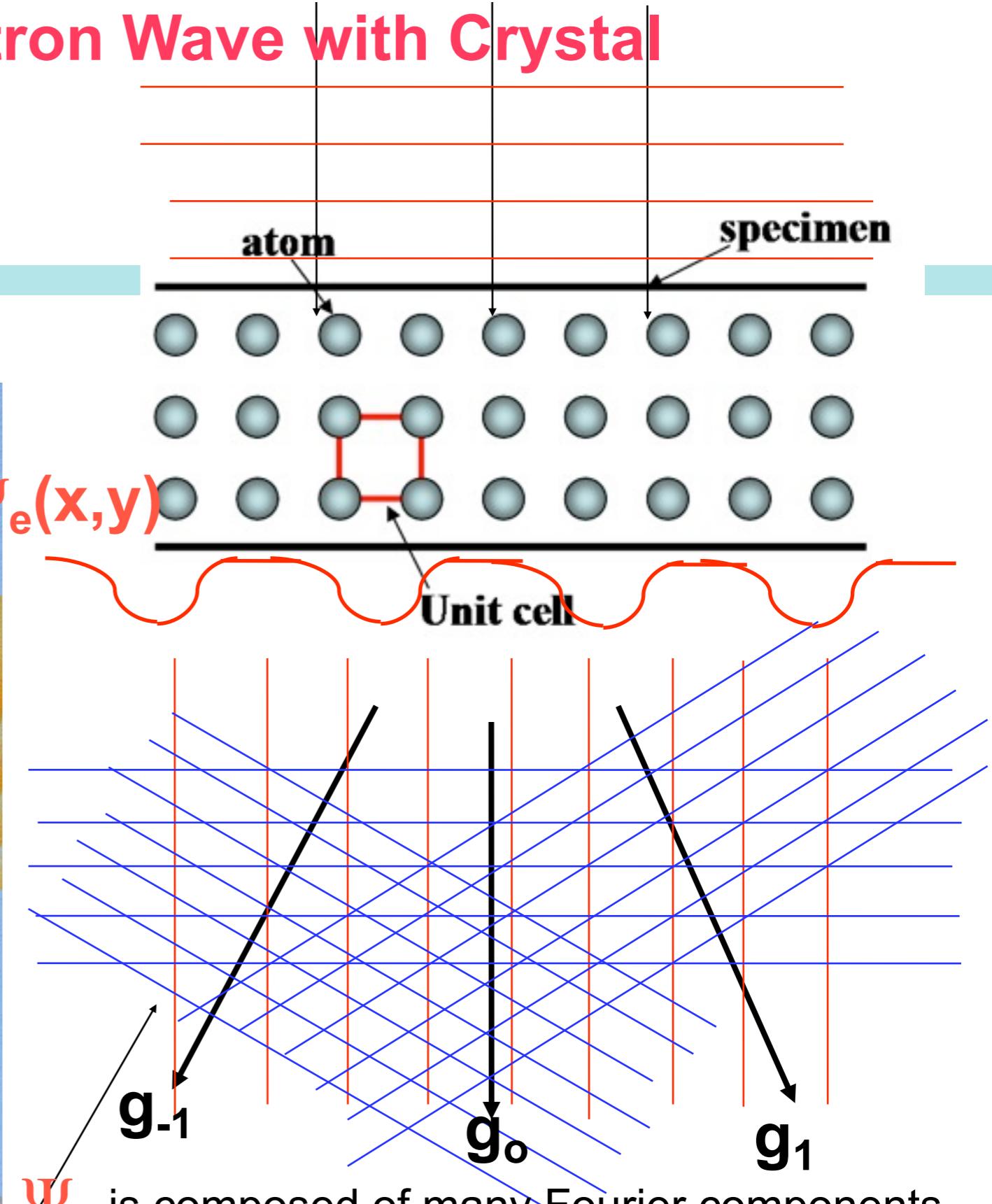
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# Interaction of Electron Wave with Crystal



亮線位置不一定與原子柱位置重疊



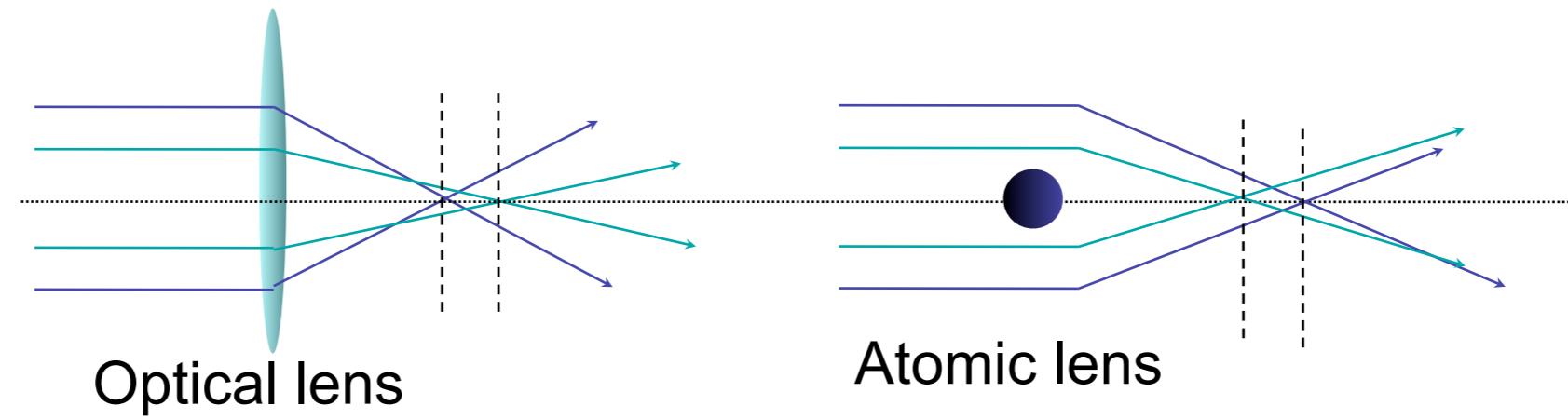
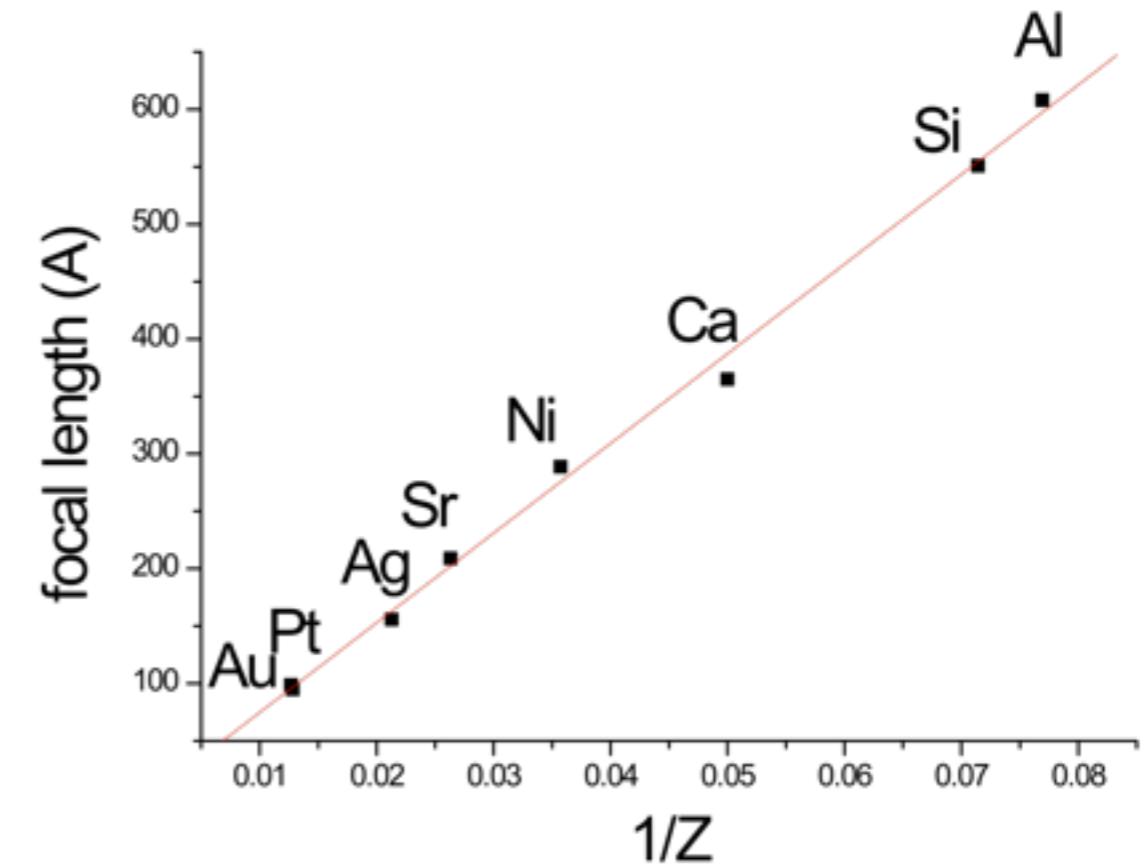
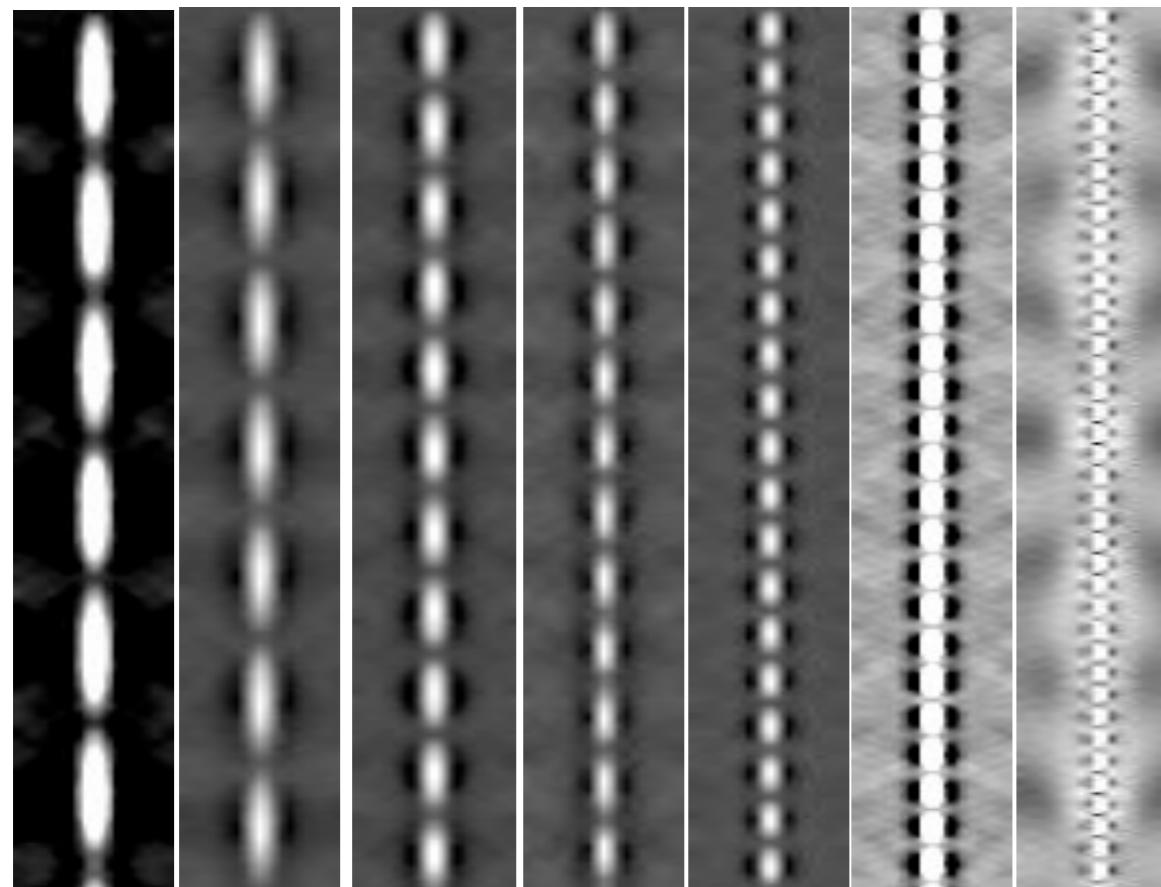
$$\Psi_e(x, y) = \sum_{H=-g}^g F(H) \exp(-2\pi H \cdot r)$$

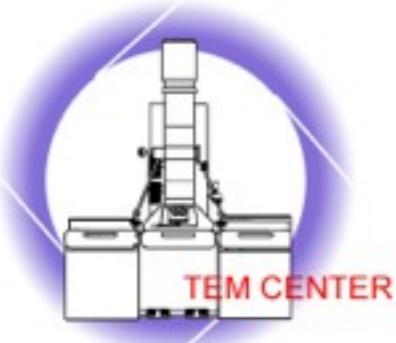
# Wave Propagates inside Crystal

## Channeling Theory

Al

Au

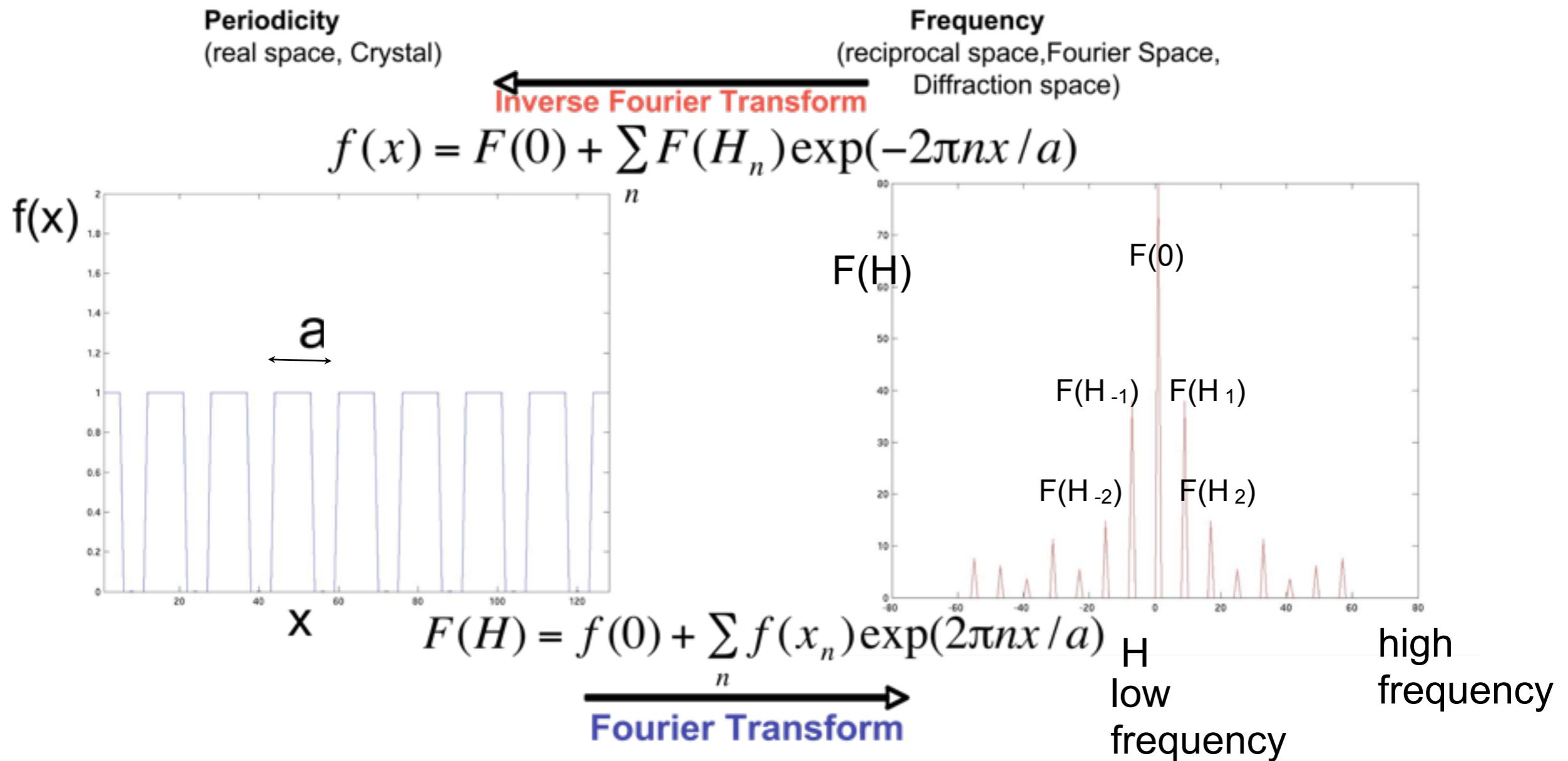




# Fourier Synthesis

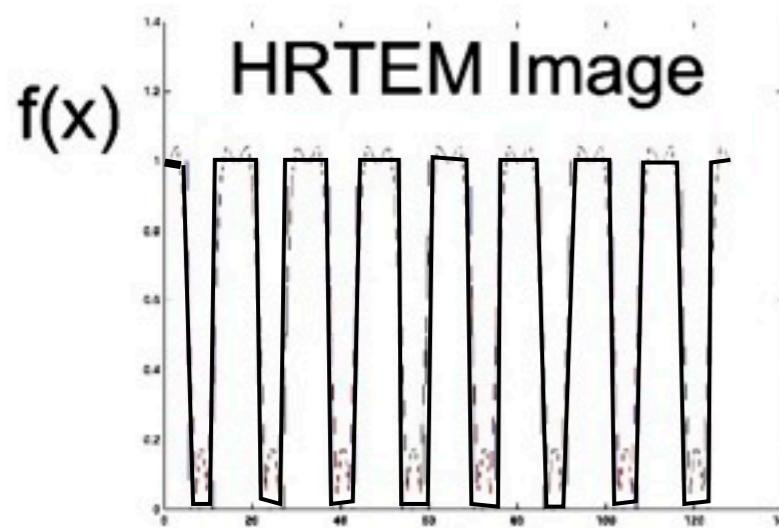
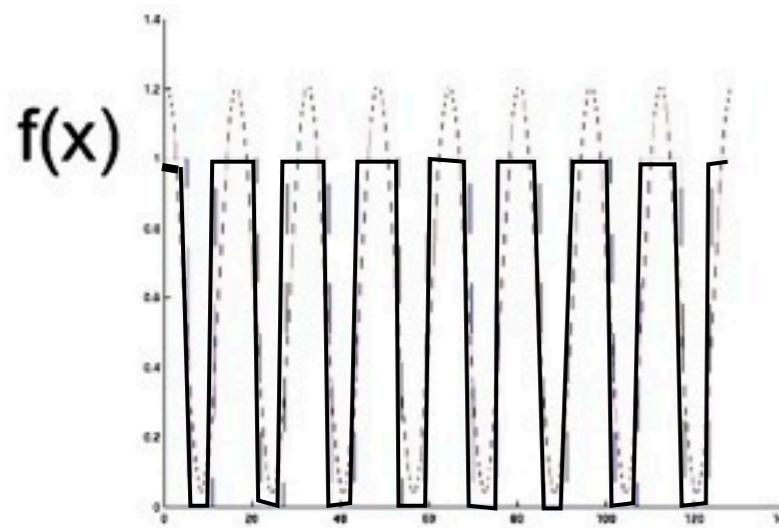
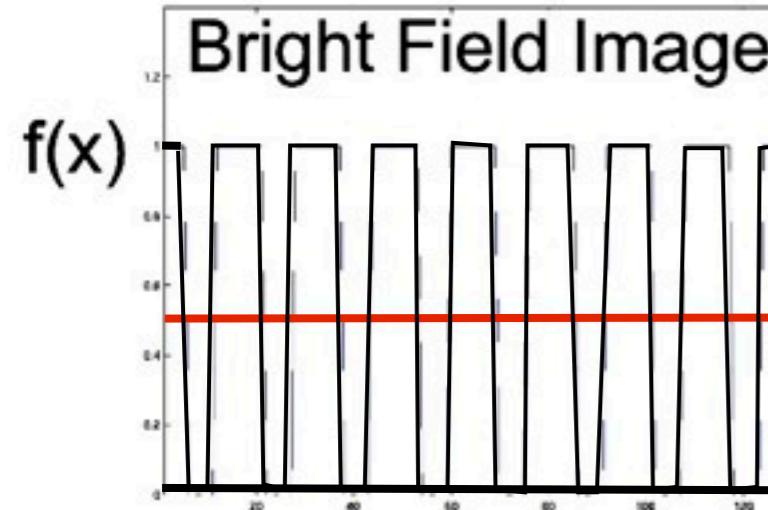
NTHU

A function  $f(x)$  can be expressed in terms of sum of a series of Fourier coefficients  $F(H)$  multiply by the sine (or cosine, or exponential) functions



**Periodicity**  
(real space, Crystal)

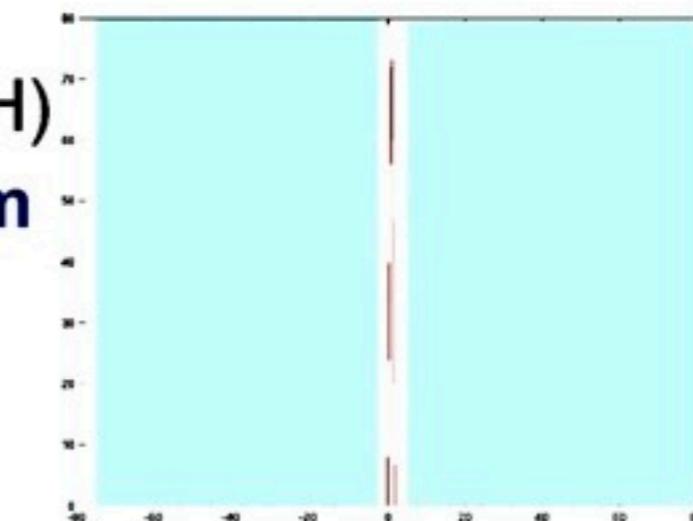
**Fourier Synthesis** **Frequency**  
(reciprocal space, Fourier Space,  
Diffraction space)



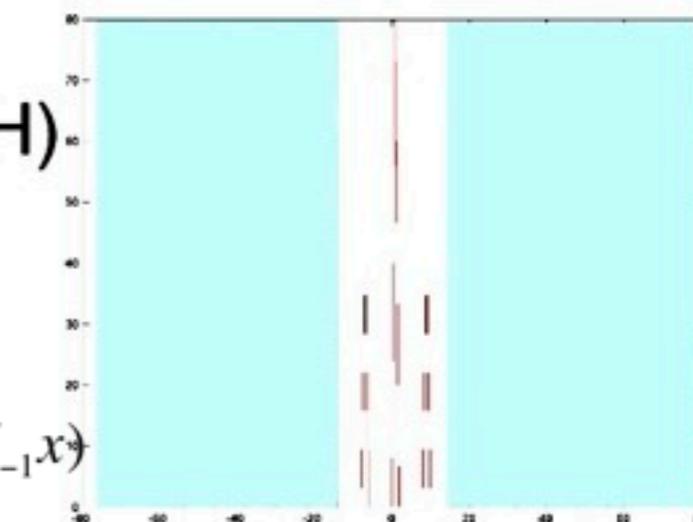
**Inverse Fourier Transform**



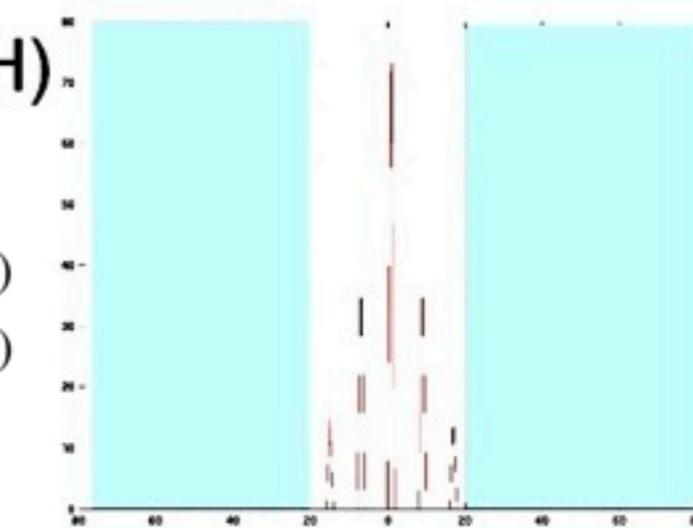
$$f(x) = F(0)\exp(-0x)$$



$$f(x) = F(0) + F(H_1)\exp(-H_1x) + F(H_{-1})\exp(-H_{-1}x)$$



$$f(x) = F(0) + F(H_1)\exp(-H_1x) + F(H_{-1})\exp(-H_{-1}x) + F(H_2)\exp(-H_2x) + F(H_{-2})\exp(-H_{-2}x)$$



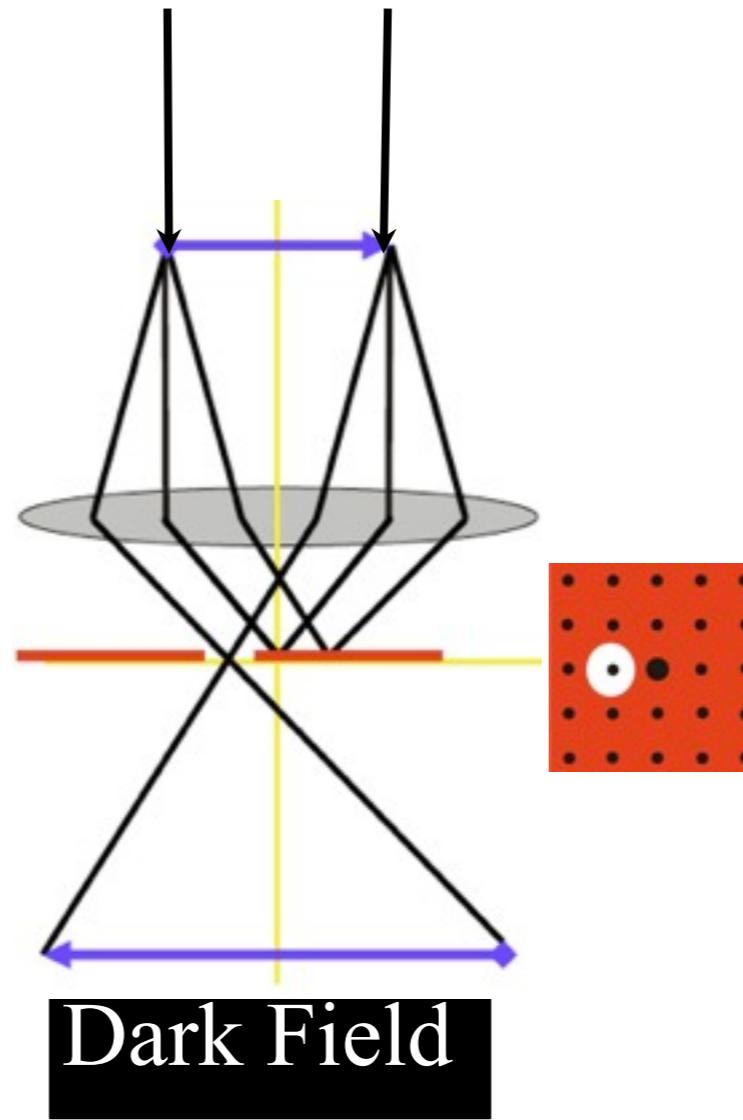
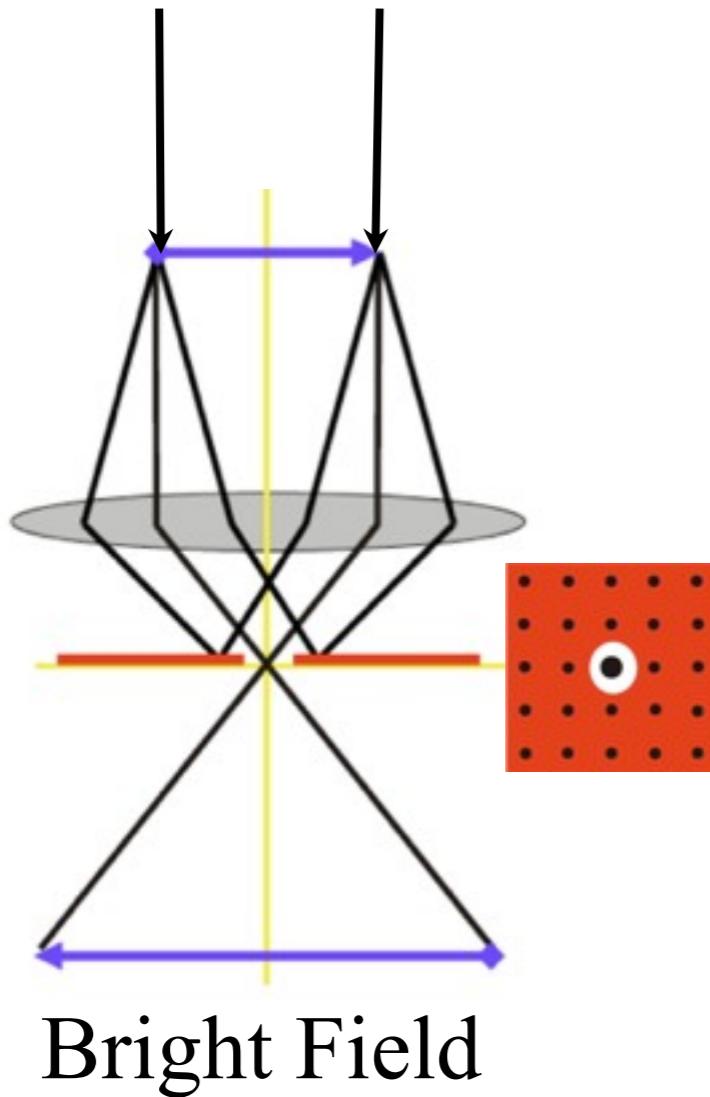
Low Frequency

High Frequency

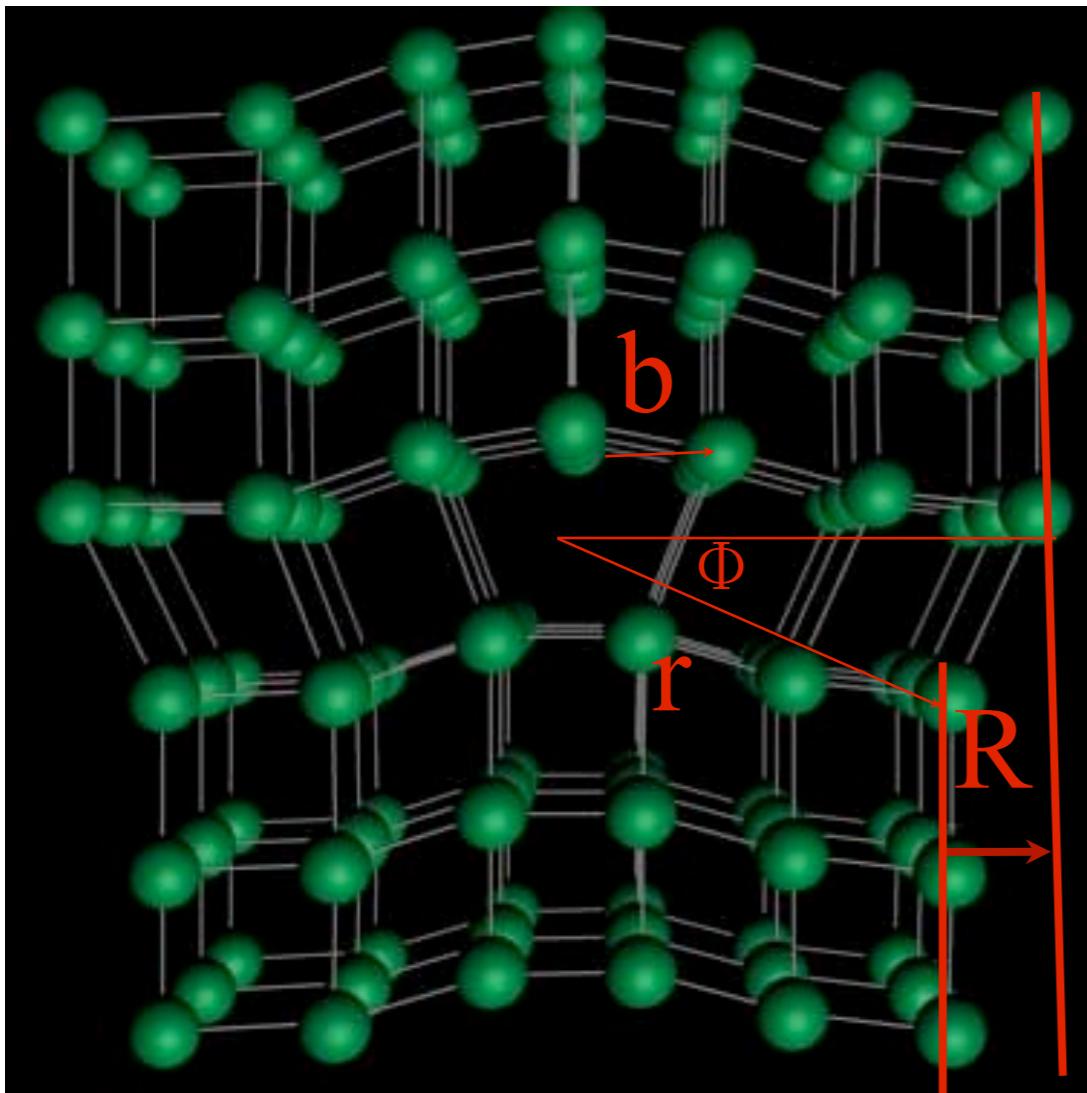
# Kinematic Contrast

---

- mass/ thickness contrast
- Bragg (orientation) contrast



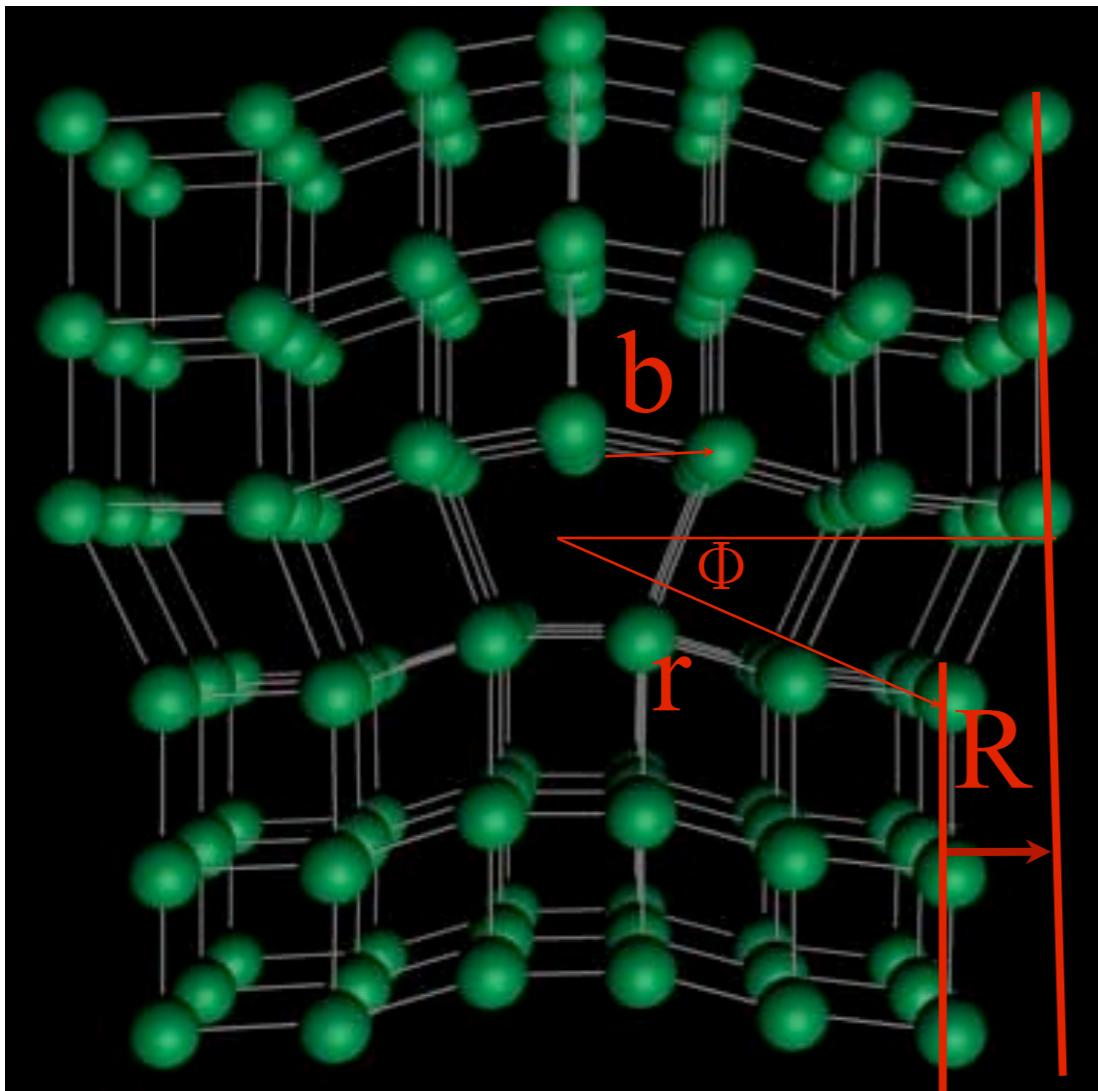
## 4.3.2 Line Defects



Edge Dislocation  
(邊刃差排)

$$R = \frac{1}{2\pi} \left[ b \frac{\sin 2\Phi}{4(1-\nu)} + (b \wedge u) \right] \left\{ \frac{1-2\nu}{2(1-\nu)} \ln r + \frac{\cos 2\Phi}{4(1-\nu)} \right\}$$

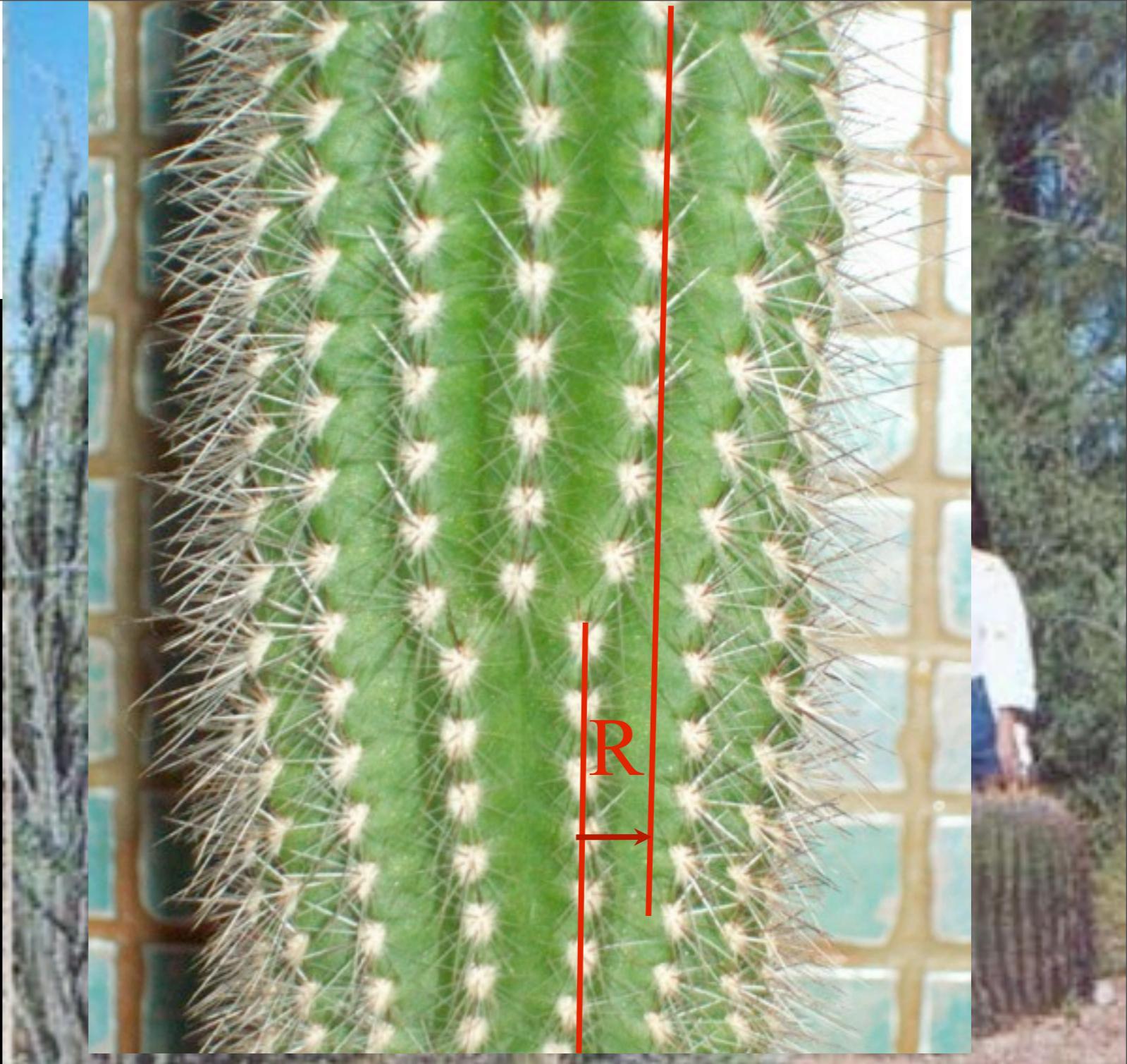
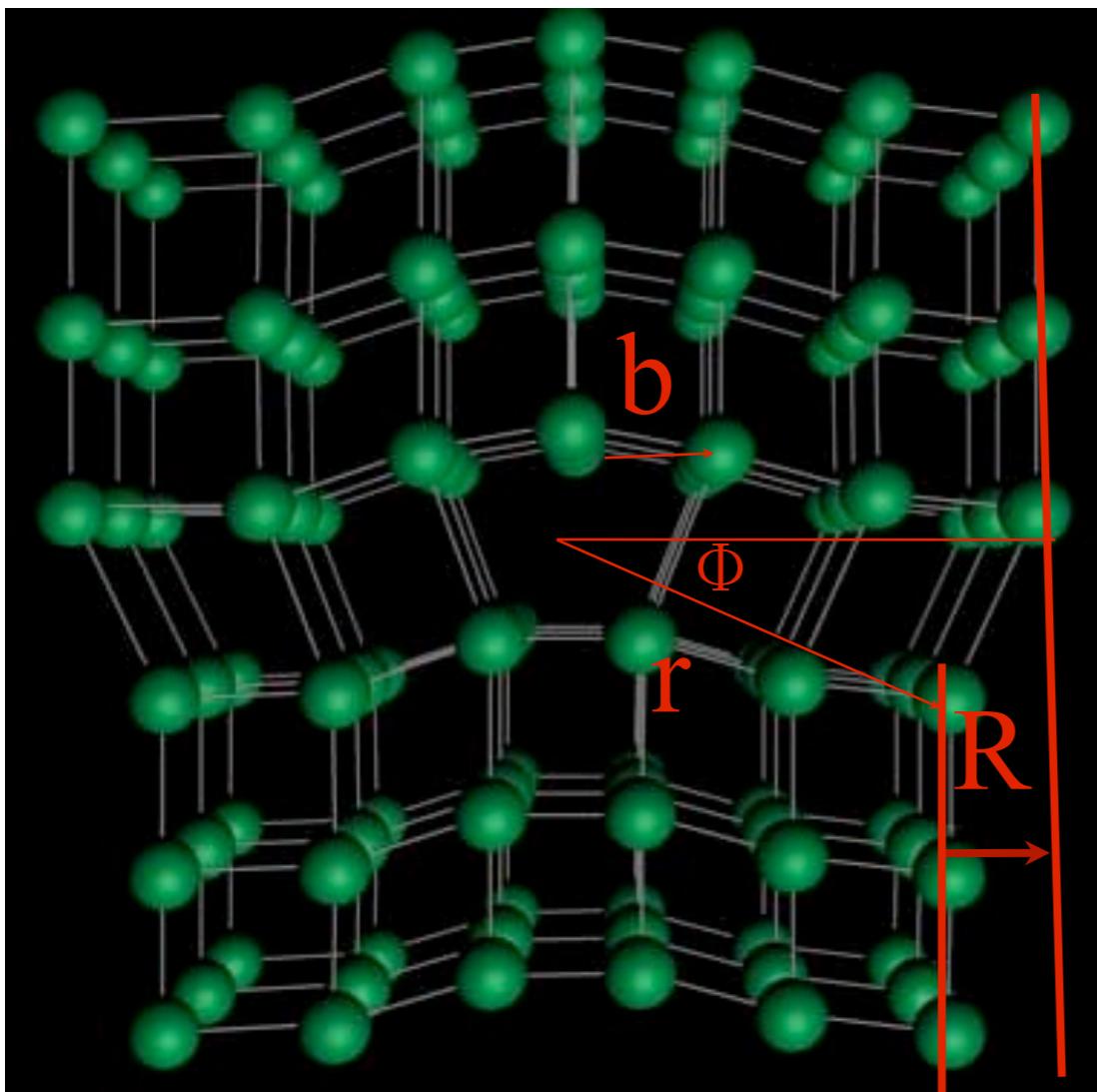
## 4.3.2 Line Defects



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$$R = \frac{1}{2\pi} \left[ b \frac{\sin 2\Phi}{4(1-\nu)} + (b \wedge u) \right] \left\{ \frac{1-2\nu}{2(1-\nu)} \ln r + \frac{\cos 2\Phi}{4(1-\nu)} \right\}$$

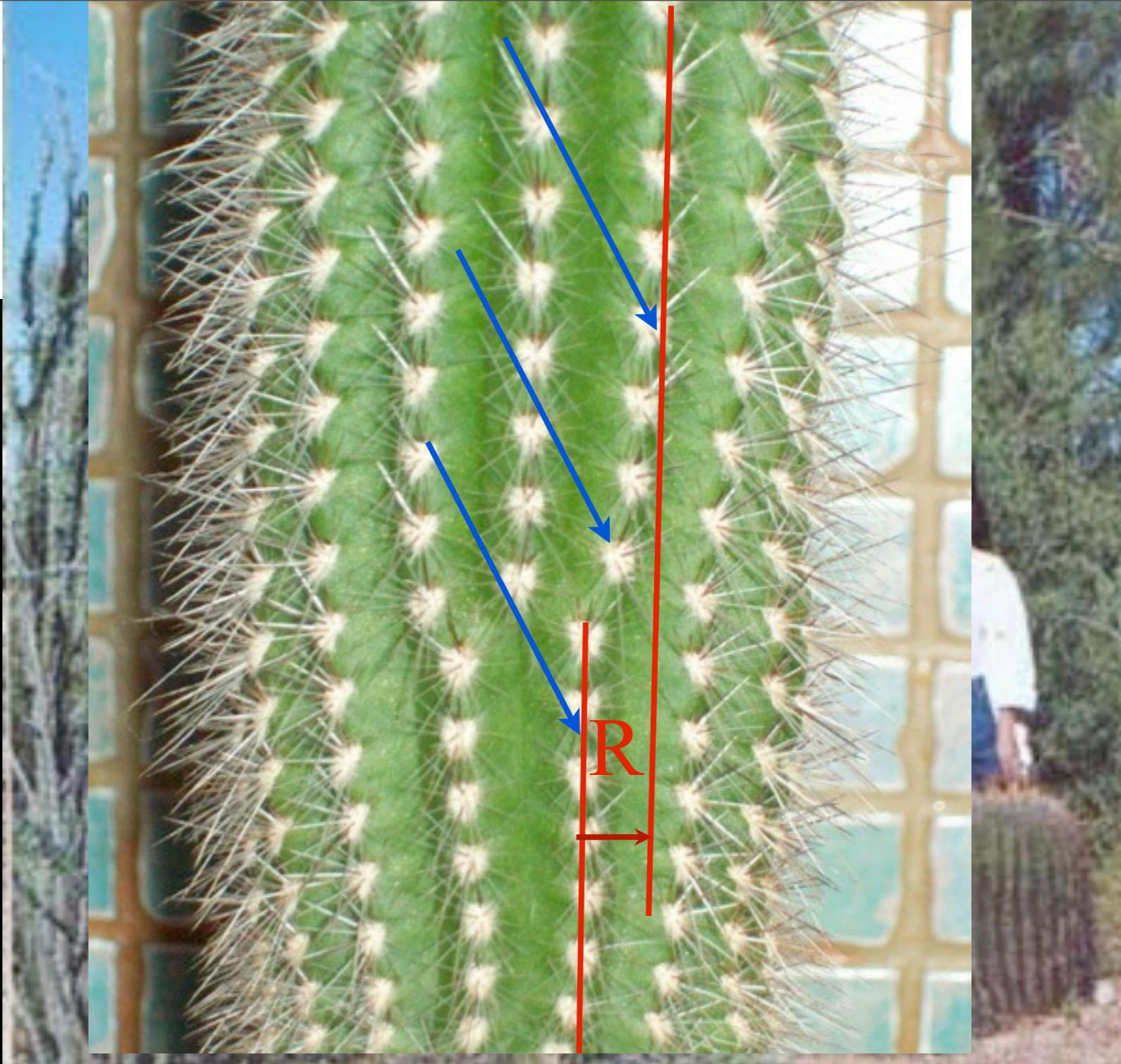
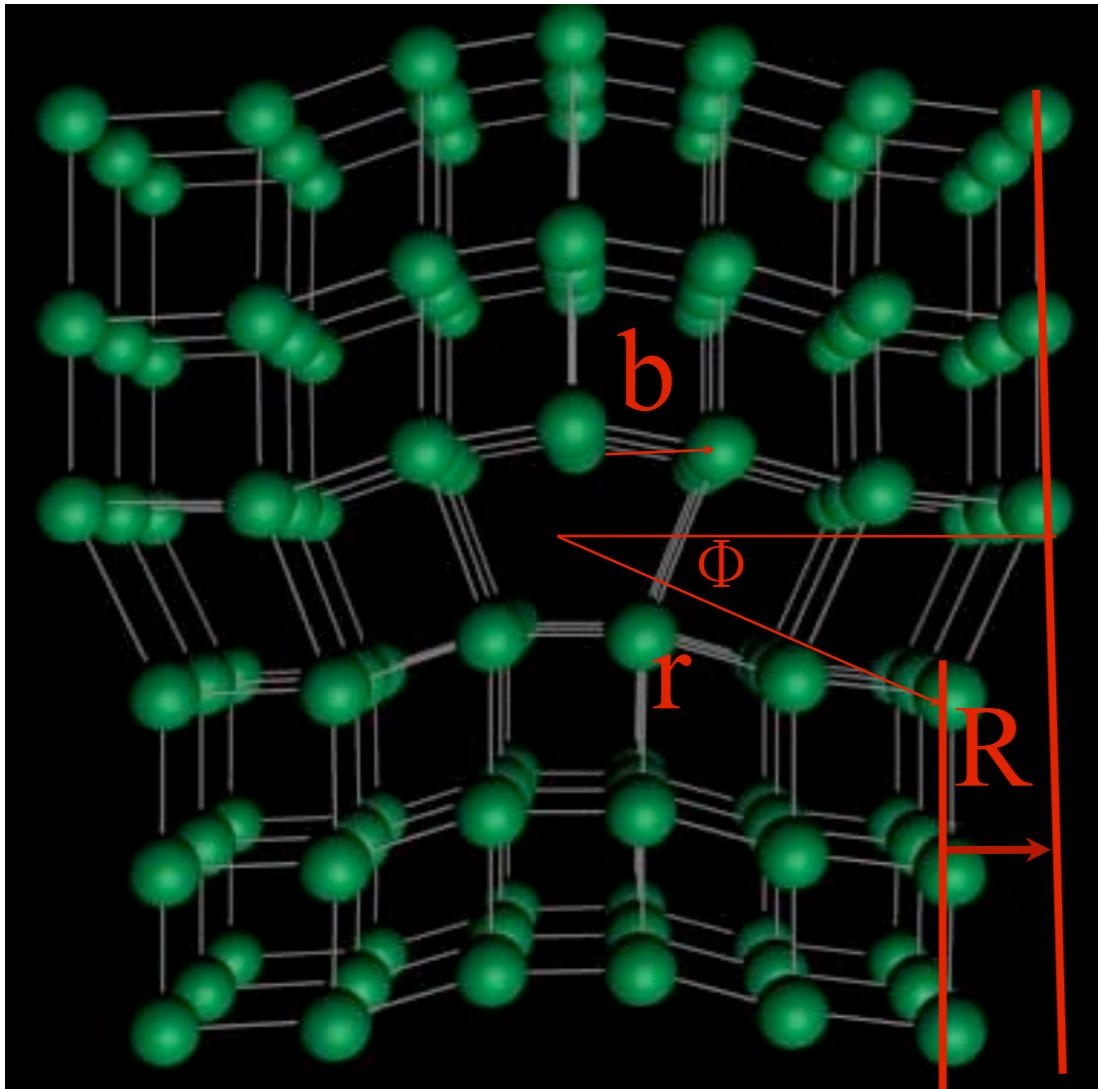
## 4.3.2 Line Defects



Edge Dislocation  
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$$R = \frac{1}{2\pi} \left[ b \frac{\sin 2\Phi}{4(1-\nu)} + (b \wedge u) \right] \left\{ \frac{1-2\nu}{2(1-\nu)} \ln r + \frac{\cos 2\Phi}{4(1-\nu)} \right\}$$

## 4.3.2 Line Defects



Edge Dislocation  
(邊刃差排)

g-R 引起的方向變化

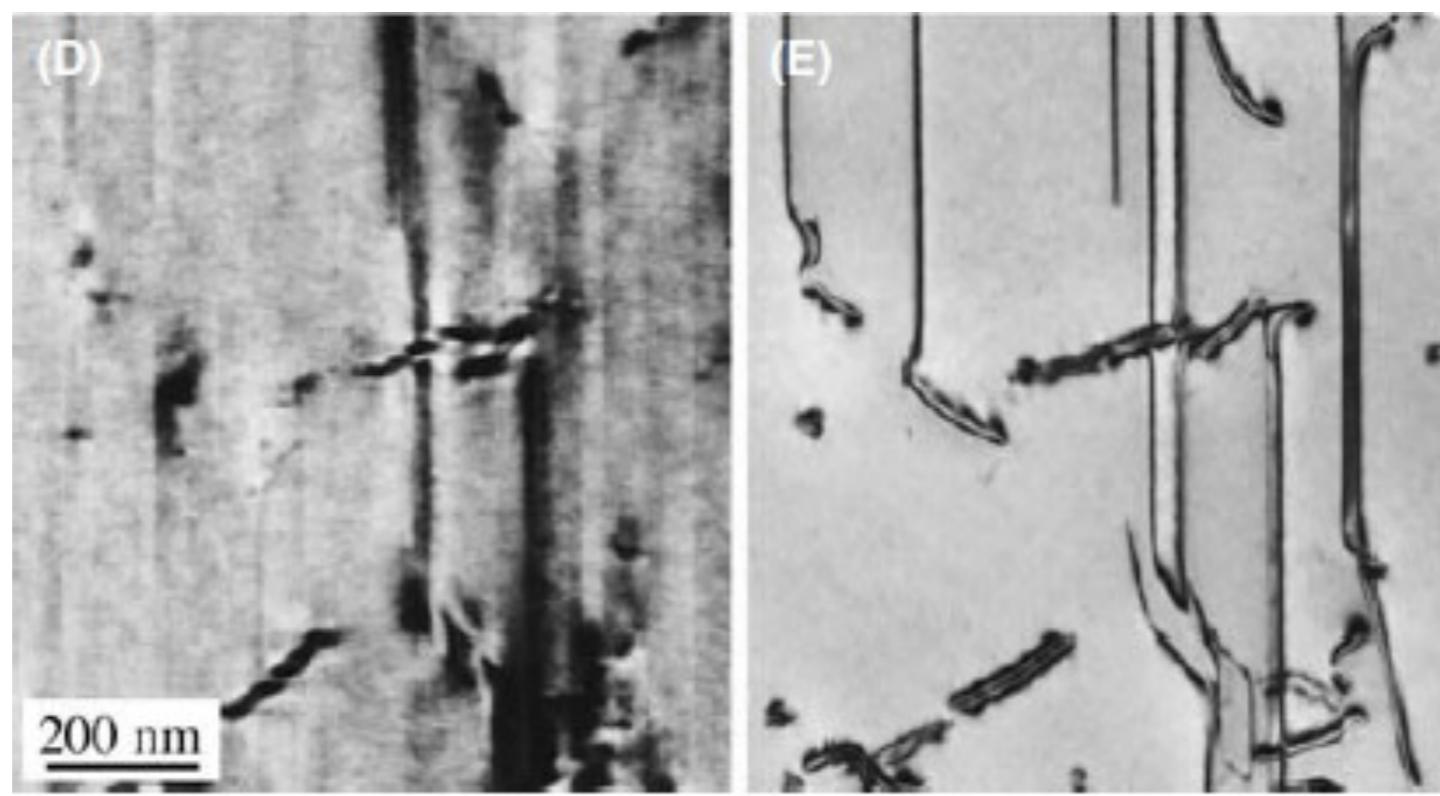
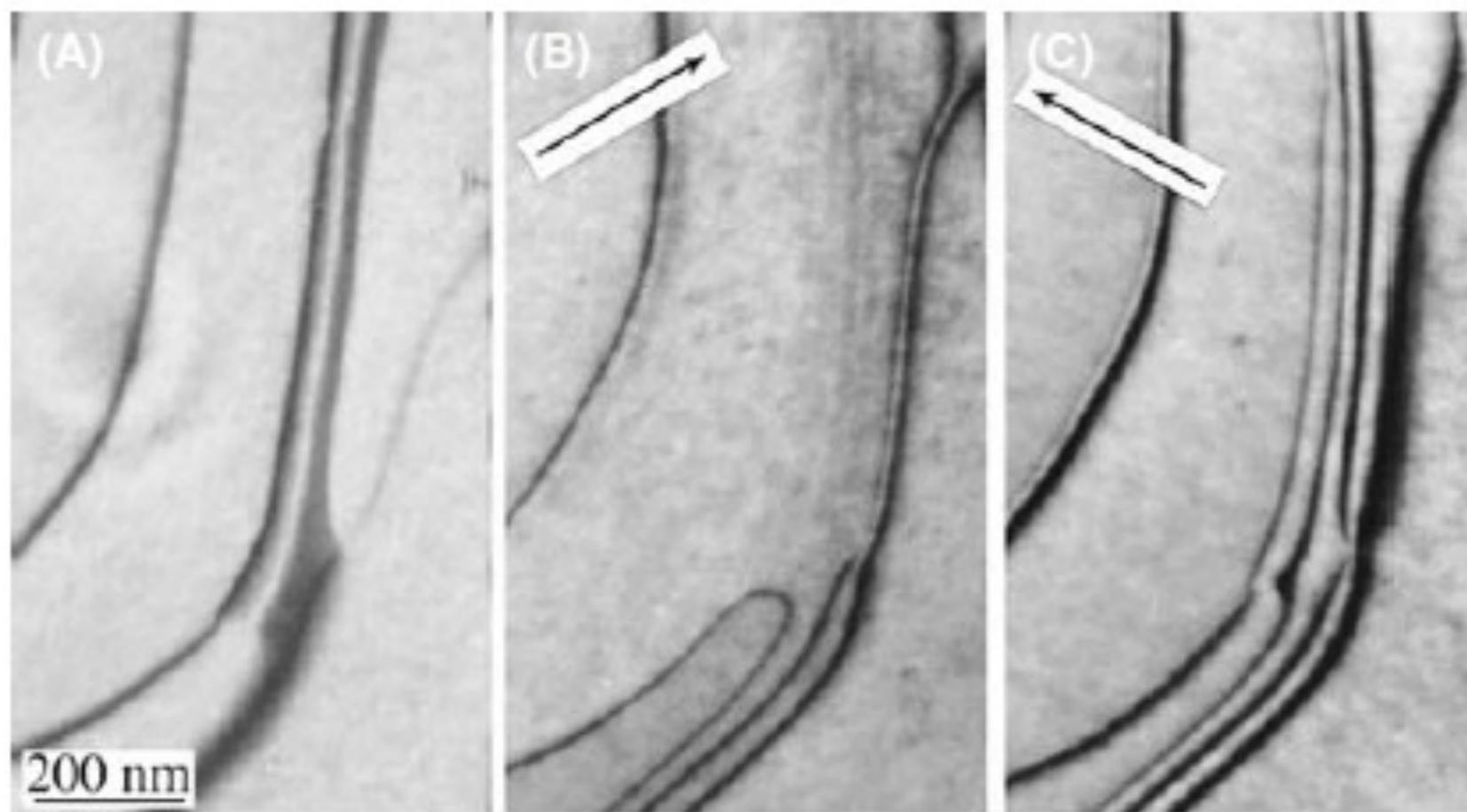
$$R = \frac{1}{2\pi} \left[ b \frac{\sin 2\Phi}{4(1-\nu)} + (b \wedge u) \right] \left\{ \frac{1-2\nu}{2(1-\nu)} \ln r + \frac{\cos 2\Phi}{4(1-\nu)} \right\}$$



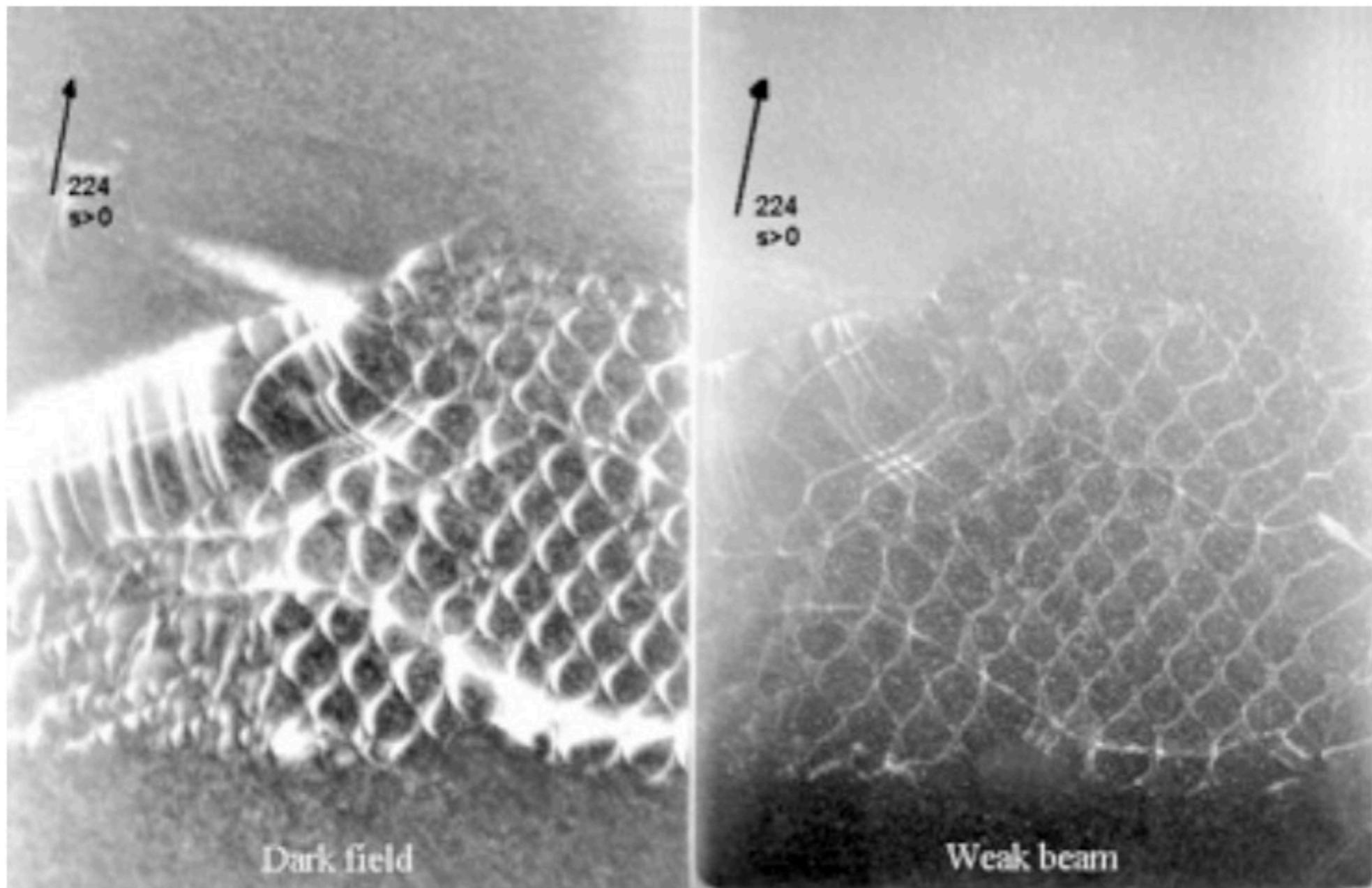




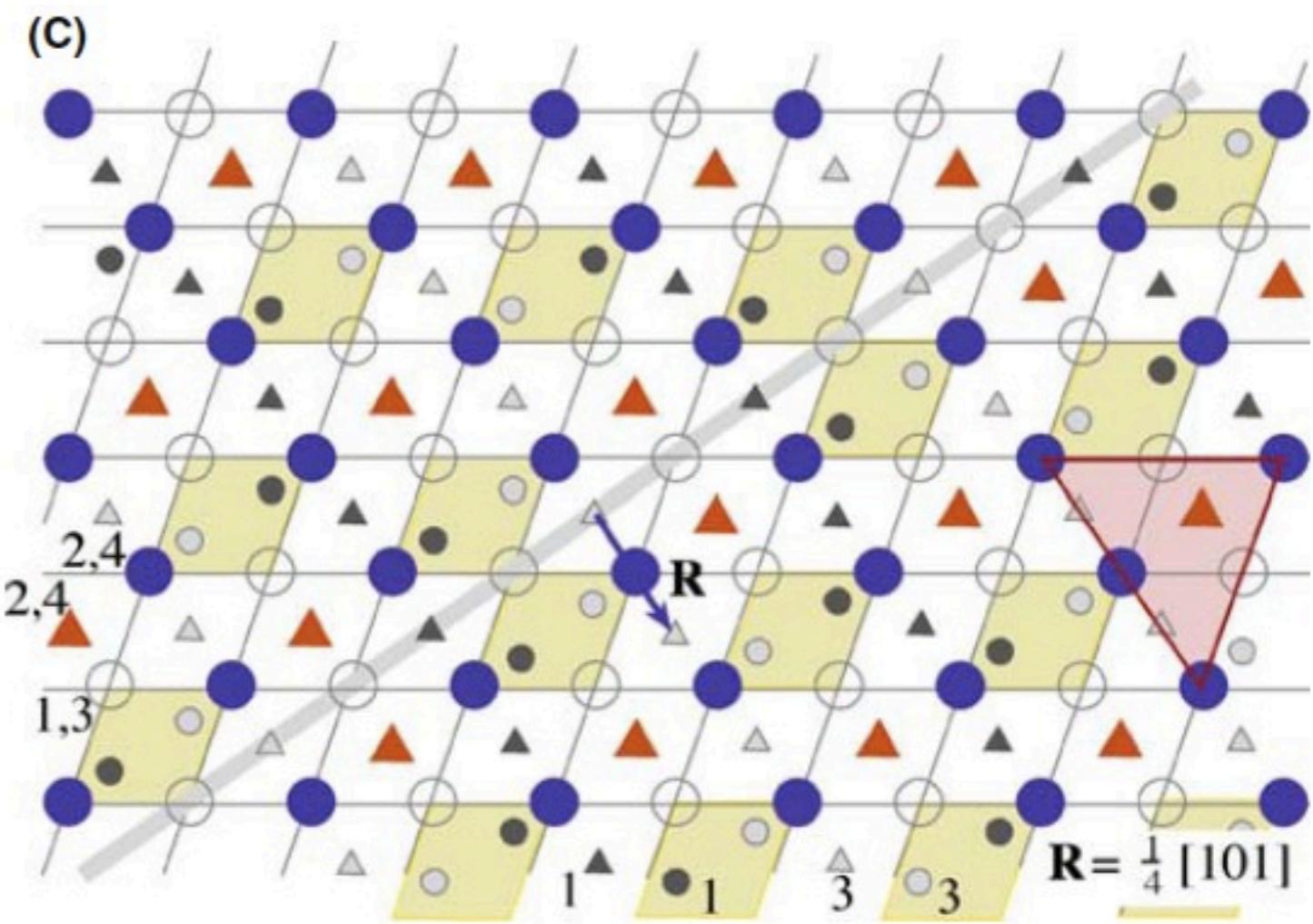
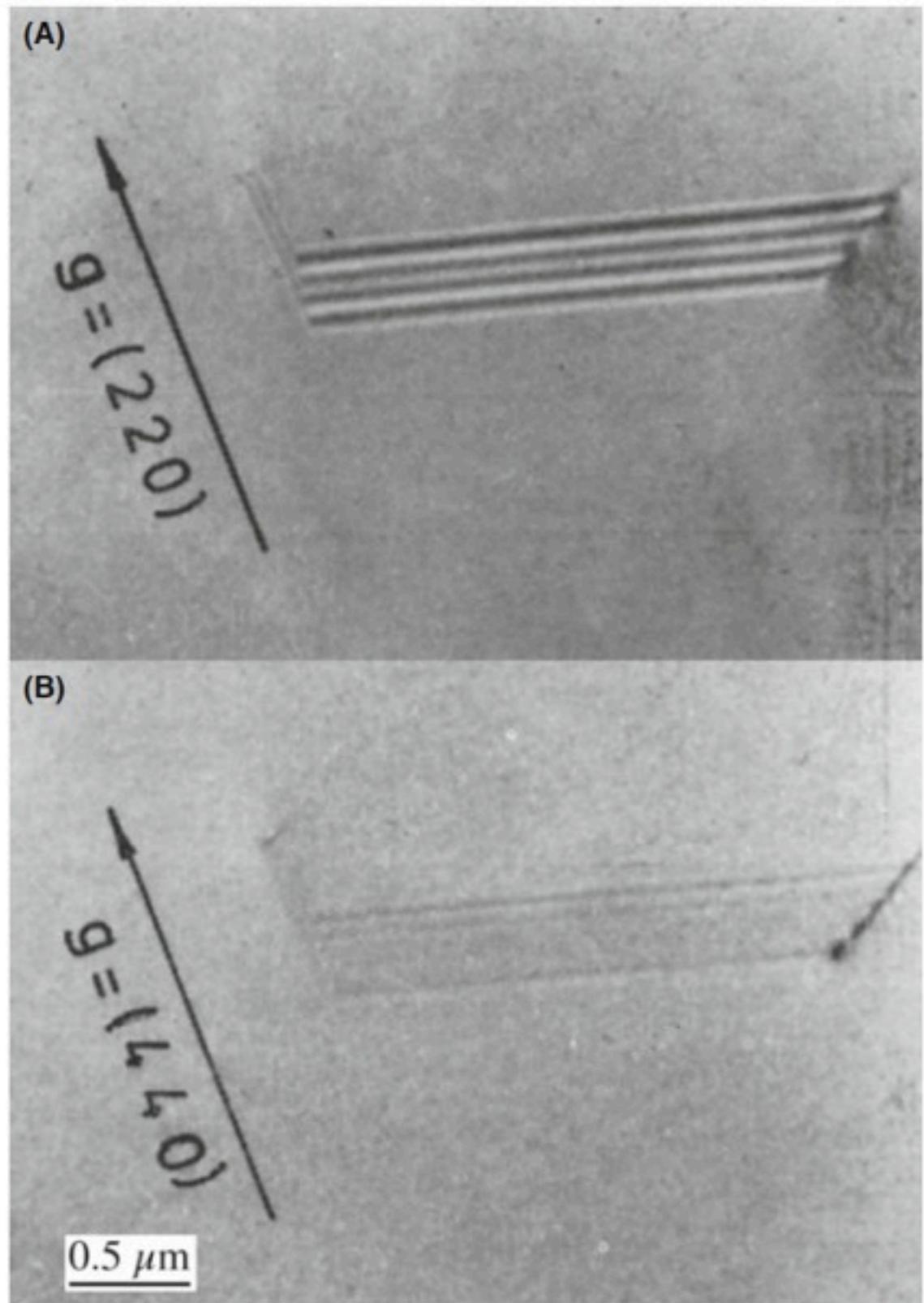
22



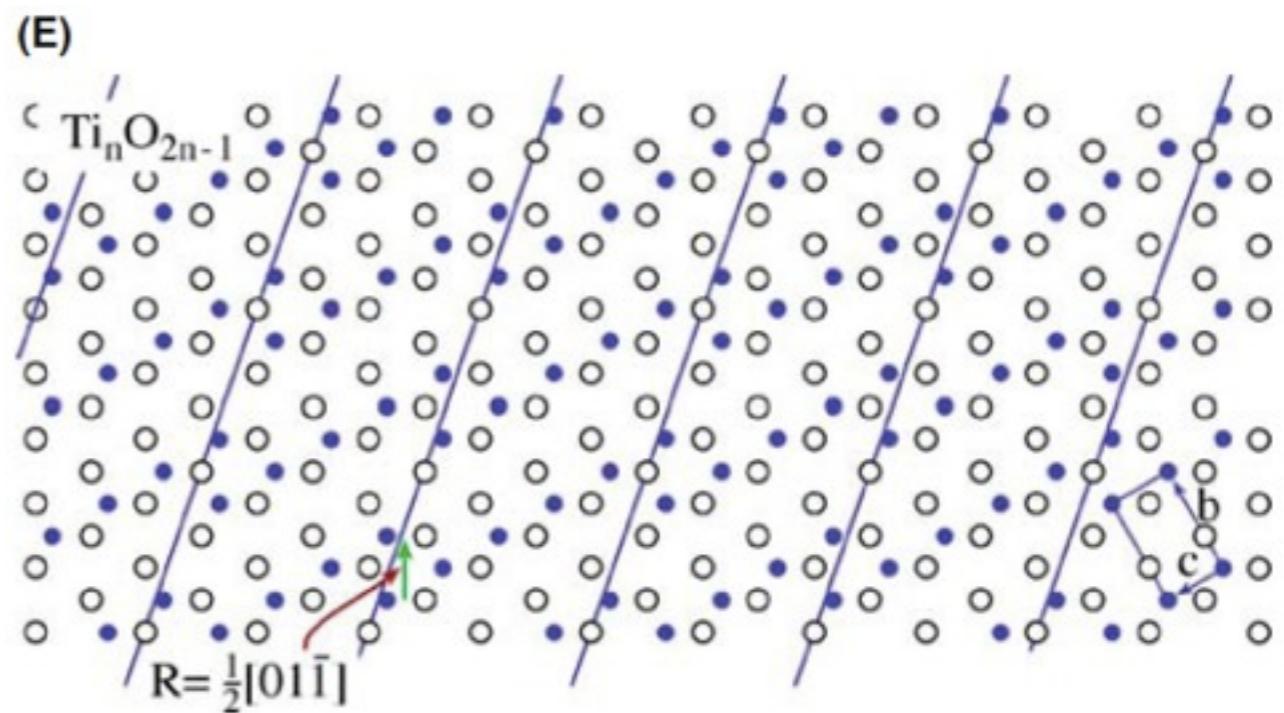
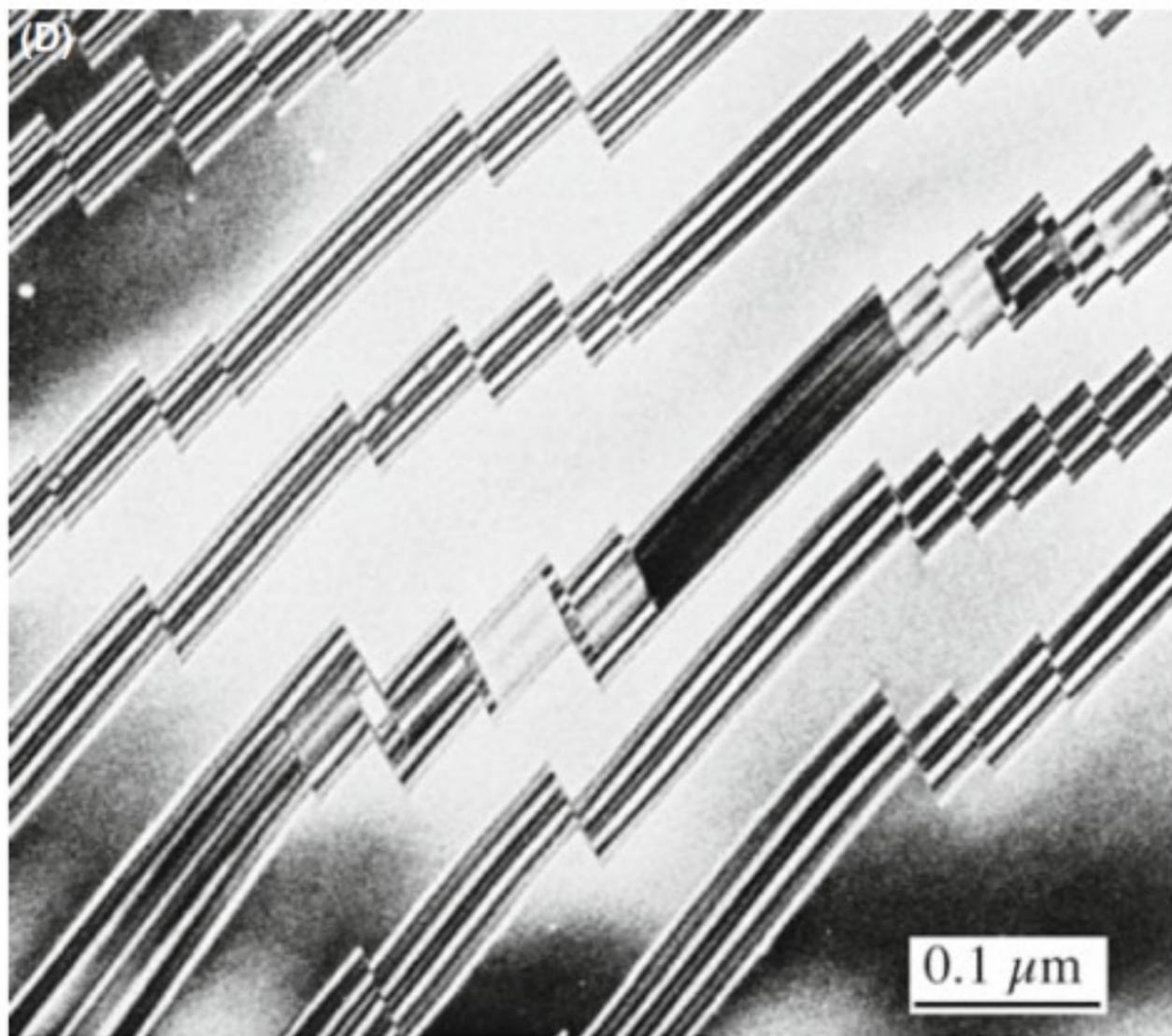
# Dark field and Weak beam



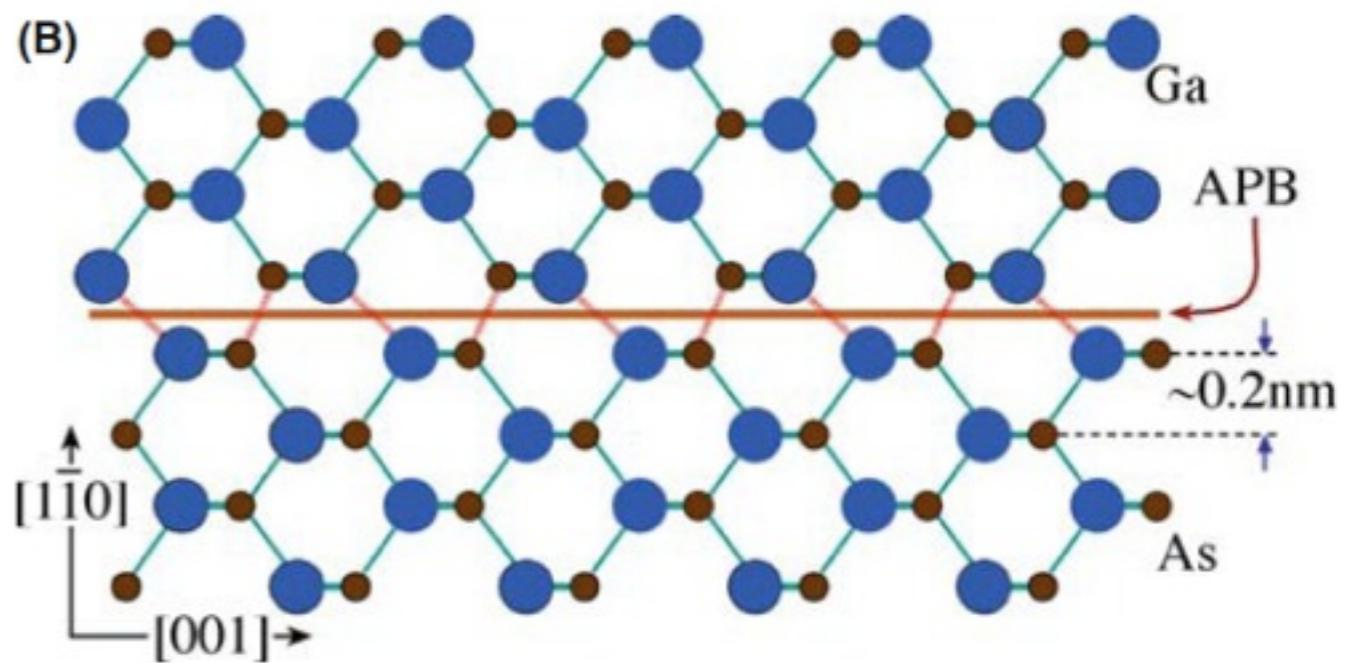
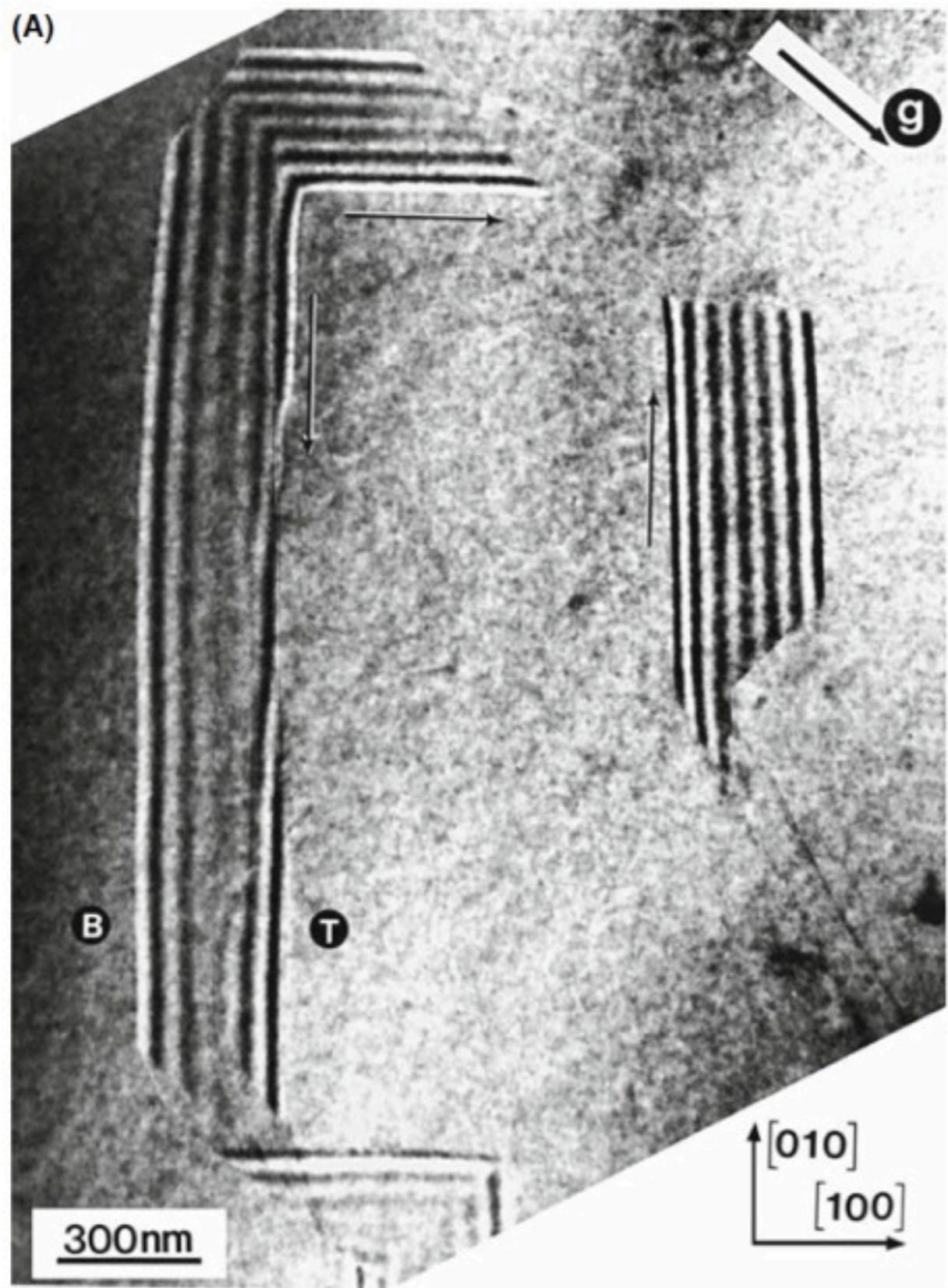
# APBs in $\text{TiO}_2$

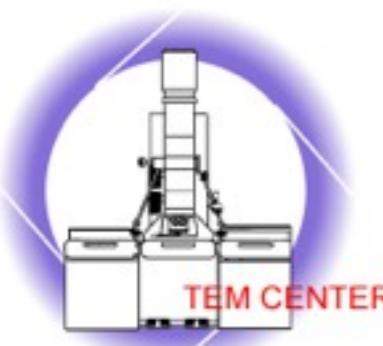


# APBs in $\text{TiO}_2$



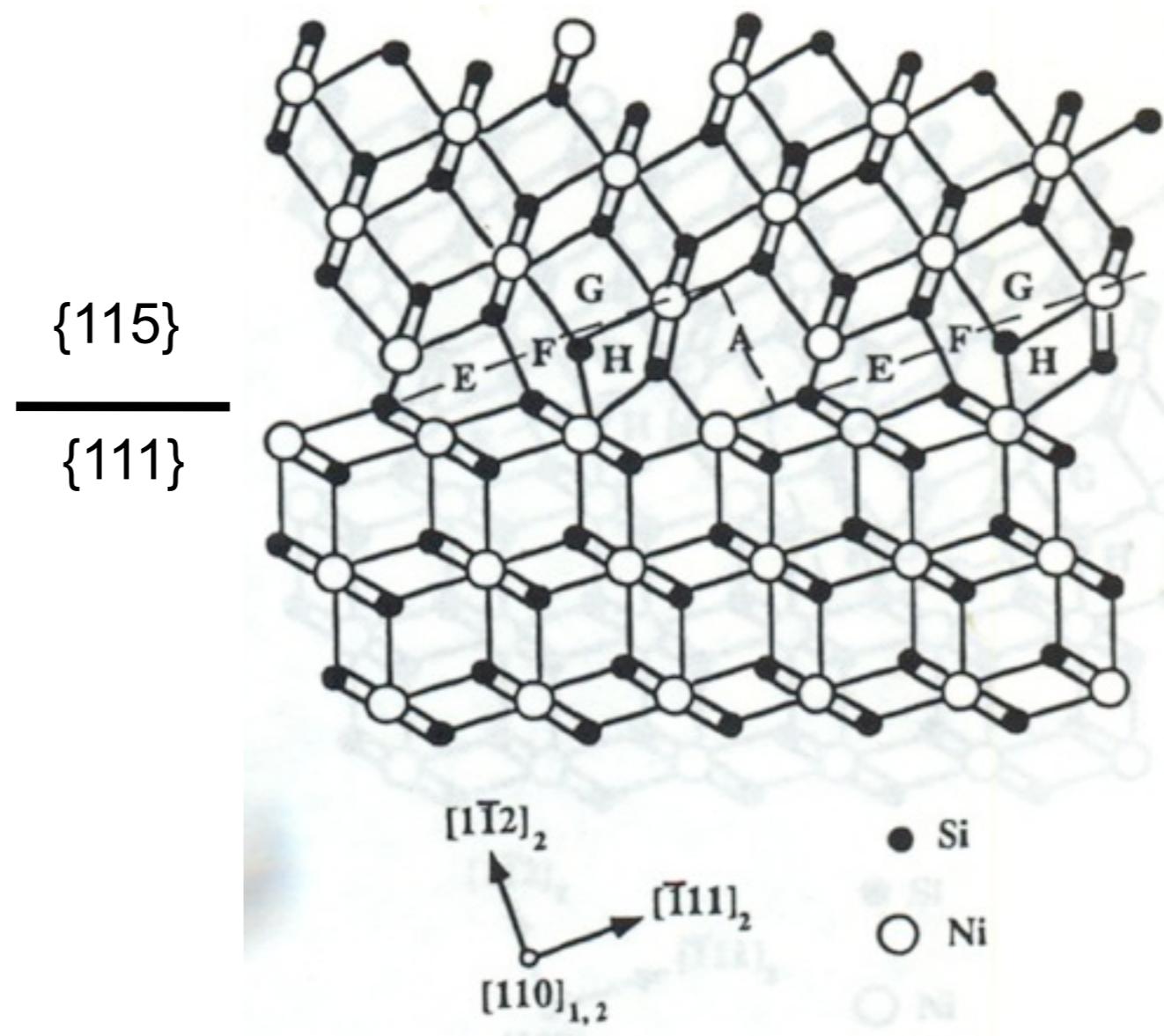
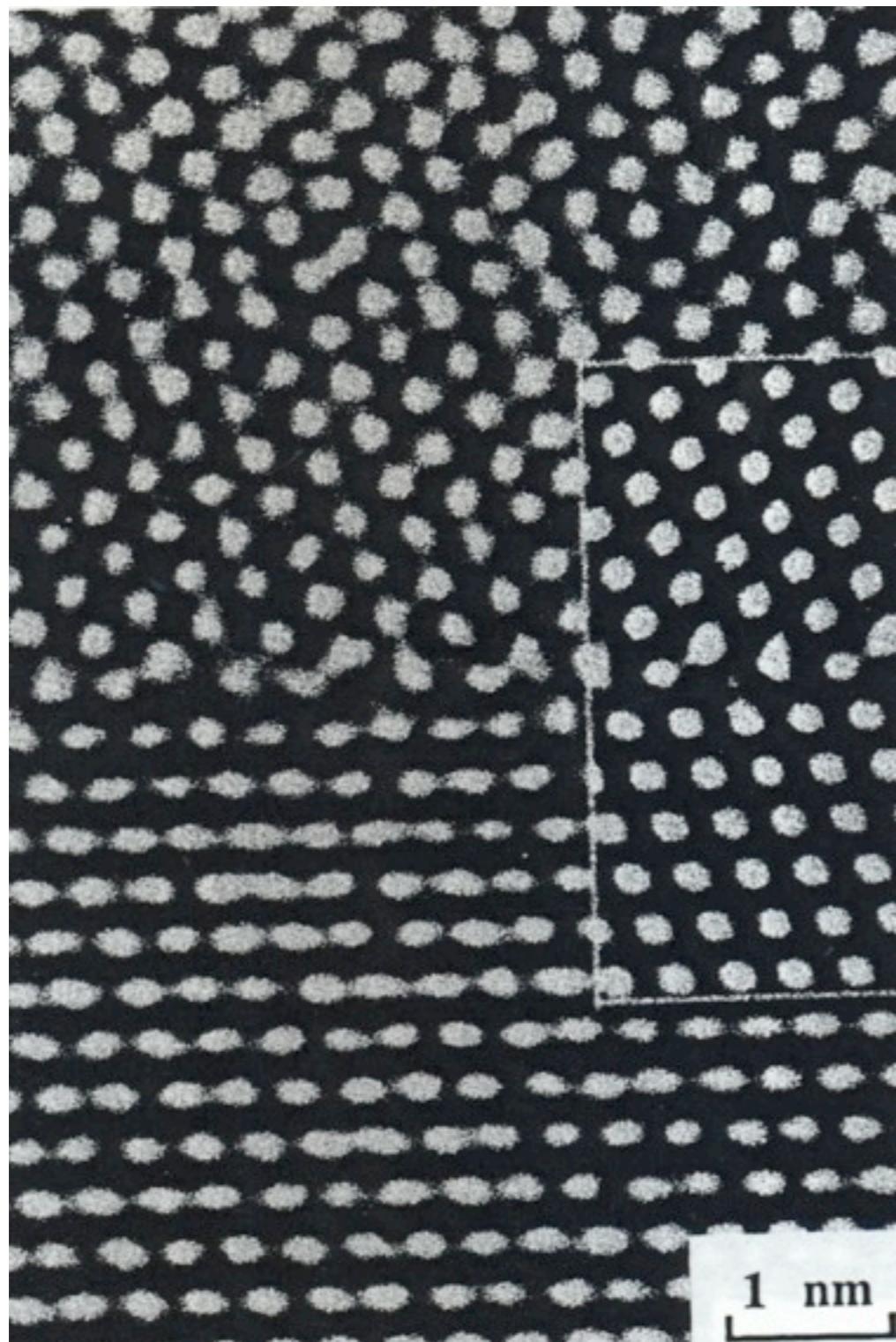
# APB (or IDB) of GaAs

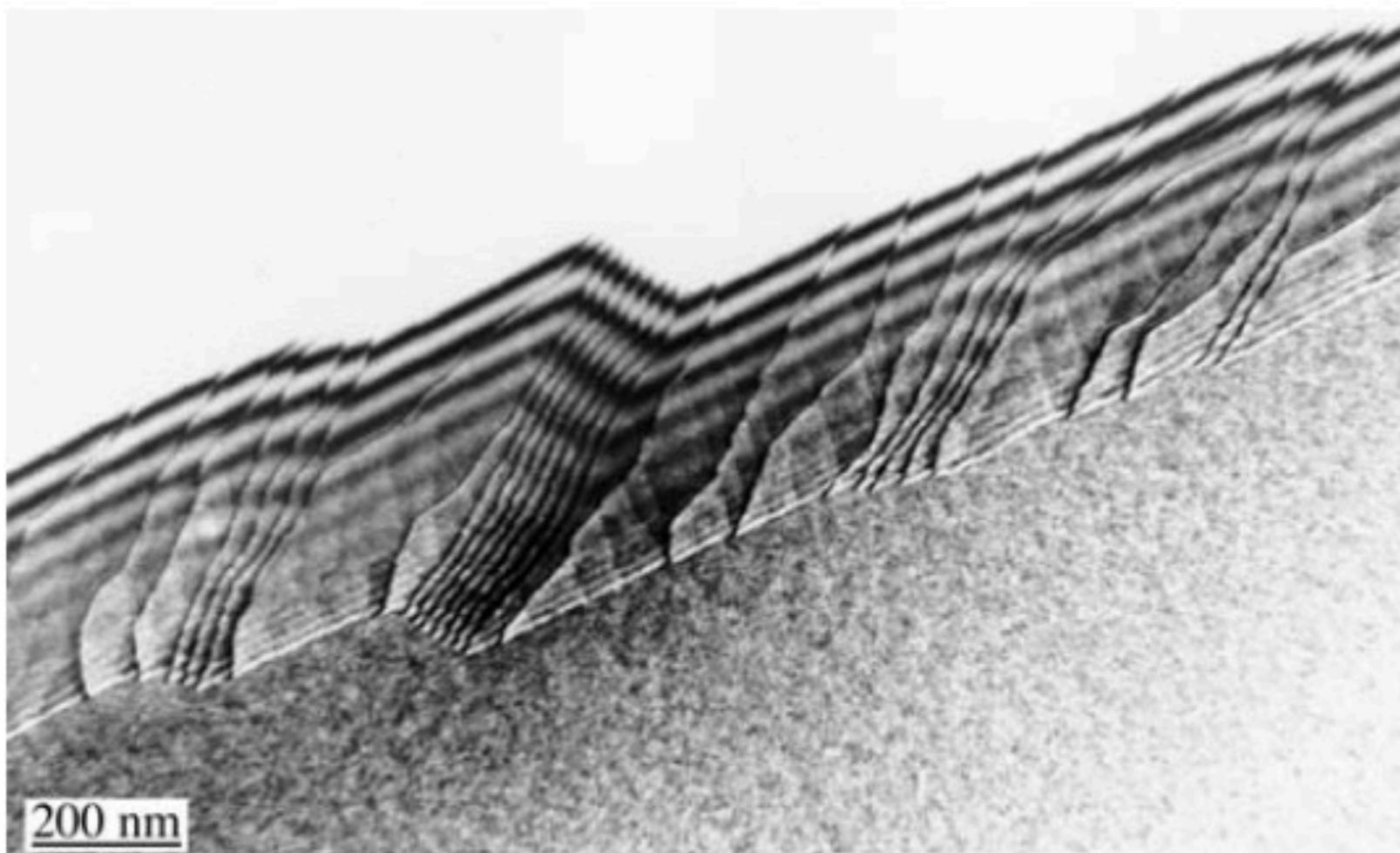




## Example: $\text{NiSi}_2$ $\{115\}/\{111\}$ Twin Boundary

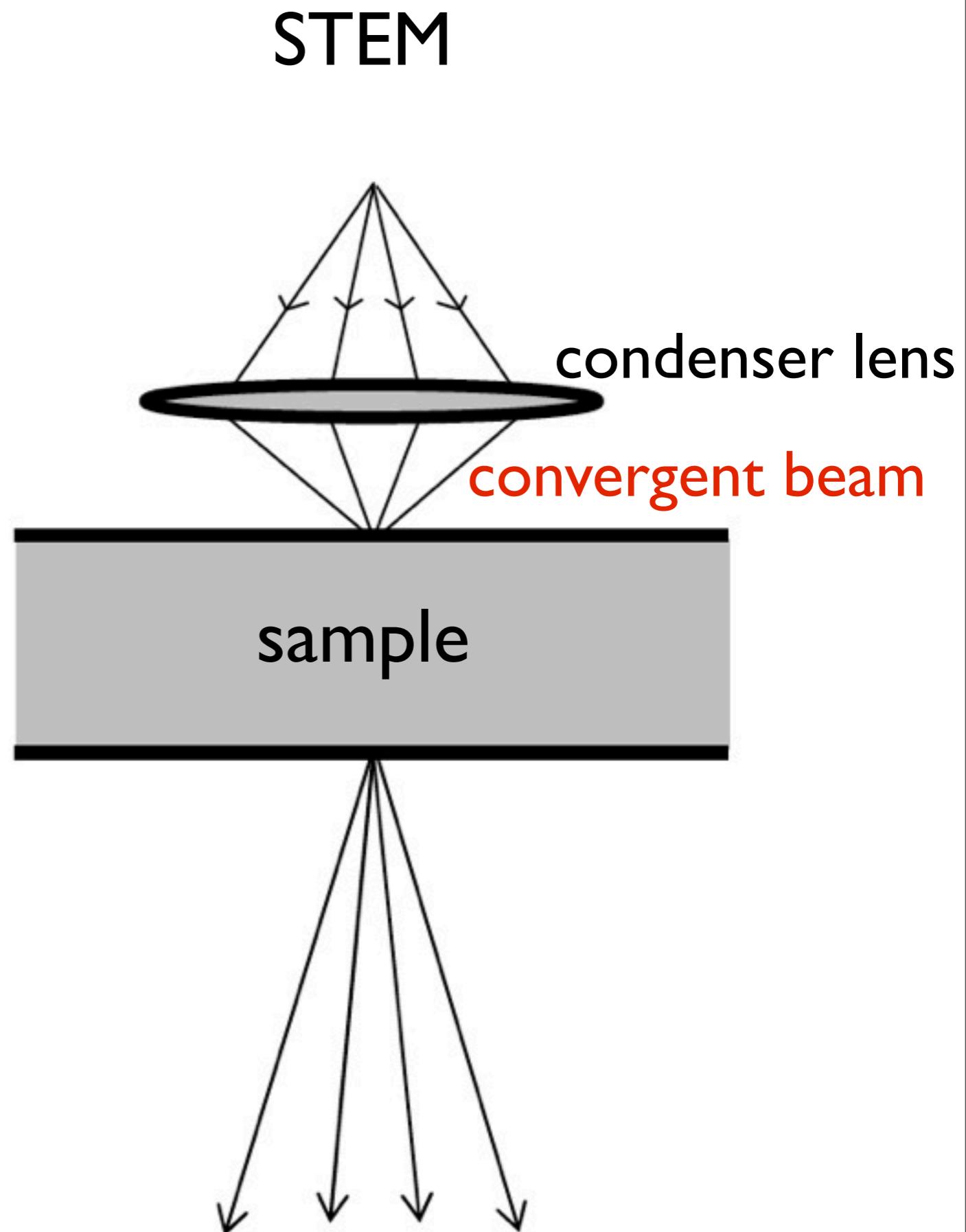
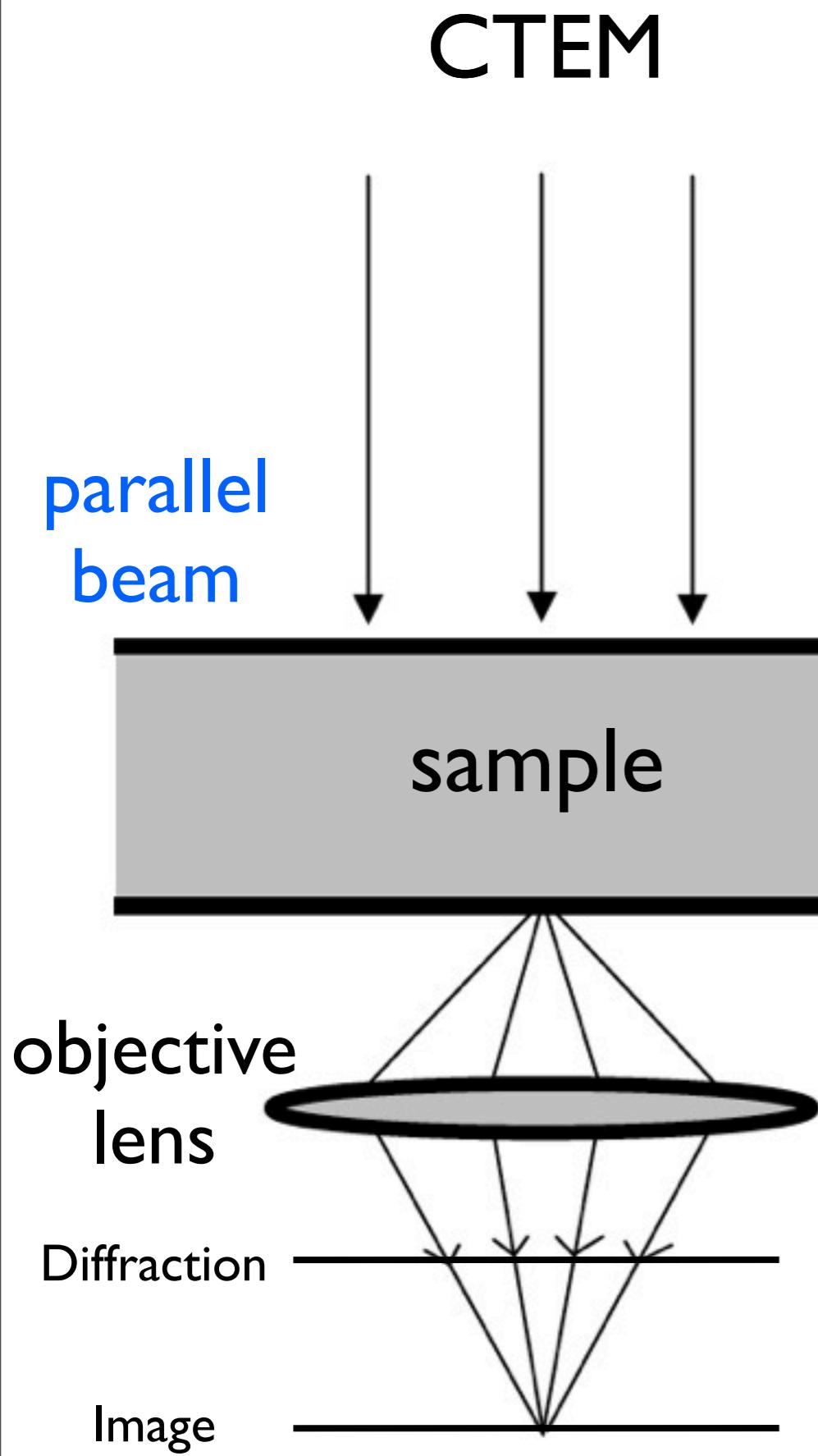
NTHU

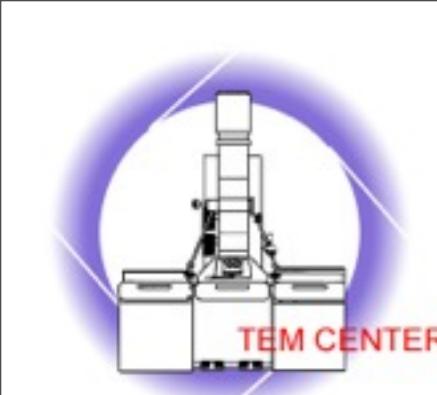




**FIGURE 26.21.** Steps at interfaces may also cause diffraction contrast when associated with strain. In this Ge specimen, the steps displace the thickness fringes in the GB so they are readily visible. The fringe spacing is different at the top and bottom of the boundary because the diffraction conditions are different at each grain.

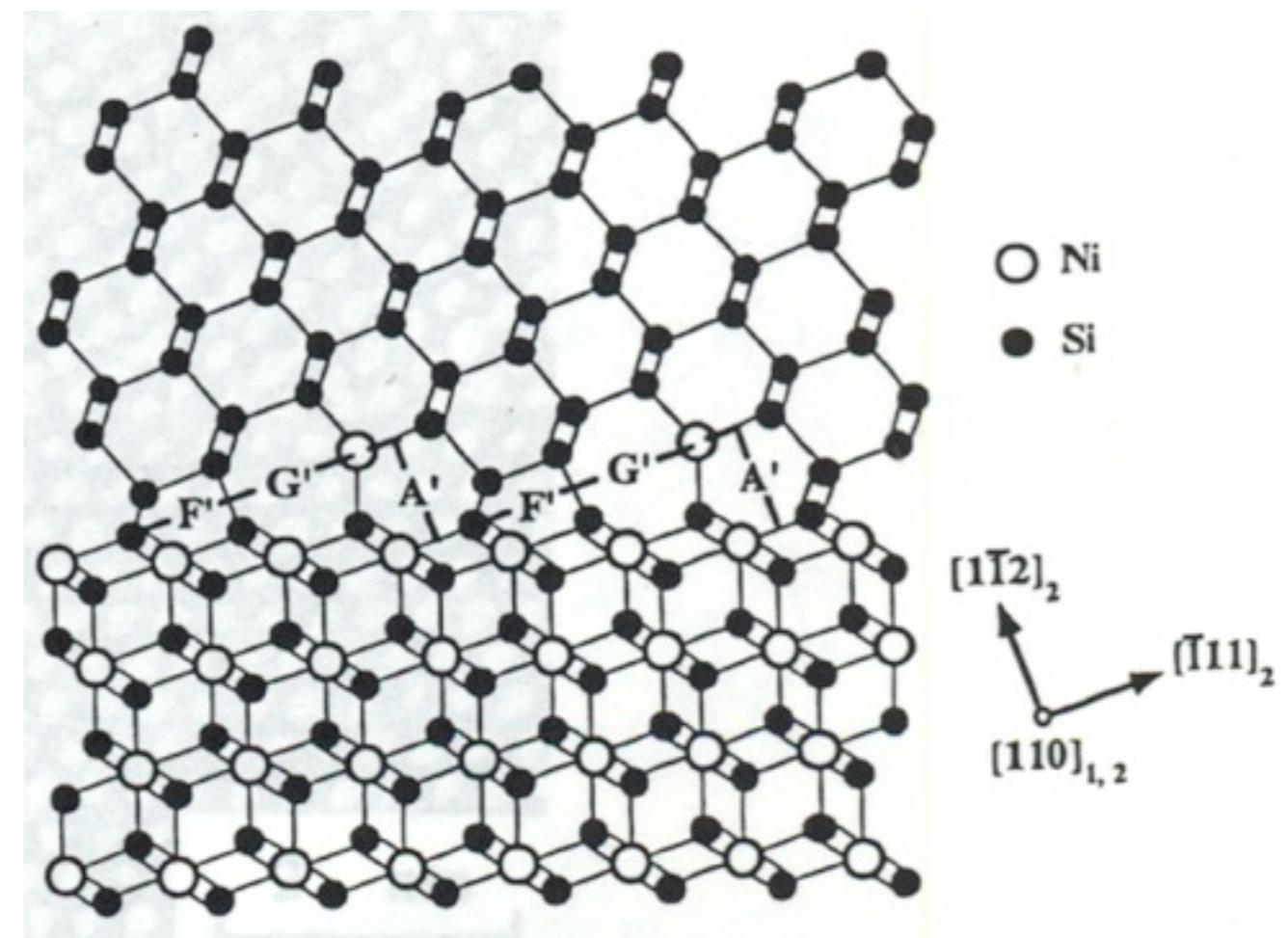
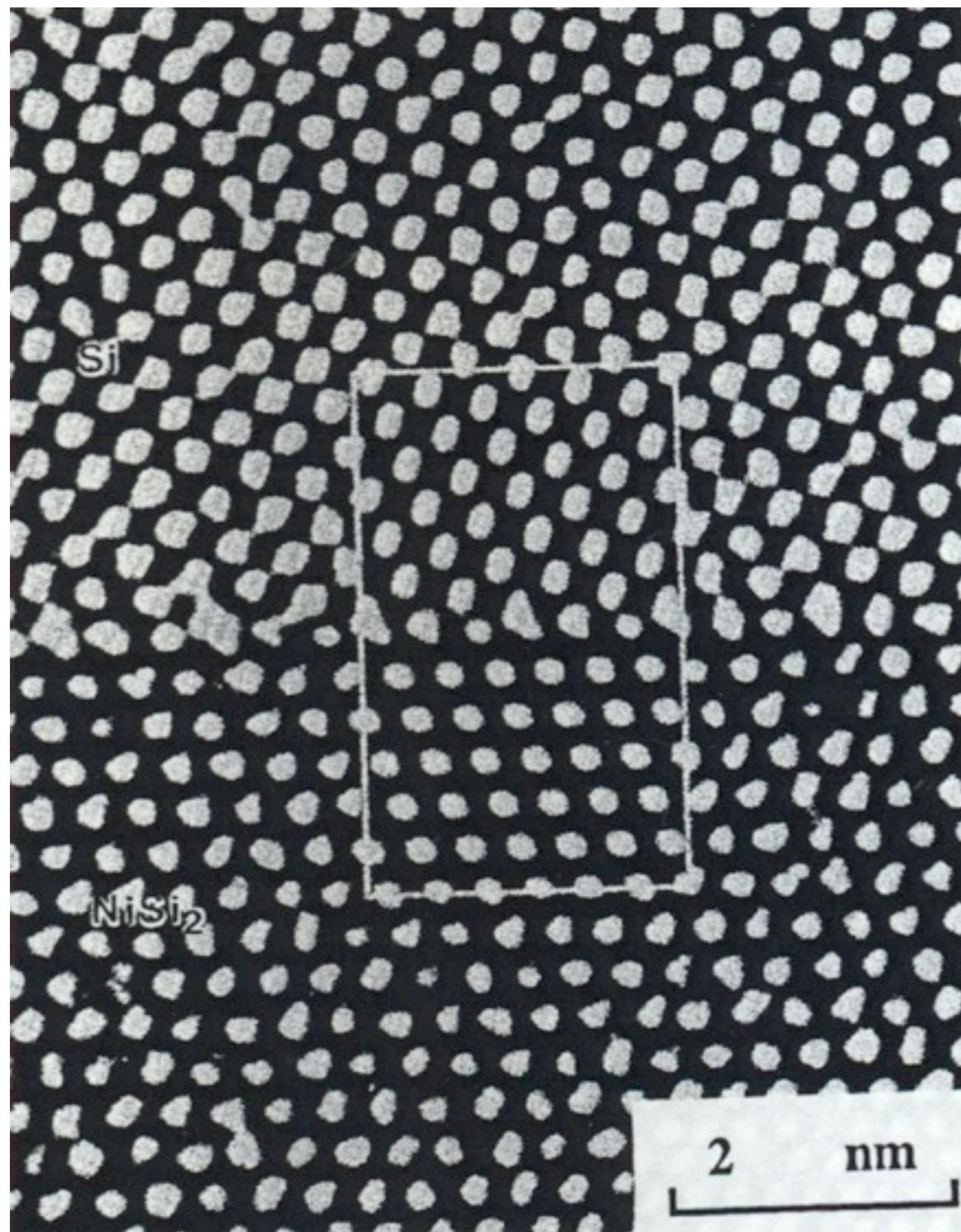
# Geometry of CTEM and STEM

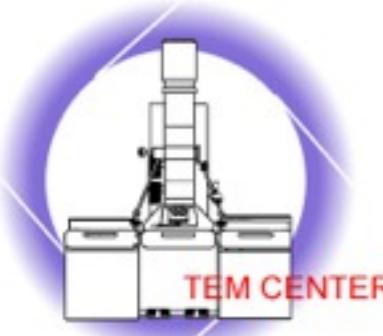




## Example: Si{115}/ NiSi<sub>2</sub> {111} Twin Boundary

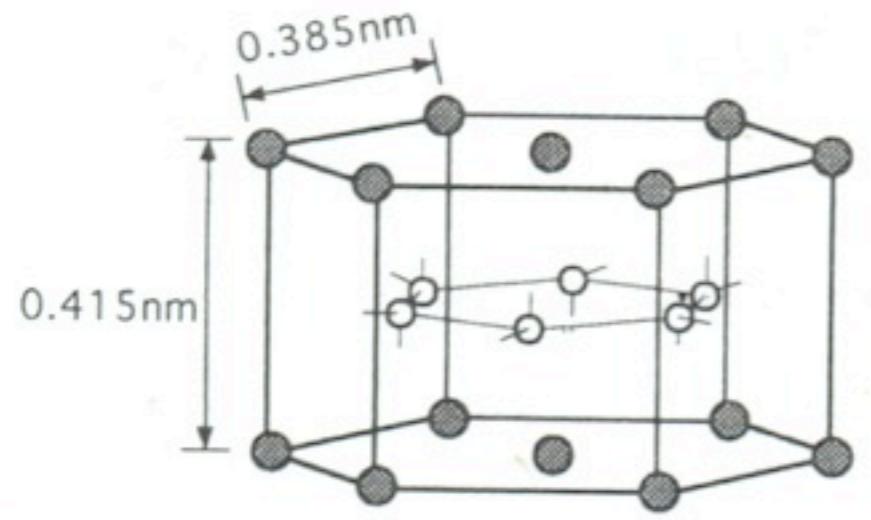
NTHU



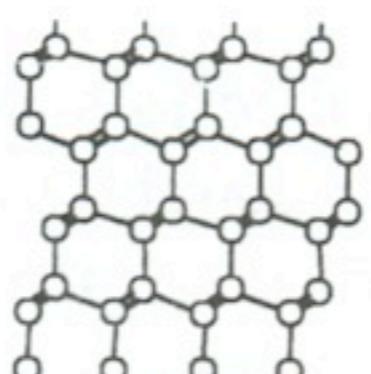
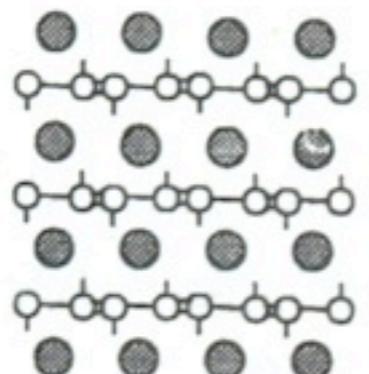


## Example: TbSi<sub>2</sub>/ Si Interface

NTHU

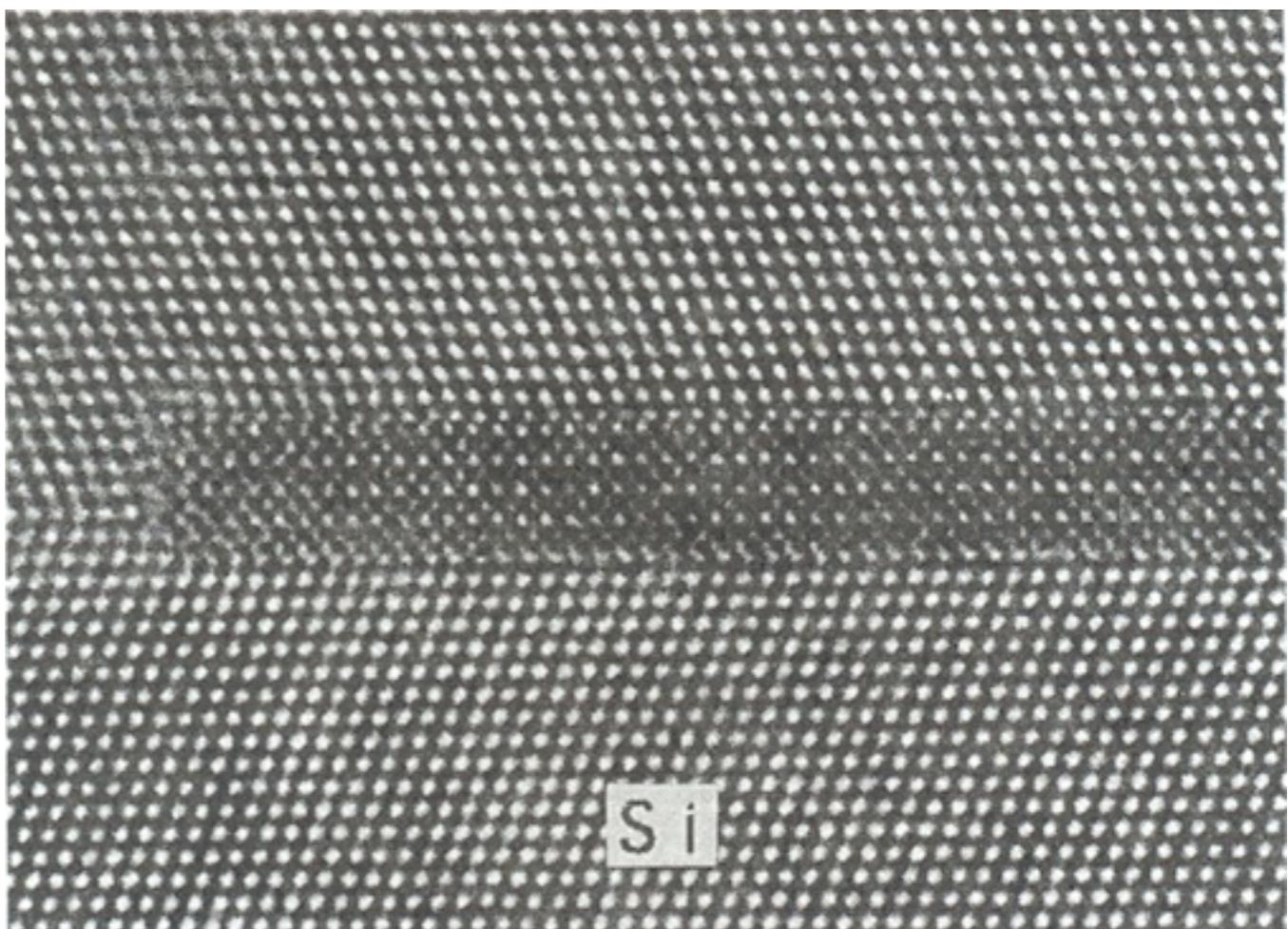


● Tb  
○ Si  
(a) [0001]  
[01 $\bar{1}$ 0]  
[10 $\bar{1}$ 0]

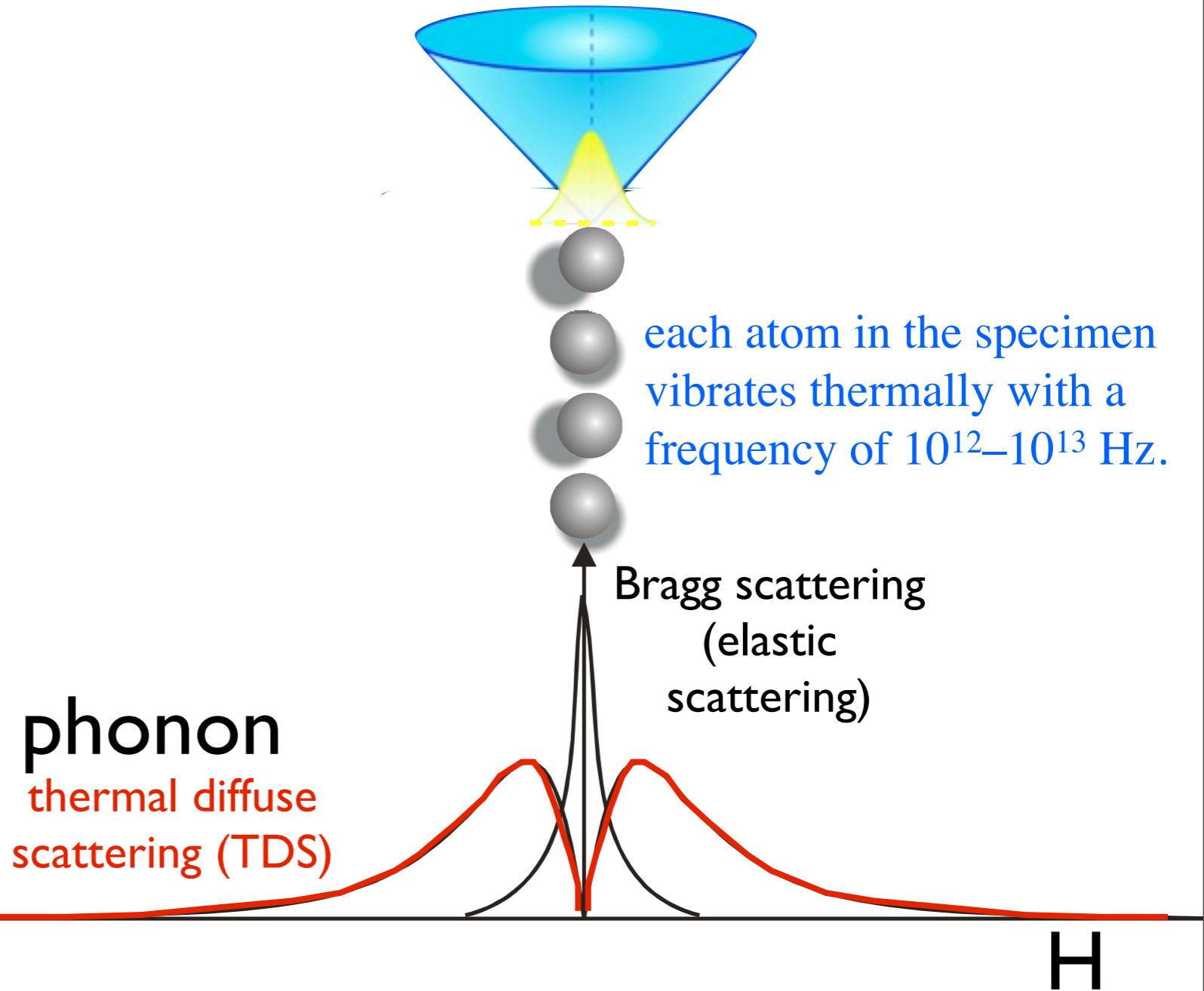
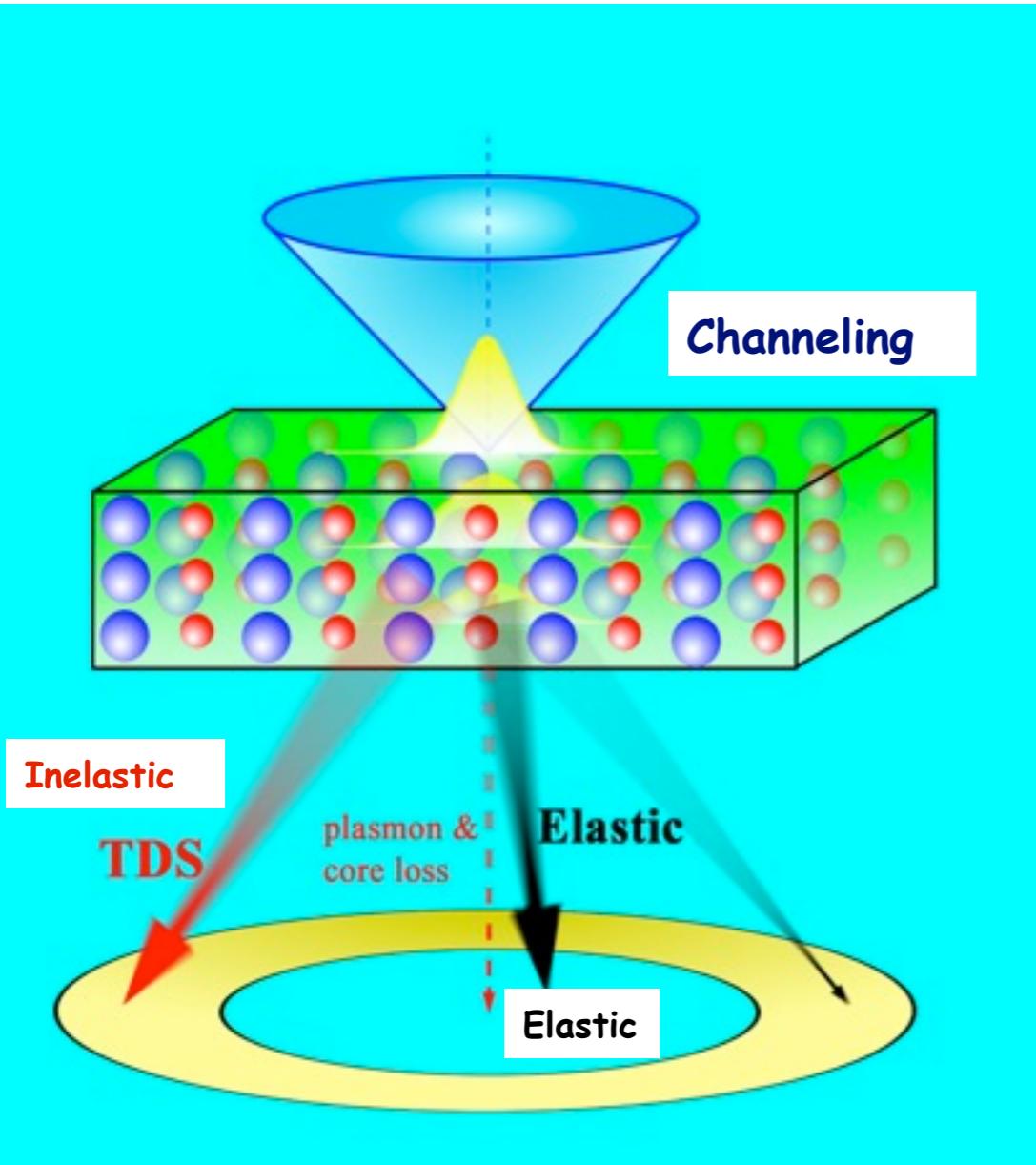


(b)

(c)

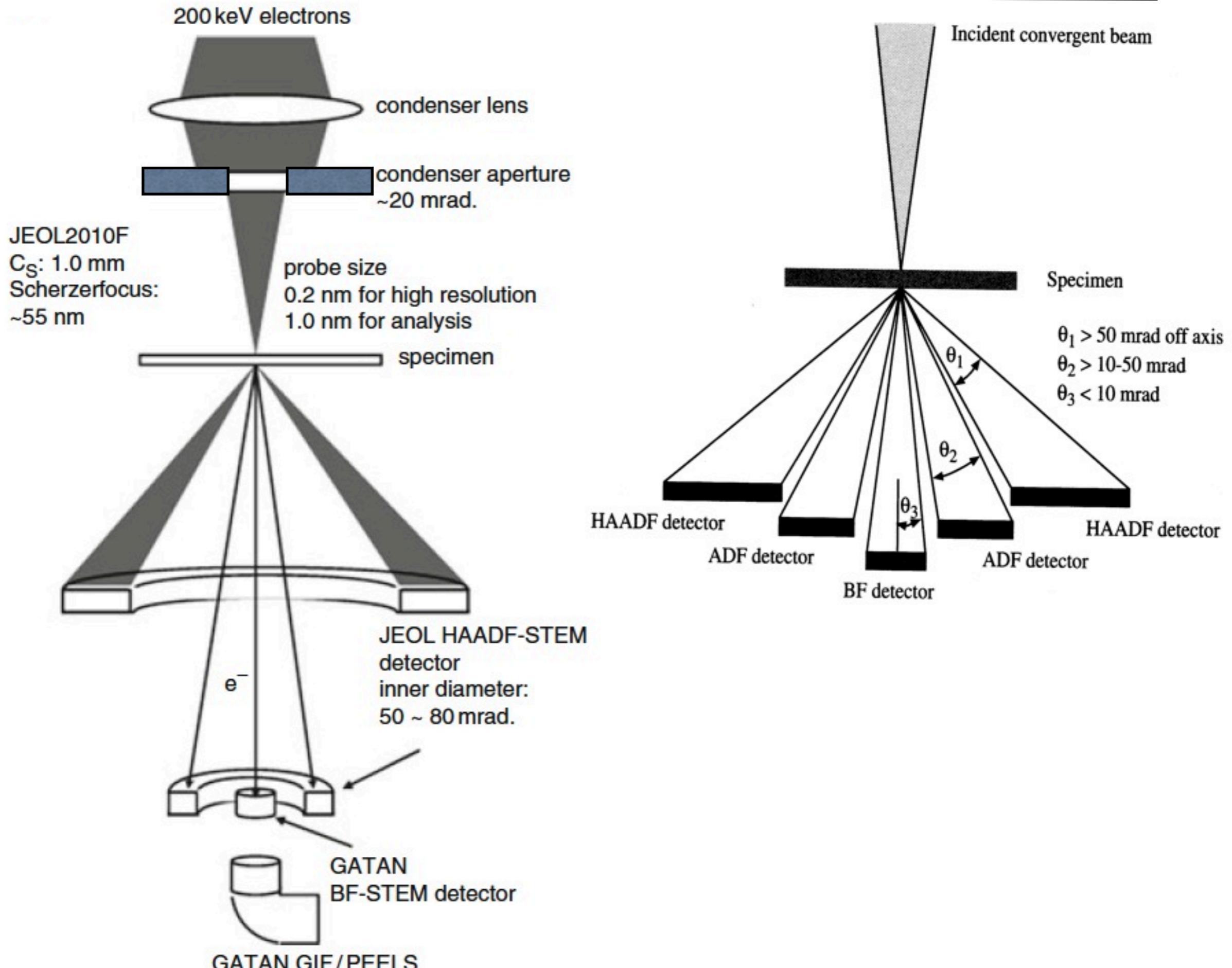


# thermal diffuse scattering (TDS)



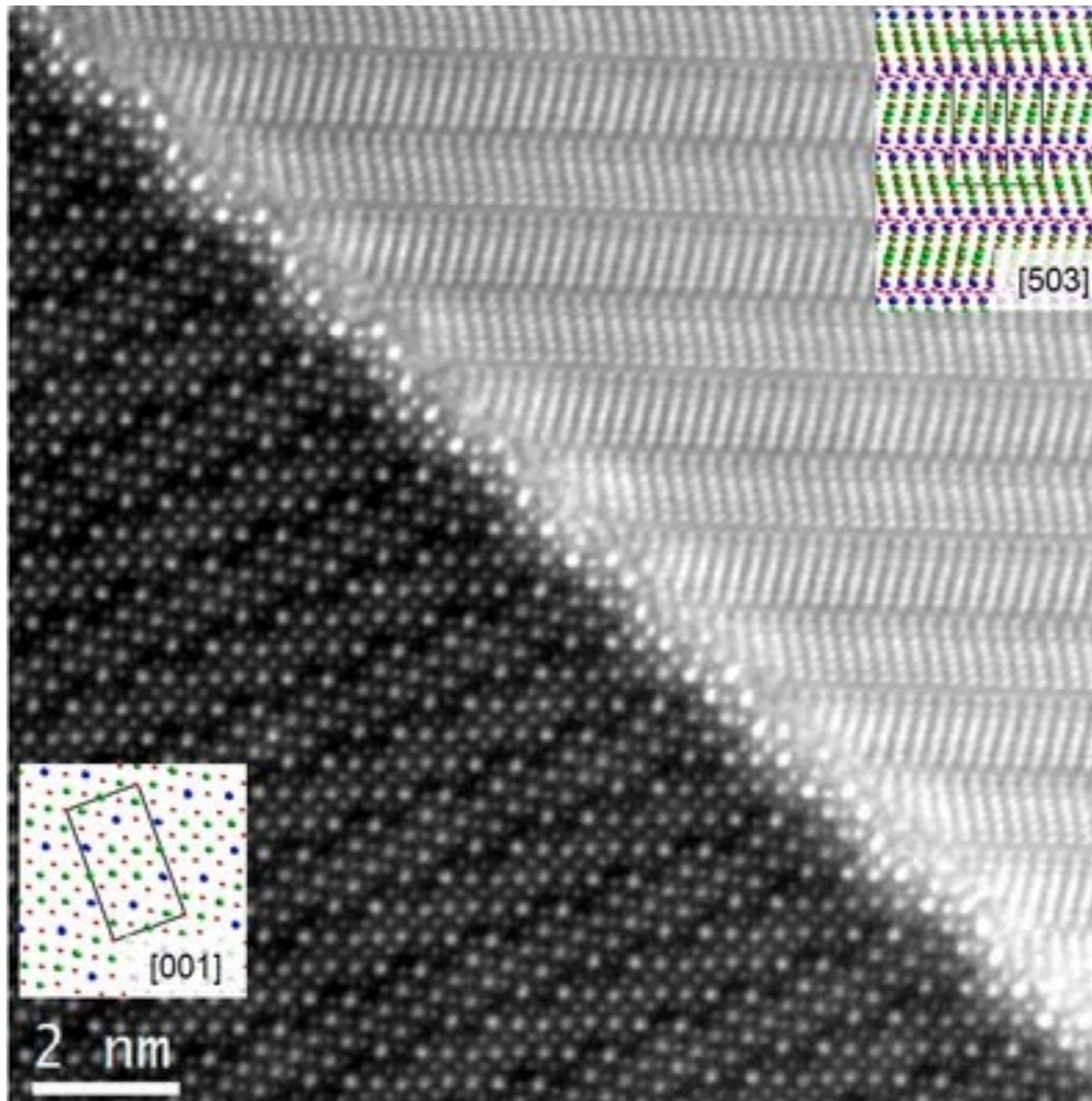
Thermal diffuse scattering (TDS), which is a signal used to form the image in HAADF-STEM and which was previously considered as “background intensity,” became a powerful source of information by using an HAADF detector.

# HAADF- STEM (High Angle Annual Dark Field)



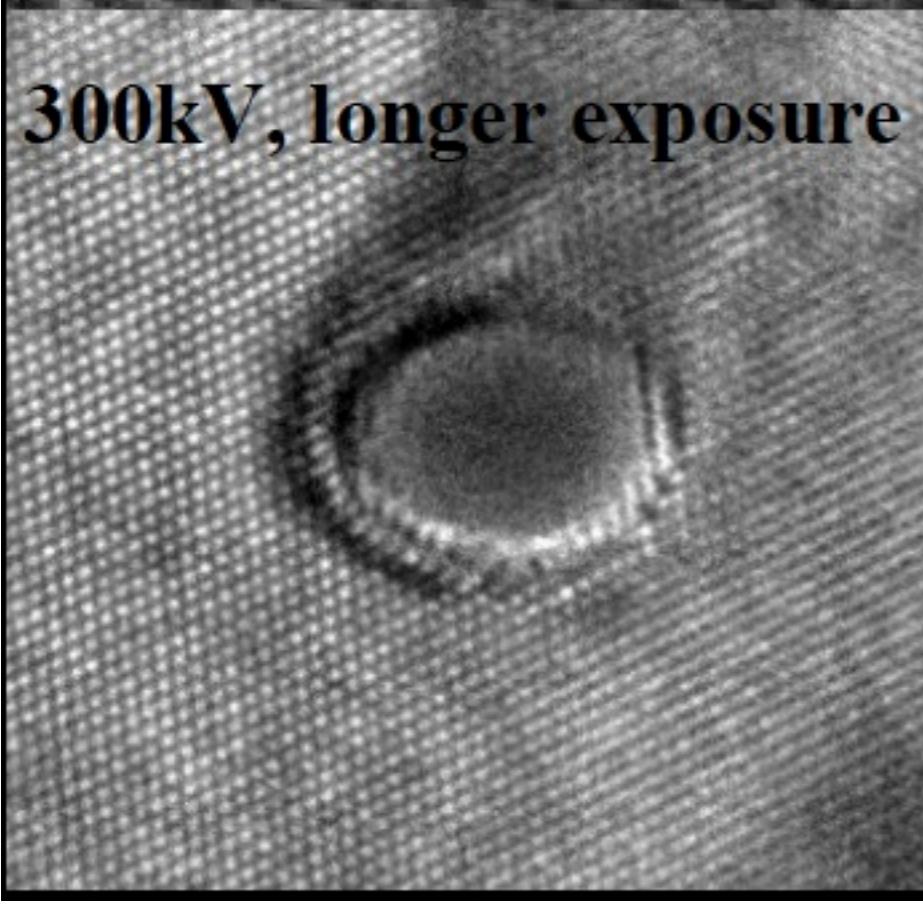
# Examples of STEM images

MAADF image of grain boundary in  $\text{Ba}_{6-3x}\text{Nd}_{8+2x}\text{Ti}_{18}\text{O}_{54}$  (BNT)



# Beware of Beam Damage!

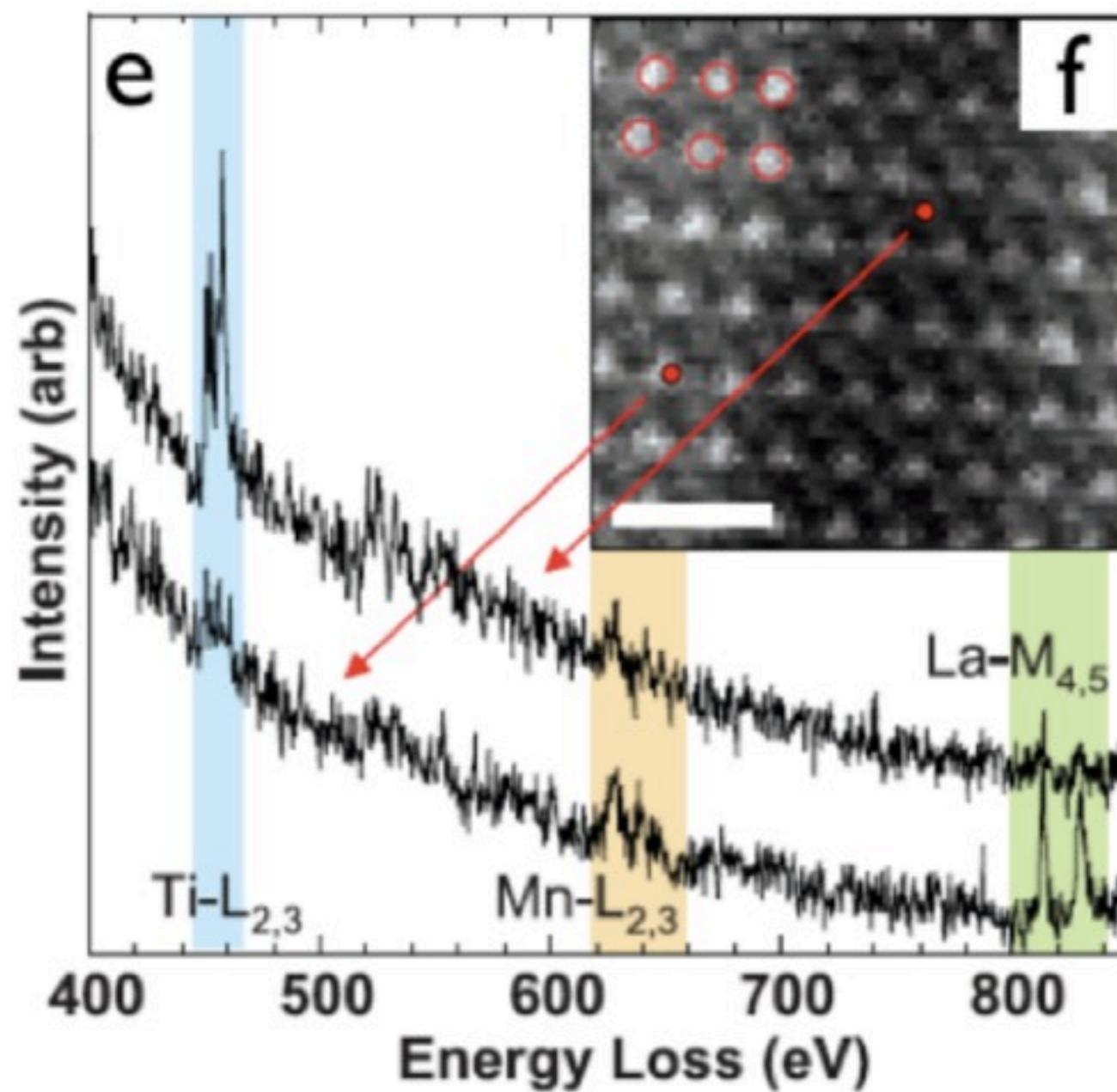
300kV, longer exposure



300kV, 1-2sec exposure

C. Kisielowski, NCEM Berkeley

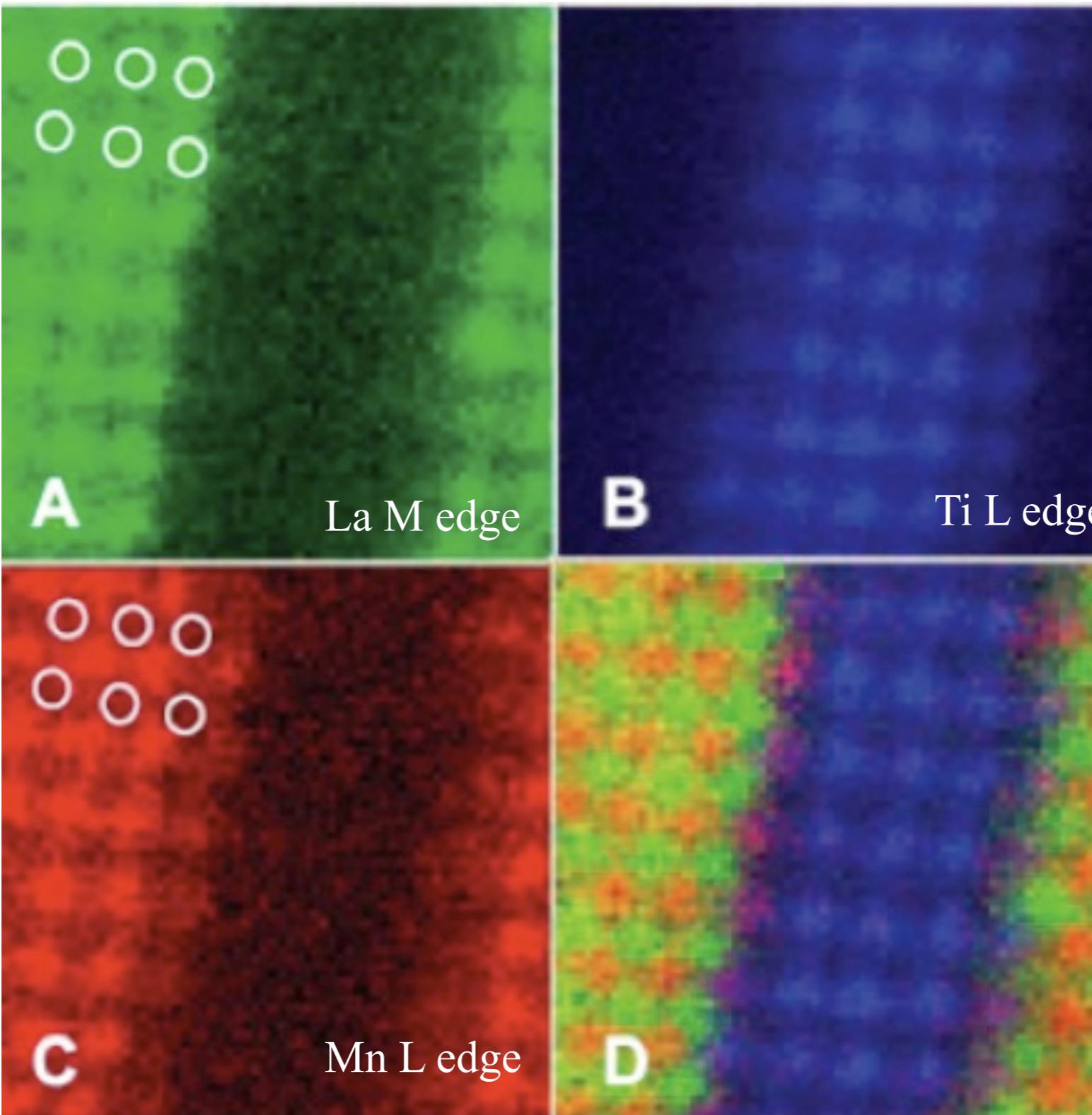
# Atomic resolution of EELS of $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3/\text{SrTiO}_3$ multilayer



- D. A. Muller, et al, SCIENCE 319 1073-1075 (2008)

# 8.7 Atomic Resolution Spectrum Imaging

## 8.7 Atomic Resolution Spectrum Imaging



Atomic resolution compositional and bonding maps